

معهد التراث العلمي العربي جامعة حلب ــ سورية





1474 دييع

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هبئة التعرين

أحمد يوصف الحسن جامعة حلب مالجمهورية المربية السورية سامي خلف الحمارته مؤسسة سبيشسونيان بواشنطن مالولايات المتحدة الامبركية وشسمة ين واشسمة المركز القومي للبحوث العلمية بباريس مفرتسا الحمادسليم سعيدان الجامعة الاردئية مصان عبد العميد صبرة جامعة هارفارد مالولايات المتحدة الامبركية ادوارد سء كتمدي مركز البحوث الامريكي بالقاهرة مصر دونالك هيسمل لندن مالملكة المتحدة

هيئة المحروين الاستشاريسان

صلاح اهمة جامة دمشق - الجمهورية العربية السورية البرت زكي اسكندر سهد ويلكوم لتاريخ الطب بلندن - انكلترا بيتسر ياخسمان المهد الالماني ببيروت - لبنان دافيله بينجسري جامعة براون - الولايات المتحدة الامبركية وريئيه تاتسون الاتحاد الدولي لتاريخ وفلسقة العلوم - فرنسا فسؤاد سسركين جامعة فوانكفورت - آلمانيا الاتحادية عبد الكريم شحادة جامعة حلب - الجمهورية العربية السورية معمله علم عاصمي اكاديمية العلوم في جمهورية تاجكستان - الاتحاد السوفياتي توفيق فهسله جامعة ستراسبورغ - فرنسا خوان فيرنيه جتيس جامعة برشلونة - اسبانيا جسون مسردوك جامعة مارفارد - الولايات المتحدة الامبركية راينس تابيلك معهد تاريخ الطبء جامعة همبولدت، يهلين - المانيا واينس تابيلك معهد تاريخ الطبء جامعة همبولدت، يهلين - المانيا فيسلمي هارتسن جامعة فراتكفورت - المانيا الاتحادية

تصدر مجلة تاريخ العلوم العربية عن معهد التراث العلمي العسريي مرتين كل عام (في فصلي الربيسج والخريف) ، يرجى ارسال نسختين من كل بحث أو متال الى : معهد التراث العلمي العربي حجامعة حلب ،

توجه كافة المراسلات النحاصة بالاشتراكات والإعلانات والأسسور الادارية الى العنوان تفسه • يرسل المبلغ المطلوب من خارج سورية بالسدولارات الامبركية بموجب شيسكات بأسم الجمعية السورية لتاريخ العلوم

اليمة الاشتراك السنوي:

المجلد الاول أو الثاني (۱۹۷۷ - ۱۹۷۸) بالبريد المادي المسجل: ۲۰ لبرة سورية أو ٦ دولارات أمركية بالبريد الجوي المسجل: ۴٪ لبرة سورية أو ١٠ دولارات أمركية

الجلد الثالث (١٩٧٩)

بالبريد المادي المسجل: كافة البلدان ١٠ دولارات أميركية بالبريد الجوي المسجل: البلاد العربية والاوروبية ١٢ دولارا أميركيا آسيا وأفريقيا ١٥ دولارا أميركيا الولارا أميركيا المركيا الولارا أميركيا

كافة حقوق الطبع محفوظة لمعهد التراث العلمي العربي

رست الذابي حبي فرانحت ازن في المثلث التالعت المذالزوايا المنيظ عتب الأصنيت لاع

نث وتحييت فعت ولأنوب

رسالة أبي جعفر [الحازن] في المثلثات العددية التي ننشرها اليوم، قد نجا منها نسخة فريدة جاءت ضمن مجموعة تمينة تحتفظ بها المكتبة الوطنية بباريس تحت رقم ٢٤٥٧ . وتضم المجموعة ٥ مقالا او قطعة ، زعم قبكه ان اكثرها بخط الرياضي المعروف ابي سعيد السجزي ؟ ومن منسوخات السجزي ما يحمل تاريخ كتبه ٣٥٨ ، ٣٥٨ ه او موضعه مدينة شيراز ولم تذكر هذه الرسالة في المؤلفات القديمة المحقوظة إلا انه يحتمل ان تكون هي احدى الرسائل التي دَلَّ عليها صاحب الفهرست ابن النديم اذ قال مجملا : كتاب المسائل العددية الابي جعفر الحازن الرابع المحبوب الخراساني المصاغاني الحازن ، وابو جعفر الحازن هو ابو جعفر محمد من الحسين الحراساني الصاغاني الحازن ، رياضي وفلكي ازهر في النصف الأول من القرن الرابع الهجري وتوفي بعيد ١٣٥٠ هـ وقد اشرئا الى جمل من حياته في مقال لنا سابق في هذه المجلة ٢ . وتبرجمة في الجزء الفرنسي من هذا المقال موضع الرسالة من تطور العلوم عند العرب ، وترجمة لمانيها مع بعض الملاحظات والايضاحات .

المخطوط :

تحوي الصفحة الواحدة من المخطوط ٢٢ سطرا او ما يقرب وقد كتب المخطوط بخط عادي واضح قليل الاخطاء . الكثير من الحروف غير منقطة سيما حروف المضارعة وقد

 الفهرست طبعة القاهرة دون تاريخ ص ٤٠٧ . و ذكر المسائل العدية ابن القفطي في الحبار الحكماه لقاهرة ١٩٣٦ ، ص ٢٥٩ .

ُ ٣ - الحبر عند العرب في القرئين التاسع والعاشر للسيلاد ، باللغة الفرنسية ، الحبلد الثاني (١٩٧٨) ، ص ٢٩ - ١٠٠ عادل انبويا

اثبتنا النقاط دون الاشارة الى ذلك إلا عرضا . نضع بعد الكلمة المصححة عددا وبعد مثيله في الحاشية الدفلي اللفظة كما وردت في المخطوط واذا شمل التصحيح بضع كلمات وضعناها بين علامتين به به والعدد داخل معكوفين مثل [١] يشير الى لفظة حدفناها من النص على انها زائدة وذكرناها في الحاشية بعد العاد وتدل العلامة] [ان بين المعكوفين ما فرجع انه من زيادة خاطئة للناسخ . وكثبنا بدل ج د ... بدلا من كل جد .. في الدلالة على الحطوط .

ثم انا قطَّعنا النص فيقرا تسهيلا للمطالعة وتمييزاً لمعانيه .

ويسرنا ان نتوجه هنا بخالص الشكر الى المكتبة الوطنية بباريس والآنسة الكريمة M.-R. Séguy حافظة المخطوطات الشرقية التي تفضلت وافنت لنا بنشر المخابوط .

> رسالة ابي جعفر [الحازن] في المثلثات القائمة الزوايا المنطقة الاضلاع ، باريس مخطوط ٧٤٥٧ ، ص ٢٠٤ أ ـــ ٧١٥ أ.

المالية المالية

1 4 . 2

رسالة الشيخ اي جعفر محمد بن الحسين ايده الله الله عبد الله بن علي الحاسب في البرهان على انه لا يمكن ان يكون ضلعاً عددين مربعين يكون مجموعهما مربعاً فردين بل يكونان زوجين او احدهما زوج والاخر فرد تتلوا رسالته اليه في انشاء المثلثات القائمة الزصلاع.

عند كذا والصحيح أن يقع الدّعاد " أيده ألفًا بعد أسم المرسل آليه; عبد أنثه بن علي أخاسب أيده ألله , و المثالة تمنى بالا عداد الصحيحة إلا في مواقع قاليلة يشير اليها النص .

- 1 1 كنت قد بينت أفيما كتبت به البك اخي ايدك الله في نشوء المثلثات القائمة الزوايا المنطقة الاضلاع انه لا يمكن ان يكون ضلعنا عددين مربعين يكون مجموعهما مربعاً فردين بل يكونان زوجين او يكون احدهما زوجا والآخر فردا ولم ابرهن على ذلك بشكل خطوطي فا فرأيت ان ابيته به ليقع تحت الحسس واذكر معه ما يتصل معناه بما كتبت ويزيده بيانا ويفيد الناظر فيه يقينا وهذا ابتداؤه فريد ان نبين كيف تنشأ الاعداد المربعة التي يكون مجموع كل عددين منها مربعا فنقدم لذلك ثلث مقدمات :
- 2 2 احداها ? انه لا يمكن ان يوجد عددان مربعان فردان يكون مجموعهما مربعا فان امكن فليكن عددا آ ب مربعين فردين وليكن مجموعهما وهو ج مربعا فيكون زوجا مما بيّن في الشكل الثاني والعشرين عن المقالة التاسعة ٢ من كتاب الاصول ونجعل د م ضلع آ و ز ضلع ب و طح ضلع ج ونفصل من طح مثل ز وهو كاح فلان طح زوج و كاح فردييقي طك واحدا او عددا فردا ونحسبه او ١٧ واحدا ٨ ونزيد في كاح مثله وهو لح فيكون ضرب طل في طك مثل مربع ط الله مثل مربع ط الله مثل مربع ده ولكن ضرب طال في طك مثل مربع ط الله مثل مربع حد ونفصل مسن مع ضرب ك ل في طك فمربع ط قد مع ضرب الله مثل مربع ده ونفصل مسن ده مثل طلا وهو م ه ونزيد فيه مثل م ه وهو مان فيكون ضرب دن في دم مع مسربع م ه مثل مربع ده ونسقط مربع م ه الذي هو مثل مربع طك في طك هر كان وضرب مثل ضرب ك ل في طك هر كان وضرب مثل ضرب ك ل في طك هر كان وضرب دن في دم عثل كان و كل واحد من دن دم زوج لان ده فرد وقد نقص منه واحد وزيد عليه واحد فيكون دن الزوج في نصف دم الزوج مثل نصف ك و وهو فرد لانه مثل ز الفرد فليس ك ط بواحد .

ة - أي باستممال الخطوط الدلا لة على الاعداد كما في مقالات اقليدس ٧ ، ٨ ، ٩ مثلا .

١ - تشو

۲ د با با

۲ – پلیاره

۽ – تندا

و د تندأ

٩ - احداهما ٧ - ني النص الثامة والتصحيح جاء في الحاش
 ٨ - فد ما ١٠

173 عادل اليويا

الىعدد مربع ومضروب احدهما في الآخر اربع مرات ومضروبه فيه مرة واحدة عددان وهما ايضا اقل هذه الاعداد من قبل انا جعلنا العددين المطلوبين اللذين افزلناهما موجودين اقل عددين مربعين وجب أن يكون كل وأحد من العدد المركب والفضلة مربعا ويكون الفضلة واحدا? اذ هر اقل المربعات والعدد المركب اربعة اذ هي اقل الاعداد المربعات وان يكون العدد الفرد منه ثاثة وهو ضلع احد المربعين المطلوبين والمربع تسعة ويكون الفضلة . فقـــد ظهر من ذلك ان فضل ما بين المربعين اللذين هما اربعة وواحد وهو ثلثة ضلح احمد المربعين المطلوبين وان مضروب ضعف ضلع المربع الاقل وهو اثنان في ضلع المربع الاكثر الذي هو اثنان وهو اربعة ضلع المربع الآخر من المربعين المطلوبين وان مجموع المربعين الذي هو خمسة ضلع مجموع المربعين المطلوبين .

وهذا الطريق مطرد في وجود سائر الاعداد المربعة التي يكون مجموع كل اثنين منها مربعًا ، فانا اذا اخذنا فضل ما بين التسعة والواحد المربعين وهو ثمنية واخذنا مضروب ١٢٠٦ ضعف ضلع الواحد في ضلع التسعة وهو ستة وضربنا كل واحد في مثله اجتمع اربعة وستون وستة وثلثون وكان مجموعهما ماية وضلعه عشرة مثل مجموع المربعين الاولين 8 إلا ان ضلع كل واحد من المربعين ومن مجموعهما ضعف كل واحد من المربعين الاولين ومن مجموعهما فاضلاعها مشارك بعضها لبعض ﴿ . وكذلك كل عددين مربعين يكون نسبـــة ضلع احدهما الى ضلع الآخر كنسبة اربعة الى ثلثة فانهما يكونان مركبين من هذين العددين ويعد ضلع مجموعهما الحمسة وذلك بيِّن . وكذلك لا يعسر وجود الاعداد المربعة الى اذا زدنا على كل واحد منها واحدا عد مجموعهما الحمسة i .

⁷⁻⁶⁻

٧ - مجموعها
 ٨ - ضلع
 ٣ - يسني ان ١٠ مجموع المربعين ألا ساسيين ١ و ٩ اللدين نشأت عنهما الاعداد المربعات الثلاث

ط - أي أن ج م ١٠ ضعف ج ٤ ٥ ألِّي تشأت من المربعين الاساسيين ١ و ٤

i – يمني ان المربع الاساسي ١ لما اعذمع ؛ او مع ٩ نشأ عن ذلك ١ + ٤ = ه ١ + ٩ = ١٠ والخمسة تمد ہ بر ۱۰ و لا يصمب ان نجد مربعات مثل ٩٤ ، ١٦٩ ، ١٩٤ ، ١٤٤ ، اذا انسيفت الى ٢ نشأ عن ذلك اعداد تعدما ، رهي مربعات کل هدد پنتهي برقم ۲ ، ۴ ، ۸ ، ۷

- آ فينبغي ان نطلب غير ذلك وهو ان نطلب العددين اللذين بعد تسعة وستة عشر ؤ واذا كان الواحد والتسعة عسد بجموعهما الخمسة فنأخذ العددين المربعين اللذين يليان الواحد والاربعة وهما اربعة وتسعة فيكون فضل مابينهما وهو خمسة ضلع احد المربعين المطاوبين ومضروب ضعف ضلع الاربعة وهو اربعة في ضلع النسعة وهو اثنا عشر ضلع المربع الآخر والخمسة والاثنا عشر اصل الاعداد الي كل اثنين منها على نسبتهما فاحد المربعين خمسة وعشرون والآخر ماية واربعة واربعون وضلع مجموعهما وهو ماية وتسعة وستون ثلثة عشر وهي مجموع المربعين المأخوذين. ونطلب العددين التاليين للاربعة والتسعة وهما واحد وستة عشر فيكون ضلع المربع الاقل ثمنية وضلع الاكثر خمسة عشر وضلع مجموعهما وهو مايتان وتسعة وثمنون سبعة عشر فهي مجموعهما وهو مايتان وتسعة وثمنون سبعة عشر فهي مجموعهما وهو مايتان وتسعة وثمنون سبعة عشر فهي مجموعهما وهو
- 8 وعلى ذلك تنشأ اضلاع هذه المربعات بان يؤخذ كل عددين مربعين يكونان اقل عددين على نسبتهما واقل عددين على نسبة عددين هما متباينان مثل الواحد والاربعة فالهما متباينان لان الواحد يعد كل عدد و كذلك اربعة وتسعة وواحد وستة عشر فيعمل بهما ما وصفتا من العمل فينشأ منها الاعداد المربعة الي يكون مجموع كل عددين منها مربعا من ٧٠ غير ان يكون بين عددين وعددين | منها عددان على صورة العددين الللين قبلهما لا يوجد مثل ٢ ستة عشر وتسعة عددان بهذه الصورة غيرهما ولاغير ٣ ماية واربعين وخمسة وعشرين .
- و فان اخذ اربعة وماية واحد وعشرين وهما متباينان ومجموعهما تعده الحمسة فانه ينشأ منهما عددان مربعان مجموعهما مربع لا يعد ضلعيهما ضلعا الستة عشر والتسعة بالسوية وهما اربعة واربعون وماية وسبعة عشر وعلة ذلك ان ماية وخمسة وعشرين مركبة من الحمسة والحمسة والعشرين وكل عدد هذه صورته فانه ينقسم بعددين مربعين وكل عدد هذه صورته فانه ينقسم بعددين مربعين مربعين مرتين كما نبيس ذلك فيما بعد فقد انقسم ماية وخمسة وعشرون

^{21 - 1}

ق - بعد ان استعمل ۲۸ و ۲۶ و ۲۸ و ۲۸ و ۲۸ و ۲۸ الركيب المربعات منها فانه يستصل ۲۲ و ۳۳ و ۱۳ و ايس النص و انسحا على كل حال

ع - فحوى الكلام الله أن تحصل على عددين سناسين لعددين سابقين فلن نحصل على عددين سناسين ١٩٠١، ٩.
 او ٩٤ و ١٣٥٠ الـــة .

^{44 - 4 1}H - 4

مرة اولى بخمسة وعشرين وبماية ومرة اخرى باربعة وبماية وأحد وعشرين فكل عدد يكون يهذه الصورة فسبيله سبيل الخدسة فان ضلعي مربعي تسميها وهما اربعة وثلثة هما اصلان للاعداد المركبة من الخمسة مثل الماية فانها تنقسم يستة وثلثين واربعة وستين وضلع ستة وثلثين مركب من الاربعة والستة والثمنية يعدهما الثلثة والاربعة بعدد واحد وهو الاثنان فيه بحي ان تعلم ذلك من خواص هذه الاعداد .

10 فان كان العددان المربهان زوجين نقصنا من ضلع مجموعهما ضلع اقلهما فيكون الباقي زوجا ونضيف نصفه 1 وهو الفضلة الى ضلع المربع الاقل فيكون ضرب مجموعهما في الفضلة مربعا اذ كان ضربه في اربعة اضعافها كما بيننا مربعا وضلعه نصف ضلع المربع الاكثر من المربعين الاولين . فقد ظهر مما قلنا ان كل عدد مربع ينقسم بعددين مربعين فان ضلعه ينقسم بعددين مربعين او ينقسم بعددين مربعين الولين .

11 وقد يمكن ان نجد عددين مربعين مجموعهما مربسع وثلثة اعداد مربعة مجموعها على ١٢٠٧ مربع | وكذلك اربعة وخمسة والى غير نهاية فوجود عددين مربعين مجموعهما مربعا ناخذ عددين مربعين ونضرب احدهما في الآخر فيخرج احد المربعين و ونأخذ مربع نصف فضل ما بينهما ١٢٠٠ فيخرج المربع الآخر ويكون مجموعهما مربعاً ضلعه نصف الاكثر مع الاتخل على مثال ذلك ان نفرض اج ب ب عددين مربعين ونجعل د مضروب اج في ب على ه فاقول ان مجموع [] د ومربع هب ضلعه هج . برهان فلك ان ضرب اج في ب ج وهو د مربع كا تبيئن في المقالة التاسعة من كتاب الاصول عن وضرب اج في ب ج مثل ضرب اب في ب ج ومربع ب ج فضرب اب في ب ج اللذي هو مثل ضرب هب في ب ج مرتين مع مربع ب ج مثل د ولكن ضرب هب فقد ومربع هب مثل عددين مربعين مجموع د ومربع هب فقد وجدنا عددين مربعين مجموعهما مربع ضلعه هج فان كان اج ب ج مربعين زوجين فقد وجدنا عددين مربعين مجموعهما مربع ضلعه هج فان كان اج ب ج مربعين زوجين فقد وجدنا عددين مربعين مجموعهما مربع ضلعه هج فان كان اج ب ج مربعين زوجين

5 41 - a

ا – لعقه أي تعبث الياقي

٦ - وتضرب تصف اكثرهما في مثله

m - أي تصف عبسوع الأكثر مع الاقل

4 -- le

ع ليس في المغالة التاسمة قضية تنص على ذلك إلا أن الدعوى

1 - ac 14

حالة خاصة من القضية : مضروب سطحين متشاجين يكون عددا مربعا (الشكل الاول من المقالة التاسعة) .

ا - مر بعين

کان کہ ومربع ہب زوجین لان ب یکون زوجا وان کان آج بج فردين كان د مربعا فردا ومربع هب زوجا لإنه لا يجتمع من عددين مربعين [فردين] عدد [٩] مربع . وان كان احدهما زوجا والآخر فردا كان د مربعا زوجا ووقع مربع هب في عدد غير صحيح ولم يُستم عددا مربعا لان العدد ما ركب من اعداد صحاح ولمذلك برى اصحاب الجبر ان يعبروا عما له جلر بمال لمعيم ماصح من الاعداد المجدورة وما به كسور.
وفي وجود ثلثة اعداد مربعة مجموعها مربع ناخذ ثلثة اعداد مربعة يكون ب فردين كان د مربعا فردا ومربع هب زوجا لإنه لا يجتمع من عددين مربعين اكثرها اكثر من مجموع الاقليّن ولتكن آب بج جد وننصف آد على ﴿ وَنَجْعُلُ زَ مُصْرُوبُ آبَ فِي بِجَ وَ حَ مُصْرُوبُ آبِ فِي جَ دَ فاقول ان مجموع عددي ز ح وهما مربعان مع مربع هد مثل مربع هب. برهان ذلك ان ضرب اب في بج وضرب اب في جد مثل ضرب اب في دب فضرب اب في دب مثل عددي ز ح ، ولكن ضرب اب في دب اب في دب مثل عددي ز ح ، ولكن ضرب اد في دب مثل دب مرتين سرتين سر

نحد أعددا كثيرة مربعة مجموعها مربع ، ولإنا نحتاج فيما نأتي به من بعد الى عددين مربعين ضلع مجموعهما مربع ٥ والى عددين مربعين مجموعهما مربع وضلع احدهما مربع ٥ فإنا نبيَّن وجود الاولين هكلًّا : كل عددين مربعين مجموعهما مربع فانه آذا ضرب احدهما في الآخر اربع مرات اجتمع أكثر المربعين اللذين ضلع مجموعهما مربع ٩ واذا أخذ فضل ما بينهما وضرب في مثله اجتمع المربع

بما قدّمنا هلكلها ازواج او بعضها ازواج وبعضها افراد وبمثل هذا الطريق

ع - او شاپه ۳ - « الذي هو مثل ضرب ه ب أي د ب مرتين » 'E = 1' + 1' - - p 1> = Tun+ Tun - a * E * W $^{Y}(^{Y}_{\overline{c}}-^{Y}\psi)=^{\eta}\psi$

الأقلُّ. مثال دلك تسعة وسنة عشر وهما اقل عددين مجموعهما مربع وأذا ضرب أحدهما في الآخر اربع مرات اجتمع خمس ماية وستة وسبعون وهي اكثر المربعين وضعه مضروب سنة في اربعة والمربع الاتن تسعة و ربعون وضلعه سبعة ، وهو فضل ما بين تسعة وستة عشر وضلع محموعهما ، وهو ستماية ^ه وخمسة وعشرون ، خمسة وعشرون؟ .

واما وجود الآخرين فعلي هذه الصفة : كل عدد ضلعه مربع اذا ضرب في ربع عدد ضلعُه مربع اربعٌ مرات اجتمع ذلك العدد نفسه ُ الذي ضلعه مربع ولكن الواحد مربع ضلعه مربع والستة عشر مربع ضلعه مربع واذا ضرب الواحد في اربعة اربع مرات اجتمع ستة عشر وهي اكثر المربعين" وضلعه مربع ونأخذ فضل ما بين الواحد والاربعة ١٢٠٨ فنضربه في مثله فيكون | المربع الاقل: ومحموعهما خمسة وعشرون وهي اول عدد يقسم بعددين مربعين ضلع احدهما مربع .

واذا اردنا وجود عدد آخر شبه بخمسة وعشرين طلبنا عددين نسبة احدهما الى الآخر نسبة عدد مربع الى عدد مربع وفضل ما بينهما مربع ليكون مضروبه" في مثله مربعاً ضلعتُه مربع . واول عددين بهذه الصفة ثلثة واثنا عشر فان نسبة احدهما الى الآخرنسية واحد الىاربعة وفضل ما بينهما مربع وهو تسعة والواحد والاربعة قسما الحمسة وفضل ما بينهما ثلثة واذا ضرب كل واحد من القسمين في ثلثة كان مجموع ذلك خمسة عشر مثل ما يجتمع من ضرب خمسة في ثلثة فخمسة عشر ضلع العدد الذي ينقسم بعددين مربعين ضلعًا حد هما مربع وهو مايتان وخمسة وعشرون واحد قسميه مضروب اثني عشر فيمثمها وهو ماية واربعة واربعون والآخر مضروب تسعة في مثلها وهو «ربع ضلعه مربع .

فَانَ اردَنَا عَدُدَا ثَالُمُ مِنْ هَذِهِ الْأَعْدَادِ وَقَدَ قَدَمَنَا أَنَا أَذَا ضَرِينًا عَدُوا ضَلِعَه مربع في ربع عدد ضلعه مربع اجتمع عدد ضلعه مربع لضربستة عشر في ربعها اربع مرات فيكون مايتين وستة وخمسين وضلعها مربع وهو ستة عشر ونأحذ فضل ما بين آربعة وستة عشر وتضربه قي مثله فيكون ماثة واربعة واربعون ومحموعهما اربعماية وضلعه مضروب اربعة

x = 1 اللي ذكره في دموى القشية وسيناه من x = 1 و د اي ما سمينه من x = 1و ساي ما سيباد ص ^{او} ۽ تا - مصروبه اي ممروب الفضل

^{1 - 1800}

٦ - في الحامل هذا جملة السرح خاطئة . ه د مایدان

في خمسة فهو عدد مربع ينقسم بعددين مربعين ضلع احدهما مربع وان ضربنا خمسة وعشرين في ستة عشر كان ايضاً اربعماية

ال وايضا اذا ضربنا خمسة في عدد نسبته الى ثلثة نسبة عدد مربع الى عدد مربع المجتمع عدد ينقسم نقسمين على نسبة عدد مربع الى عدد مربع وفضل ما بينهما مربع ومضروب احدهما في الآخر مربع وذلك مثل خمسة في اثني عشر قاله ستون وهي تنقسم بائني عشر وثمنية واربعين وثمنية واربعون في اثني عشر ربع مرات مربع وهو الفان وثلثماية واربعة والمعتقدة والمعتق

ب وجمعة القول انه اذا اخل عددان ا مربعان لاحدهما ربع وعمل بهما ما تصيف وجد العدد المطاوب . مثان ذلك تسعة في ماية واربعة واربعين فان ضلع ذلك وهو ستة وثلثون مربع واذا جعل احد العددين ستة وثلثين والآخر تسعة وعمل بهما وبفضل ما بينهما مثل ما تقدم اجتمع عهما الفان وخمسة وعشرون وانقسمت بمربعير ضمع احدهما مربع وهو الف ومايتان وستة وتسعون وضلعه ستة وتشون والآخر سبع ماية وتسعة وعشرون وضلعه سبعة عشر واربعة .

وفي وجود ذلك طريق آخر وهو ان مضروب اثنين وثلثين في ثمنية ضلعه مربع وهو ستة عشر فإن اخذ ربعه وهو اثنان وجعل احد العددين والآخر اثنين وثكثين حدث من ذلك الف وماية وستة وخمسون وانتسم بمأتين وستة وخمسين وبتسع ماية إلا أن طريق هذا الباب لا يجري على نظام بالمطريق الذي ذكرناه وله طريق يلزم النظام في المربعات التي اضلاعها ازواج وذلك ان يجعل احد العددين عددا مجلورا له ربع والآخر ربعه واولها ربعة وستة عشر واربعة وستون . وقد بينا فيما تقدم انه لا يمكن ان يوجد عددان مربعان يكون مجموعهما مربعا فيكون ضلعاهما زوجي الزوج والهما اذا كانا زوجين امكن ان يكون احدهما زوج الزوج والقرد او القرد او روج الزوج والفرد ، وان كان احدهما فردا امكن ان يكون الخهما في الآخر زوج الفرد او روج الوج والفرد ، وان كان احدهما فردا امكن ان يكون الجهما في الآخر مرتين زوج الوج والفرد ، والفرد . والملك يكون مضروب حدهما في الآخر مرتين زوج الروج والفرد ابدا .

۷ → اریمون

20 واقول ان كل عدد ينقسم بعددين مربعين فان ضعفه ينقسم بعددين مربعين . برهانه ان كل عددين نحتفين فان مجموع مربعيهما مثل مضروب احدهما في الآخر مرتين ومربع على اوجه الله ينبيس في الوصع العددي في الشكل الخامس والتاسع من المقالة السابعة على الوجه الذي بنيس في المقالة الثانية من كتاب الاصول ، فيكون مضروب احدهما في الاخر اربع مرات وصعف مربع عضل ما بيسهما مثل ضعف محموع مربعيهما ، ولكن مجموع مربعيهما ومضروب احدهما في الآخر مرتين مثل مربع مجموعهما فاذن ضعف محموع مربعيهما فاذن ضعف محموع مربعيهما يزيد على مربع محموعهما بمربع فضل ما بينهما فالملث كل عدد ينقسم بعددين مربعي فان ضعفه ينقسم بعددين مربعين وضعف هذه الوجه كل عدد ينقسم بعددين مربعين الربعين الاولين وضلع الاقل هضل ما بين الضبعين . وعلى هذا الوجه كل عدد ينقسم بعددين مربعين هان ضعفه ينفسم بعددين مربعين وضعف ضعفه و كذلك الى غير ينقسم بعددين مربعين هان ضعفه ينفسم بعددين مربعين وضعف ضعفه و كذلك الى غير المهاية .

واقول ايضا أن كل عدد زوج ينقسم بعددين مربعين فان قصفه ينقسم بعددين مربعين

22 وبعد تقديم ما قدمناه تصير الى الغرض الذي نحوناه وهو ان نبيّن اذا فرض لنا عدد من الاعداد كيف **نطلب عددا مربعا اذا زدنا عليه العدد المفروض ونقصناه منه كان ما بلغ**

وما بقي عددين هربعين . فسنزل وجود الاعداد المربعة الثنثة وهي الاقل والاوسط والاكثر على جهة التحليل فاقول ٪ العدد المربع الاوسط ينقسم بعددين مربعين لان المجموع منه ومن العدد المقروض مربع واذا زيد عليه فضل ما بين العدد الاوسط والعدد المفروض وهو كما قلمنا مربع اجتمع ضعف العدد الاوسط فهو اذاً زوج فقد انقسم مع ذلك بعددين مربعين فنصفه ابضاً ينقسم بعددين مربعين . فقد ظهر من دلك ان كل عدد [مربع] يزاد عليه عدد مفروض وينقص منه فيكون المحتمع والباقي عددين مربعين فآله ينقسم بمددين مربعين وأقول أن العدد المفروض هو ضعف العدد الذي يحيط نه ضلعا العددين المربعين اللذين ينقسم نهما العدد الاوسط . برهان ذلك الله فضل المربع الاكثر على العدد المربع الاقل وهو ضعف العدد المعروض مثل مضروب مجموع ضلعيهما في فضل ما بيمهما مما يتمين في الوضع العددي على الوجه الدي بُيِّن في الشكل السادس من المقالة الثافية من كتاب الاصول ولكن محموع ضلعي العددين المربعين اللذين ينقسم بهما العدد الاوسط هو الضلع الاكثر من صلعي المربعين اللذين ينقسم بهما ضعف العدد الاوسط والضلع الاقل هو فضل ما بيهما كما بيَّنا فيما تقدم والمثلك يكون العدد المعروض ضعف مضروب احد الصَّلعين في الآخر فالعدد المفروص ضعف العدد الذي يحيط به ضلعا المربعين اللَّذين ينقسم بهما العدد الاوسط وهوروح فقد انعكس آخر؟ التحليل على انه متى فرض لما عدد وطلب منا عدد مربع ان زدنا عبيه ذلك العدد ونقصناه منه كان المجتمع والباقي مربعين وجب إان يكون العدد المعروض زوجا والا يكون نصفه أوَّل لانه بحيط به عددان مركبان والعدد الاول غير مركب والا يكون نصفه يضا فردا وان كان مركبا لانه يحيط به عددان فردان ولا يمكن ان يكون مجموع مربعيهما مربعا فان كان العدد المفروض على احدى الحالين كان ما طلب محالاً .

لا فقي ان يكونكلا العددين المربعين اللذين ينقسم بهما العدد المطلوب زوجا او يكون الحدهما وردا والآخر زوحا وايهما كان فان مضروب ضلعيهما احدهما في الآخر مرتين وهو مثل العدد المفروض يكون زوح الزوج والفرد لان كل عدد زوج فان ضعفه يعده الاربعة وكل عدد يعده الاربعة فان العدد الذي يحدث من ضربه في عدد فرد يكون زوج الزوج والفرد فمتي فرض لما عدد لم يكن روج الزوج والفرد علمنا ان الذي طلب منا ممتنع

يه ســـ اسر بـ س ؛ اجراء . نقول وأبيا كانت القراءة فالتمير فير وأضح

الوجود لإنا قد بينًا انه لا يمكن ن يوجد عددان مربعان كل واحد منهما زوجالزوج ويكون محموعهما مربعا . عال كال احد ضمعي المربعين الزوجين روح لزوج كان الآخر روج الفرد او زوجالزوج والفرد وايهما كان فان مضروب احدهما في الآخر مرتين زوج الزوج والفرد . وان كال احد الصلمين فردا وكان الآخر احد اقسام الزوج كان مضروب احدهما في الآخر مرتين لا محالة روج الزوج [والفرد] .

ولذلك اذا مرص لنا عدد هو زوج الزوح والعرد وطلب منا عدد مربع ان زدنا عايه ذلك العدد كانالمجتمع مربعا وان نقصنا منه دلك العددكان الباقي مربعا فانا نأخذ بصفه ونأخذ الاعداد التي تعده فال كان منها عددان يكون مجموع مربعيهما مربعا فقد وجه نا مطلوبها وتسمي هذين العددين من بين كل عددين يعدانه ومحيطان به وحما ضلعاه] [قرينين . ١٢٠ و ن لم تحدهما كانك كان الذي طب عبر ممكن. واول هذه الاعداد اربعة وعشرون عان نصفه اقل عدد من اعداد روج الزوح والعرد فنأخذكل عدد يعد التي عشر وهو الثان وستة وثنثة واربعة فقط ومجموع مربعي ثلثة واربعة مربع وهو خمسة وعشرون فخمسة وعشرون فخمسة كان الباقي مربعاً ثم لا يوجد لاربعة وعشرين من الاضعاف ما له تصف يعده عددان قريفان حتى نتهي الى مايتين واربعين فان تصفها وهو ماية وعشرون يعده عددان قريفان ومجموع مربعيهما مايتان وتسجة وتمنون وجذره سبعة عشر الاواذا زيد عبيه او تقص مته ومجموع مربعيهما مايتان وتسجة وتمنون وجذره سبعة عشر الاواذا زيد عبيه او تقص مته مايتان واربعون كان المجتمع الباقي عربعين .

25 فلإن مايتين واربعين يعدها عددان مربعان وهما اربعة وستة [عشر] نقسمها على كل واحد منهما فيخرج ستون وخمسة عشر ، فلإن نسبة مايتين واربعين الى ستين كنسبة عدد مربع وهو نسبة الاربعة الى الواحد تكون هذه النسبة كنسبة مايتين وتسعة وثمنين الى مال مجدور ان زيد عليه او نقص منه ستون كان المحتمع والباقي مالين مجلورين فنقسم مايتين وتسعة وثمنين على اربعة فيخرج المال ويقع فيه كسر ولذلك لفظنا بالمال وايضا فنسبة مايتين واربعين الى خمسة عشر كنسة ستة عشر الى واحد فنقسمها على ستة عشر فيخرج المال الذي اذا زيد عليه ونقص منه خمسة عشر كان المجتمع والباقي مالين مجلورين.

۱۰ - في لمخطوط عبارة . او بعده اه ولا يحيطان به . كما قرأناها ۱۵ او يعدانه و لا يحيطان به ۱۱ ورأينا
 ۱۵ ومها ريادة لقاريء ما تفسد الممي و قرآها الدكتور سيدان على وجه حسن د ۱۱ او بعداه او يحيطان به ۱۱ .
 ۱ - ثلاثة وعشرون

وهذا طريق مطرد في وجود هذا النوع من المجذورات وهو انا اذا وجدنا مالا له جدر ال زدنا عليه عددا كان لما بلغ جذر وان نقصناه منه كان للباقي جدر ثم فرض لتا عدد نسبته الى ذلك العدد كنسبة عدد مربع الى عدد مربع وجدنا المال الذي اذا زيد عليه العدد المفروص كان لما بلغ جلس وان نقص منه كان لما يقي جدر . مثال ذلك ان يكون المال الموجود خمسة وعشرين والعدد الذي يراد عليه وينقص منه اربعة وعشرين والعدد الذي يراد عليه وينقص منه اربعة فالمال المعللوب ربع الذي فرض لنا سنة ونسبته الى اربعة فيخرج سنة وربع فهي المال المجذور الذي اذا وقص منه سنة كان المجتمع والباقي مجذورين . وكدلك اذا فرض لنا اربعة وخمسون ونسبتها الى اربعة وعشرين نسبة تسعة الى اربعة فيكون المال المطلوب ضعف وربع خمسة وعشرين فنسبة تسعة الى اربعة فيكون المال المطلوب ضعف وربع خمسة وغشرين فنه المال اربعة وخمسين كان لما بلغ جذر وان نقصناها وربعا وجذره سعة ونصف فان زدنا على المال اربعة وخمسين كان لما بلغ جذر وان نقصناها

وان كان العدد المفروض سبع ماية وعشرين كان لنصفه عددان قرينان احدهما تسعة والآخر اربعون لان مضروب احدهما في الاخر ثلثماية وستون ومجموع مربعيهما الف وستماية وأحد وثمنون ولان نسبة سبع ماية وعشرين الى ثمنين كنسبة تسعة الى واحد تقسم ألفا وستماية وأحد وثمنين على تسعة فيخرج المال الذي اذا زيد عليه ونقص منه ثمنون كان المحتمع والباقي مائين مجذورين . فأما الاربعون فان نسبتها الى هسبع ماية وعشرين و كنسبة واحد الى ثمنية [عشر] وليست كنسبة عدد مربع الى عدد مربع فليس يوجد من هذا الوجه مال يزاد عليه وينقص منه اربعون فيكون الزائد والناقص مائين مجذورين .

ومن وجه آخر فان نصف الاربعين اتما يعده اثنان وعشرة وخمسة واربعة فقط وليس فيها عددان قرينان يكون مجموع مربعيهما مربعا . وعلامة ضلعي المسدد المفروض هسل يمكن ان يكون مجموع مربعيهما مربعا أو لا يكون ذلك ان يقسم مربع الأقل على ضعف به الاكثر فان كان ما يخرج | « جذرا لما بقي ٣٠ ستهئل وجود ما نريد والا تعذر وامتنع

الى الف ومثماية واحد وتمين
 أو ما يقى له جلو

مثل ماية وعشرين فانه يحيط بها تمنية وحمسة عشر واذا قسمنا مربع ثمنية على ضعف الحمسة عشر خرج اثنان وبقي مربع الاثنين وهسو اربعة فيتفقد ذلك في طلب هذه الاعداد . ومثل ثشماية وشتين هانه يحيط بها اربعون وتسعة بهذه الصفة وذلك ان مربع تسعة اكثر من أربعين واذا قسمناه على ضعف الاربعين خوج واحد وبقي واحد ولان مربع ما خرج مثل ما بقي يمكن وجود ما نريد .

وفي وجود الفرع الذي قدمنا ذكره من الاعداد طرق أخر مرجعها كلها الى خمسة وعشرين . منها انّا متى وجدنا عددا مربعا اذا زدنا عليه عددا مربعا ضاعه مربع كان للمجتمع جنر ثم قسمنا جدر مجموعهما على جنر جنر العدد المربع خرج لنا جنر مال اذا زدنا ضعف جنر العدد المربع على المال ونقصناه منه كان المجتمع والماقي مجلووين . واول هذه الاعداد تسعة فاننا ان زدنا عليه ستة عشر ولها جنر والحارها جنر كان خمسة وعمير واذا قسمنا جنرها وهو خمسة على جنر جنر ستة عشر خرح اثنان ونصف وهي جنر المال الذي ان زيد عليه ضعف جنر تسعة كان لما بلع جنر وان نقص منه كان لما بقي جنر . ومن هذا النوع عدد اثني عشر فان مربعه الذي هو ماية واربعة واربعون اذا زدنا عليها احد وتمنين وهي عدد مربع ضلعه مربع اجتمع مايتان وخمسة وهي جنر مال مربع صلعه خمسة وهي جنر مال اذا ردنا عليه ونقصنا منه صعف اثني عشر كان المجتمع وانباقي عددين مجنورين .

ومنها أنّا نطب عددين مربعين ضلع احدهمها مربع ومجموعهما مربع ووجوده ان نجعل احد العددين كما بيننا فيما تقدم ربع عدد مجذور والآخر ذلك العددين كما بيننا فيما تقدم ربع عدد مجذور والآخر ذلك العدد للمجلوو ونضرب احدهما في الآخر | اربع مرات فيجتمع أحد العددين المربع الآخر ومجموعهما عدد مربع ثلثة ارباع الاكثر و ويكون مضروبه في مثله العدد المربع الآخر ومجموعهما عدد مربع واذا قسمنا جذره على جدر العدد الاول خرج جذر المال ان زدنا عليه ذلك العدد ونصفه كال لما بلغ جذر وال نقصناه منه كان لما بقي جدر . مثال ذلك ستة عشر واربعة فانا نضرب احدهما في الآخر اربع مرات فيكول ما بينهما فيكون احدهما في الآخر وهو اثنا عشر ومربعها ماية واربعة واربعون ومجموعهما اربعماية وجدرها مجموع ستة عشر خرجت خمسة وهي مجموع ستة عشر خرجت خمسة وهي

س - اي ثلثة ارباع العدد المجدور المختار

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جَلْس حمسة وعشرين وادا زدنا عليه بجموع ستة عشر وقصمتها وهي اربعة وعشرون وتقصناه منها كان ما بلغ وما بقى عددين مجذورين .

ويشبّس من دلك انه ادا فرض لنا عدد المثنيه جذر وجدنا المال الذي ان ردن عده ذلك العدد كان لما نلع حذر وان نقصناه منه كان لما يقي جذر ووجود جدر دلك المال المطبوب كما قدمنا ان ازيد على جذر ثاثي العدد المعروض ربعه * فيكون جذر المال المطبوب . وذلك ان ثني اربعة وعشرين وهو ستة عشر جذرا وهو اربعة وادا زيد عليه ربعه كان خمسة وهو جذر خمسة وعشرين واربعة وهو جذر خمسة وعشرين واربعة وعشرين كا بيتاه في اول الامر ومن تأملها وقف على علتها ان شاء الله .

32 واقرب هذه الوجوه كلها ان نأخذ اي عدد شتنا ونريد عليه ربعه وهو الاول ونزيد على ما اخدناه نصفه ونضر به فيما اخذناه فيكون الثاني ، فاذا زدنا الثاني على مربع الاول كاد لما بلغ جذر وان نقصتاه ممه كاد لما بقي جدر مثال ذلك ان نأخد تمنية ونزيد عميها ربعها فيكون عشرة وهو الاول ونزيد على ثمنية نصعها ونضرب ما بلغ في ثمنية فيكون بي ستة وتسعين وهي الثاني وادا ردنا هذا الثاني على مربع الاول كان لما بلغ جدر وان نقصناه حنه كان لما يقى جدر ،

وقد ينشد في صناعة الحسير عن مال له جسلر واذا ريد عليه عشرون كان لما بلغ جذر وان تقص منه عشرون كان لما بقي جذر وذلك يتعذر وجوده في عدد صحيح والوجه في معرفته ان نضرب عشرين في ستة وثلثين وهي عدد مربع فيجتمع سمع ماية وعشرون فنطلب عدداً ان زدنا عليه سبع ماية وعشرين اجتمع مربع وان تقصناها منه كان الباقي مربعا وهو الف وستماية وأحد وتمنون ١٦٨١ ووجودها يكون بالعمل الذي قلمناه فنقسمها على ستة وثلكين فيخرج المال المطلوب على ان هذا الطريق غير محصور وهو شبيه بالاستقراء اذكانت الاعداد المربعة بلا لهاية ولدلك ربما اتفق ما قطلبه وربما تعذر

34 والطريق الصناعي في ذلك ان المخذ نصف العشرين ونضربه في مثله فيكون ماية وتطلب هالا له جذر ولجذره جذر اذا زدناه على ماية كان لما يجتمع جذر . وانما يتغق لنا ذلك في

^{× -} أي ربع ثلق المدد غ - ذك.

العدد الذي قدمناه وهو الف وستماية واحد وثمنون اذا جعلناها اجزاء من ستة عشر ليكون احد وثمون خمسة وجزءا من ستة عشر وجذرها تسعة اجزاء من اربعة وهي جذر ستة عشر فهي اثنان وربع وجذرها واحد ونصف فنزيد خمسة وجزءا من ستة عشر على ماية ويكون جذر الجميع عشرة وربعا . وذلك ان جلمر الف وستماية واحد وثمنين احد واربعول وهي اجزاء من جذر ستة عشر واذا قسمناها عليه خرج عشرة وربع فنقسمها على واحد ونصف فيخرج ستة ونصف وثلث فهي جدر المال المظلوب والمال ستة وادبعون [وخمسة وعشرون] جزءا من ستة وثلثين فزيد عليه عشرين فيبلغ ستة وستين وخمسة وعشرين جزءا من ستة وثلثين وجدره ثمنية وسدس وننقص من المال عشرين فيبقى ستة وعشرون وخمسة و عشرون المال عشرين فيبقى ستة وعشرون اذ فرض لنا عدد وضرينا نصفه في مثله وحقظناه وطلبنا عددا له جذر ولحدره جدر اذا ردناه على ما حفطنا كان لما بلغ جدر فانا نجد المطلوب .

الاعداد التي ينقسم كل واحد منها بعددين مربعين كان احدهما مربعا أو مك كان كل واحد منها بعددين مربعين اذ مرب في عدد ينقسم بعددين مربعين كان احدهما مربعا أو مكن واحد منهما مربعاً فان ذلك مما يوضح المقدمة التي قلعها فيوفنطس للمسئلة التاسعة عشرة من المقالة الثالثة من كتابه في الحجر ويتنفع به في غيرها من المسائل . وأول خلك ان نقول كل عدد ينقسم بعددين مربعين فانمربعه ينقسم بعددين مربعين لان مضروب احدهما في الآخر اربع مرات يكون احد مربعي مربع ذلك العدد وضلعه مضروب جذر احدهما في جلو الآخر مرتين وضلع المربع الآخر فضل ما بين قسمي ذلك العدد .

3 وكذلك يكون حال كل عدد ينقسم بعددين مسطحين متشابهين . مثال ذلك عشرة فائها تنقسم باثنين وثمنية وهما مسطحان متشابهان فنقسم الماية نعددين مربعين احدهما الاكثر اربعة وستون وهي مضروب ثمنية في اثنين اربع مرات والاقل! ستة وثلثون وهي مربع فضل ما بينهما .

37 فان [كان] العدد الذي ينقسم بعددين مربعين مربعا مثل خمسة وعشرين فان موبعها وهو ستماية وخمسة وعشرون ينقسم بعددين مربعين مرتين لان مضروب تسعة في خمسة

> ٣ ــ رجزه ٧ ــ وجار ٨ ــ اذ ۴ ــ عش ١ ــ والاكثر

وعشرين مربع وكذلك مضروب ستة عشر في خمسة وعشرين فينقسم ستماية وخمسة وعشرون بمربعين احدهما اربعماية والآخر مايتان وخمسة وعشروں . وينقسم ايضا بمربعين آخرين على الطريق الذي قدمنا وذلك ان مضروب احد قسمي خمسة وعشرين في الآخر اربع مرات يكون مربعا وهو خمسماية وستة وسبعون ويكون المربع الآخر مربع فضل ما بينهما وهو تسعة واربعون .

فان ضربنا عددا ينقسم بعددين مربعين مرة واحدة في عدد ينقسم بعددين مردمين مرة واحدة انقسم العدد المركب منهما بعددين مربعين مرتين . مثاله ان خمسة مركبة من واحد واربعة وثلثة عشر مركبة من اربعة وتسعة ومضروب احدهما في الآخر خمسة وصنون فهي تنقسم بعددين مربعين مرتين لانه من السِّن ان خمسة في ثلثة عشر هو خمسة في اربعة وخمسة في تسعة وان خمسة في اربعة هو اربعة في اربعة وواحد في اربعة وخمسة ٢١١ في تسعة هو اربعة | في تسعة وواحد في تسعة الان الخمسة ينقسم باربعة وبواحد وثلثة عشر ينقسم باربعة وبتسعة ويكون اضلاع هده المرىعات اثنين واربعة وثلثة وستة . ولان نسبة اثنين الى اربعة كنسبة ثلثة الى ستة يكون مضروب اثنين في ستة مثل مضروب اربعة في ثلثة ومضروب ثلثة في اربعة مرتين مثل مضروب اثنين في ستة مرتين ، ولإن مضروب اثنين في ستة مرتين مع مربع فضل ما بينهما مثل محموع مربعي اثنين وستة ، ولكن مضروب اثنين في ستة مرتين مثل مضروب ثلثة في اربعة مرتين ، ومضروب ثلثة في اربعة مرتين مع٬ مجموع مربعي ثلثة واربعة مثل مربع محموع ثلثة واربعة ، يكون مربع فضل ما بين اثنين وستة مع مربع مجموع ثلثة واربعة مثل مجموع مرىعات اثنين وثبثة واربعة وستة وهي خمسة وستون . فلذلك ينقسم خمسة وستون بمربعين ضلع احدهما مجموع ثلثة واربعة وضلع الآحر فضل ما بين اثنين وستة ، مرة اولى ؛ وينقسم مرة اخرى بمربعين ضلع احدهما فضل ما بين ثلثة واربعة ، وضلع الآخر مجموع اثنين وستة فينقسم خمسة وستون مرة اولى بتسعة واربعين وستة عشر ومرة اخرى بواحد واربعة وستين . وكذلك ينقسم مضروب كل عددين يتقسم كل واحد منهما بعددين مربعين احدهما في الآخر .

فان ضُرب خمسة وسنوق وهي تنقسم بعددين مربعين مرتبن في أحد وستين وهي 39

۳ – کل

تنقسم بعددين مربعين مرة واحدة كان ذلك ثنثة الأف" وتسعماية وخمسة وستبن ٣٩٦٥ وهي تنقسم بعددين عددين مربعين اربع مرات لأنه اذا ضرب عدد ينقسم بعددين مربعين مرة في عدد ينقسم بعددين مربعين مرة تولُّنُد من ذلك عدد ينقسم بعددين مربعين مرتين . عادا كان احدهما ينقسم بعددين مربعين مرثين وجب ان يكون مضروب احدهما في الآخو ينقسم بعددين مربعين اربع مرات وذلك يظهر هكدا : وهو أن تصرب كل وأحد من ضلعي خمسة وعشرين وستة وثلثين في كل واحد من اضلاع مربعات⁴ خمسة وستين فيحدث من ذلك اربعة اعداد متناسبة على نسبة خمسة الى ستة واربعة اخرى على هذه النسبة ولضعها على الرسم فيكون خمسة

وعشرون في اثنين واربعين مثل اربعة وعشرين في خمسة وثلثين . فادا عملنا في ذلك على نحو ما عملنا فيما تقدم وهو ان نأخد فضل ما بين خمسة وثمنية واربعين وهو ثلثة واربعون ونجمع ستة مع اربعين فيكون ستة واربعين وهي قرين ثلكث واربعين وينقسم الاصل بمربعيهما مرة وتجمع خمسة مع تمنية وارىعين فيكون ثلثة وخمسين ونأخذ فصل اربعين على ستة فيكون اربعة وثائمين وهي قرين ثلثة وخمسين فينقسم الاصل ممريعي ثلثة وخمسين واربعة وثلَّثين مرة اخرى فيكون قد انقسم الاصل بمربعين مرتين . وكذلك يعمل بالاربعة الاعداد الباقية وهي عشرون واربعة وعشرون وخمسة وثلثون واثنان واربعون فينقسم مضروب خمسة وستين في احدوستين بعددين عددين مربعين اربع مرات

- وان ضربنا خمسة وستين في خمسة وعشرين وهي عدد مربع ينقسم بقسمين مربعين فاله يجتمع منه الف وستماية وخمسة وعشرون وينقسم نقسمين قسمين مربعين ست مرات اربعا منها على نحو ما بيناه ومرة خامسة من مضروب كل واحد من تسعة واربعين وستة عشر في خمسة وعشرين ومرة سادسة من مضروب كل واحد من اربعة وستين وواحد ني خمسة وعشرين .
- قان ضربنا خمسة وستين في مثلها اجتمع اربعة الف° ومايتان وخمسة وعشرون وهي 41 ٣ - كتبت الاف بشكل الف اي عقدير تف الحسم وهي كتابة حائزة في الاف ، دراهم ، أذ لم يقع

التباس في المعنى .. و -- الريمات

تنقسم بعددين عددين مر بعين اربع مرات وذلك يظهر على ما بياه . وطريق معرفة ذلك ان نعمل بخمسة وستين كما عملنا بالجمسة و ذلك ان نقسمها باربعة وستين وبواحد و نضرب ضعف ضلع اربعة وستين في ضلع الواحد فيكود ستة عشر وهي ضلع القسم الاقل من مربع خمسة وستين و تأخل فضل ما بين اربعة وستين و واحد وهو ثلث وستون وهي قرين ستة عشر . وكذلك نعمل بستة عشر و تسعة واربعين فيخرج ضلعا المربعين في المرة الثانية ثلكة وثلثين وستة وخمسين فقد قسمنا مربع خمسة وستين بعددين مربعين مرتبن و نقسمه ايضا مرتين كما قسمنا مضروب خمسة في ثلثة عشر وذلك ال نضرب كل واحد من ضلع واحد ومن ضلع اربعة وستين في كل واحد من صلع ستة عشر و فلك به نغضرب واحدا في اربعة ويكون اربعة ، وتمنية في اربعة فيكون اثنين و ثلثين ، و نضرب واحدا في سبعة فيكون إ سبعة و نضرب تمنية في سبعة فيكون ستة وخمسين . فمربعات هذه وستة مجموعة مثل خمسة في ثلثة عشر . ولان نسبة اربعة الى سعة كنسة اثنين و ثلثين و ثلثين الى ستة وخمسين عمل اثنين منها مربع خمسة وستين فيكون ستين و ذلك اثنين منها مربع خمسة وستين ، وذلك ان نجمع اربعة مع ستة وخمسين فيكون ستين و ناخذ فضل اثنين و ثلثين على سبعة و هو خمسة و عشرون قيكون ستين و ناخذ فضل اثنين و ثلثين على سبعة و هو خمسة و عشرون قيكون قوين ستين و ناخذ فضل ستة و خمسين على اربعة على سبعة و هو خمسة و عشرون قيكون قوين ستين و ناخذ فضل ستة و خمسين على اربعة على سبعة و هو خمسة و عشرون قيكون قوين ستين و ناخذ فضل ستة و خمسين على اربعة على سبعة و هو خمسة و عشرون قيكون قوين ستين و ناخذ فضل ستة و خمسين على اربعة على سبعة و هو خمسة و عشرون قيكون قوين ستين و ناخذ فضل ستة و خمسين على اربعة عمر اربعة عمر اربعة عمر عمسة و عشرون قيكون قوين ستين و ناخذ فضل ستة و خمسين على اربعة عمر اربعة اربعة عمر اربعة عمر اربعة عمر اربعة عمر اربعة عمر اربعة عمر ارب

| 4414 | 74 | 17 | 107 |
|------|----|----|------|
| 77 | 3+ | 40 | 170 |
| 4141 | 67 | 44 | 1114 |
| YV+1 | ₽Υ | 44 | 1011 |

فيكون اثنين وخمسين وتجمع اثنين وثلثين وصبعة هيكون تسعة وثبتين وهي قوين اثنسين وخمسين . ونضع ذلك على هذا الرسم. ومربع الخمسة والستين معما ينقسم به من المربعات هوالذي قدّمه فيوفنطس في المسئلة التي ذكوناها ٢ وهي وجود اربعة اعداد أذا زيد كل واحد منها على مربع مجموعها كان لما بلغ جذر وان نقص منه كل واحد منها كان لما بلغ جذر وان

وقد تتبيح هذه المقدمة طريقاً يوجد به اربعة اعداد مختلفة يكونجموعها مربعا ومجموع كل اثنين منها مربعا . فقد ينبغي للانسان ان يكون غرضه في المقدمات التي يعطاها ابتداع ما ينتج منها دون الاشتغال بزيادتها وتكثيرها فكم من لنائج ومطاوبات في المقدمات التي

و د انظر المقطع ۳۰ ...

ہ ۔ سے . س ۽ تتنج

عادل اتبوبا

اعطاناها فيقوها حوس في صناعة العدد ، وفي الأصول التي ضمنها اقليدس مقالاته العددية الخطوط ثم ختمها بوجود العدد الثالث ونقله اليها من الارتماطيقي وبرهن عليها من جهة الخطوط ثم ختمها بوجود العدد التام الذي هو اجل الاغراض ، وجمه من الاعداد الارواج لان اصحاب الارتماطيقي قسموا العدد الزوج قسمة اخرى الى ثلثة انواع زائد وناقص وتام ، وكان ينبغي لهم الا يخصوه بهذه الاقسام وقد وجد في العدد الفرد زائد وناقص . ولللك وقع للسائلين سؤال الاعداد الافراد ام لا . وقد يقع سؤال اخر إجليل وهو هل يجوز ان يوجد في بعض العقود دون بعض . فان المفسرين لكتاب الارتماطيقي قالوا : العدد التام موجود في كل عقد من العقود ولكن الناظرين في هذا الكتاب كثيراً والمستقصين التام موجود في كل عقد من العقود ولكن الناظرين في هذا الكتاب كثيراً والمستقصين جزئياتها ما امكن ، ولا يقتصر على كلياتها فقط ، فان اواثل كل صناعة هي كليات و كمالها جزئياتها ما امكن ، ولا يقتصر على كلياتها فقط ، فان اواثل كل صناعة هي كليات و كمالها جزئياتها ما امكن ، ولا يقتصر على كلياتها فقط ، فان اواثل كل صناعة هي كليات و كمالها جزئياتها ما امكن ، ولا يقتصر على كلياتها فقط ، فان اواثل كل صناعة هي كليات و كمالها جزئياتها ما امكن ، ولا يقتصر على كلياتها فقط ، فان اواثل كل صناعة هي كليات و كمالها جزئياتها ما امكن ، ولا يقتصر على كلياتها فقط ، فان اواثل كل صناعة هي كليات و كمالها جزئياتها ما امكن ، ولا يقتصر على كليات و كمالها حدالها المكن ، ولا يقتصر على كليات و كمالها حدالها الكناب و كليات و كليات و كمالها حدالها الكناب و كليات و كليات

تم ولله الحمد والمئة .

عورض بالاصل

۹ ساس : کثر ۷ سالمانیها س ؛ لمانیها

On pourra prendre par exemple, $0.240 < k \le 0.273$

$$1.217 \le k \le 1.393$$

par exemple,
$$k = 0.15$$
, $b = 1.25$.

Note: On trouve dans Diophante des exemples d'inégalités du second degré V, 30, 16. Voir la discussion qu'en fait Heath, Diophantus, op. cit., pp. 60-65.

D'autre part la décomposition du trinôme du second degré en un carré de binôme du premier degré est explicitement attribuée à Diophanto par el-Karaji dans el-Fakhri (Caire Ms 8663, f. 22a, 24a) encore qu'on n'en voit pas d'exemple dans l'Arithmétique de Diophante, éd. Tannery.

Le considération que nous avons faite que la racine de $(3k^2 - \frac{7}{3})^2$ est, suivant le cas $3k^2 - \frac{7}{3}$ ou $\frac{7}{3} - 3k^2$ cat également faite par al-Karaji par exemple dans "Ral hisés aljabr w'al-muqdhala, MS Bodl. Oxford. I. 936, 3, f. 4a, 1. 1, et al-Fakhri, Caire MS 8663, f. 24a, l. 1.

éème siècle H. comme le 3ème d'ailleurs furent un effet une époque de racherche active où l'esprit critique – que l'on voit poindre ici – avait tous ses droits. On peuse à ces réunions de penseurs et philosophes des lêmes et deme siècles, où chose inquie, des hommes de races, de confassions, d'appartenances différentes mettasent leurs livres révéiés de côté, pour discuter su nom de la raisen. Abû Jafar se fait ici l'ècho des critiques soulevées à propos de la théorie des nombres et des recherches entreprises. Le fait qu'il nous propose de trauver quatre nombres dont la samme est un carré et qui ajoutés doux à deux donnent un carré signific sinon qu'il en avait le solution du mous qu'il était sur la voie de la recherche. Ce joh problème est digne de figurer dans des commentaires sur Diophante cumme en ont écrit al-Bûzjanî ou al-Samaw'al. Le solution que nous en donnous à la manière de Diophante montre que le problème viest pas au-dessu des possibilités d'Abû Jafar. Il s'agit de treuver des nombres possédant les propriétés étaouées. On peut voir une solution par Fermat du système ax + b = □, ex + d = □, ex + f = □, dans T. L. Heath, Diophantes, p. 321.

Problème - Trauver quatre nombres dont la somme est un carré et qui, additionnés deux à deux donnent des carrés.

Solution: Soient a,b,c,d, cea quatre numbres. Nous faisons $a=x^2,b=-2$ $mx+m^2,c=2nx+n^2,d=2px+p^2$, de sorte que a+b,a+r,a+d sont des carrés. La somme $a+b+c+d=x^2+2$ $(-m+n+p)x+m^2+n^2+p^2$ sera identique à un carré, si nous prenons $(m-n+p)^2-(m^2+n^2+p^2)$ ou $-2mn-2mp+2np=0, m=\frac{np}{n+p}$, égalité vérifiée par une infinité de solutions (m,n,p) entières ou rationnelles. Heste à égaler b+c, b+d, c+d, à des carrés

$$2(n-m)x+n^2+m^2$$
, $2(p-m)x+p^2+m^2$, $2(p+n)x+p^2+n^2$

Nous réduisons la difficulté en prenant deux de ces trois expressuos égules. Il suffit de prendre n=p. Faisons par exemple, n=p=1, d'où $m=\frac{1}{2}$,

$$b+c=x+\frac{5}{4}$$
, $b+d=x+\frac{11}{4}$, $c+d=4x+2$.

Il s'agit de rendre 4x + 5 et 4x + 2 carrés.

Posons
$$\begin{cases} 4x + 5 = u^2 \\ 4x + 2 = v^2 \end{cases}$$

 $\mathbf{D}^{1}oh \ \mathbf{x} = \frac{u^{2}-5}{4} \quad \text{où} \quad u \quad \text{est rationnel, et} \quad u^{2}-v^{2}=3, \quad u \quad \text{et} \quad v \quad \text{rationnels.}$

$$\label{eq:Anderson} {\rm Aind}\, u = \frac{3k^2+1}{2k} \;, \quad v = \frac{3k^2-1}{2k} \;, \quad v = \frac{9k^4-14k^2+1}{16k^2} \;\;.$$

Condition
$$b = -a + \frac{1}{4} > 0$$
, good $0 < a < \frac{1}{4}$

6. Voir al-Dabbi, Bughyat al-multamis fi tarikh rijāt ahl al-andalus (Caire, 1967), p. 155.

entre les textes grecs de Diophante tels qu'ils ont été connus des Arabes et ceux qui sont conservés de nes jours. En même temps elle confirme l'affirmation émise par Roshd: Rashed que le livre III du texte est conforme au hyse III de la traduction arabe.²

Texte

Cette proposition pourrait fournir un moyen de trouver quatre nombres dont la somme est un carré et qui additionnés deux à deux donnent des carrés. Car il convient de tirer des propositions préliminaires, leurs conséquences immédiates saus chercher à augmenter le nombre de ces propositions.3 Que de résultats et de questions posées dans les propositions que Nicomague nous a données dans la théorie des nombres (sinàcar al-cadad) et dans les Eléments qu'Euchde a transférés de la théorie des nombres à ses trois livres arithmétiques, éléments qu'il a démontrés au moyen de segments et qu'il a couronnés, par la recherche du nombre parfait qui est le but suprême. Euclide a placé les nombres parfaits dans la catégorie des nombres pairs car les arithméticiens ont réparti les nombres pairs en trois classes: surabondants, déficients et parfaits. Il n'auraient pas dû caractériser les nombres pairs par cette division puisqu'on a trouvé des nombres impairs surabondants et déficients. On s'est demandé de même s'il existe un nombre parfait impair. Une autre question importante que l'on peut se poser c'est si le nombre parfait peut se trouver dans certains caquada et pas dans d'autres. Car les commantateurs du livre de l'Arithmètiques ont dit qu'il y a un nombre parfait dans chacun des "ugad. (Mais tant s'en faut) car les lecteurs de ce livre sont nombreux et ceux qui approfondissent ses notions sont très rares. Or les personnes qui acquièrent un renom dans la science (sing at) ne doivent pas se contenter d'en connaître les généralités mais être maîtres aussi de ses plus petits détails. Le début de chaque science est généralités la perfection en est dans les minuties.

Observation. L'intérêt du langage précédent est évident il évoque un climat. L'attitude d'Abū Jeffer qui n'ast pas celle d'un isolé est que le rôle de savont ne doit pas se limiter à celui de transmettre. Bien des questions laissées sans réponse attendeut de lui leurs solutions. Le

Voir l'important article de Rushdi Rashed, "Les traveux perdus de Diophante," Revus d'Histoire des Sciences, 27 (1974), 99-122, p. 105; 28 (1975), 3-30.

It ust possible que le suppression, par un copiste, de la négation id° avant le mot convient sit modifié le sens de la phrass.

^{4. &}quot;aqd, pl. "uqud signifa ici la diasse des unités, celle des dizzines, des containes, des milliers, des dizzines de mille. . Dans l'Arithmétique de Nicomaque il est dit que dans chaque classe jusqu'à celle des mille, il y a un nombre parfait et un seul 6, 28, 496, 8128 (Kitab al-madkhal ild "ilm al-"adad, trad. Thähit b. Qurra, W. Kutsch, S. J. (Beyrouth, 1958) pp. 38-29).

^{5.} Il s'agit s'videmment de l'Arithmétique de Nicomaque qui connut chez les Crees et les Arabes un crédit considérable. Jambhque (283-330) énonça qu'il y avait dans chaque classe de nombres, unités, dinantes, etc. . . . , jusqu'à l'infim un nombre parfait et un seul, affirmation erronée (Voir Dickeus-op cir., vol I, p. 4). On doit à Thàbit b. Quira un mémoire sur les nombres parfaits (F. Woepcke, Jour. As., 20 (1852), 420-9). Le Sènse nombre parfait 35550336 se trouve meotionné dans un ms. latin daté en par tie de 1456, en partie de 1461 (Dickeon, pp. ch., p. 6).

Et nous avons

$$xy' = |ac - bd|^2 + (bc + ad)^2$$

$$= (ac + bd)^2 + |bc - ad|^2$$

$$= |a'c - b'd|^2 + (b'c + a'd)^2$$

$$= (a'c + b'd)^2 + |b'c - a'd|^2$$

Teste Si un nombre x se décompose en une somme de 2 carrés de deux manières différentes et si un carré y² se décompose d'une seule manière, leur produit se décompose de six manières différentes en une somme de 2 carrés.

$$x = a^2 + b^2 = a^{2} + b^2$$
 $y^2 = c^2 + d^2$

Aux quatre décompositions déjà vues s'ajoutent:

$$xy^2 = a^2 (c^2 + d^2) + b^2 (c^2 + d^2)$$

$$xy^2 = a^{12} (c^2 + d^2) + b^{12} (c^2 + d^2)$$

Ex. : 65 25 etc. . . .

Teste (Si un nombre est une somme de deux carrés de deux manières, 41 son carré l'est de quatre manières).

$$x = a^{2} + b^{2} = c^{3} + d^{2}$$
D'où
$$x^{2} = (2ab)^{2} + |a^{2} - b^{2}|^{2},$$
et
$$x^{2} = (2cd)^{2} + c^{2} - d^{2}|^{2}.$$
On a aussi
$$x^{2} = (ad + bc)^{2} + |ac - bd|^{2},$$

$$x^{2} = (ac + bd)^{2} + |ad - bc|^{2}.$$

La question est exposée dans le texte sur $65 = 8^2 + 1^2 = 4^2 + 7^2$, et les résultats groupés dans un tableau.

$$x^2 = 16^2 + 63^2 = 60^2 + 25^2$$

 $x^2 = 56^2 + 33^2 = 39^2 + 52^2$

L'auteur ajoute: La décomposition de 65² en somme de deux carrés est ce que Diophante a placé en tête de la question (qaddama) que nous avons rappelée: Trouver

| 256 | 16 | 63 | 3969 |
|------|----|----|------|
| 625 | 25 | 60 | 3600 |
| 1089 | 33 | 56 | 3136 |
| 1521 | 39 | 52 | 2704 |

quatre nombres qui ajoutés successivement au carré de leur somme donnent des carrés et qui, retranchée du carré de leur somme, donnent des carrés.

Observation: Nous avons rendu le mot gaddama per placer en tête. Ce mot signifie également donner ou lemme et l'expression utilisée par l'auteur dans le paragraphe 35 rend clairement nette dernière signification : al-maquddima allati gaddamaha Dyhofanjus til'-mas'alat al-téus' ata "athara. Dans le texte établi par Tannery la décomposition de 652 en aomine de deux carrés de quatre manières est rapportés dans le texte de la prop. 19 du livre III, mais en lemme. Si notre interprétation du mot qaddama est exacte, cette sirconstance montrerait les différences

Quelques propriétés des nombres qui se décomposent en sommes de Texte carrés, utiles dans certaines questions et éclairant le lemme dont Diophants 25 a fait précéder la proposition III, 19 de son Algèbre.

Si x est une somme de deux carrés son osrré est aussi une somme de deux carrés.

$$x = a^2 + b^2$$
, $x^2 = (2ab)^2 + (a^2 - b^2)^2$.

Texte Si x est une somme de deux nombres plans semblables, son carré

36 est une somme de deux carrés.

$$x = ab + cd$$
 avec $a:b = c:d$. Done $(ab)(cd)$ est un carré (Euclide, IX, I). $x^2 = 4(ab)(cd) + (ab - cd)^2$.

Teste Si un carré se décompose en une somme de 2 carrés, son carré se décompose en une somme de 2 deux carrés de deux manières différentes.

$$x^{2} = a^{2} + b^{2} \text{ donne } x^{4} = (2ab)^{2} + (a^{2} - b^{2})^{2},$$

$$x^{4} = a^{2} (a^{2} + b^{2}) + b^{2} (a^{2} + b^{2}).$$
Ex.: $25 = 3^{2} + 4^{2}$, $625 = 4 \cdot 9 \cdot 16 + (4^{2} - 3^{2})^{3}$,
$$625 = 9 \cdot 25 + 16 \cdot 25.$$

Teste Si deux nombres sont des sommes de 2 carrés leur produit est une somme de 2 carrés de deux manières différentes.

Si
$$x = a^2 + b^2$$
 or $y = c^2 + d^2$,
on a $xy = a^2c^2 + a^2d^2 + b^2c^2 + b^2d^2$.

Mais ac:ad = hc:bd done ac.bd - ad.bc (Euclide VII, 19). Par suite on peut écrire:

$$xy = |ac - bd|^2 + (ad + bc)^2 \quad \text{et}$$

$$xy = (ac + bd)^2 + |ad - bc|^2.$$

$$E\pi_*: 5.13 = (1^2 + 2^2) \cdot (2^2 + 3^2).$$

$$5.13 = 4^2 + 7^2.$$

$$5.13 = 8^2 + 1^2.$$

Teste Si deux nombres se décomposent en une somme de deux carrés, 39 l'un de deux manières différentes, l'autre d'une seule manière, leur produit se décompose de quatre manières en somme de 2 carrés.

On a
$$x = a^2 + b^2 = a'^2 + b'^2$$
, $y = c^2 + d^2$, $xy = a^2c^2 + b^2c^2 + a^2d^2 + b^2d^2$ $xy = a'^2c^2 + b'^2c^2 + a'^2d^2 + b'^2d^2$

Les produits de c et d par les termes a, b; a', b' sont huit nombres dont le rapport (deux à deux) est celui de c à d.

| | 20 00 60 | n/a | -ta 1/2 -/3 1/3 | (ac: ad = bc: bd donne | | | | |
|-----|----------|-----|-----------------------|------------------------|-----|-----|-----|--|
| GC. | 06 | ши | DEA | 0.6 | 0.6 | a a | 0.0 | (ac: ad = bc: bd donno $ac\cdot bd = ad\cdot bc).$ |

x tel que
$$x^3 \pm a = \Box$$
 prendre $x = b + \frac{b}{4}$.
[En effet, $\left(\frac{5b}{4}\right)^2 \pm \frac{3b^2}{2} = \frac{25b^2 \pm 24b^2}{16}$].
Ex. : $a = 24$, $\frac{2}{3}$ $a = 16 = 4^2$, $x = 4 + \frac{1}{4} \cdot 4 = 5$.

Texte S2 La méthode la plus simple pour trouver un (x,a) tel que $x^2 \pm a = \square$ est de choisir un nombre arbitraire 1 et de poser $x = \frac{5i}{4}$, $a = \frac{3i^2}{2}$.

Alore
$$x^2 \pm a = \square$$
.

Ex.:
$$t = 8$$
, $x = 10$, $a = t \cdot \frac{3t}{2} - 96$. On a bien $102 \pm 96 = \Box$.

Teste On recherche en algèbre (sinā at al-jabr) x tel que $x^2 \pm 20 = \square$, 33 équation impossible pour x entier. (Pour x fractionnaire) on considère le produit $20 \cdot 36 = 720$. Il est facile de trouver un carré d'entier u tel que $u^2 \pm 720 = \square$, u = 41, $41^2 \pm 720$ \square . Par division par 36, $\left(\frac{41}{6}\right)^2 \pm 20 = \square$.

Teste Cependant cette méthode est une méthode d'essaîs qui peut donner 34 ou ne pas donner de résultat.

La méthode régulière ($\sin a^{c}i$ artisanal) pour calculer x tel que $x^{2} + a = \Box$ où a est donné, est de trouver un u tel que $(u^{2})^{3} + {a \choose 2}^{2} = \Box$.

Soit
$$(u^3)^2 + \left(\frac{a}{2}\right)^2 = b^2$$
, d'où $u^2 + \left(\frac{a}{2u}\right)^2 = \left(\frac{b}{u}\right)^2$.
On $u = x = \frac{b}{u}$. En effet, $x^2 \pm a = u^2 + \left(\frac{a}{2u}\right)^2 \pm a = \left(u \pm \frac{a}{2u}\right)^2$.

(Les explications sont données sur $x^2 \pm 20 = \Box$).

On a
$$\frac{1681}{16} = 100 + \frac{81}{16}$$
 ou $\left(\left(\frac{3}{2}\right)^2\right)^2 + \left(\frac{20}{2}\right)^2 = \left(\frac{41}{4}\right)^2$.

Alors
$$x = \frac{41}{4} : \frac{3}{2} = \frac{41}{6} (\text{on } 6 + \frac{1}{6}) \text{ etc.},$$

Note préparatoire

Diophante a montré que :

- Tout carré, ou toute somme de deux carrés, peuvent se décomposer en somme de deux carrés de rationnels, d'une infinité de manières (II, 8 et 9).
- Si deux entiers cont chacun la somme de deux carrés leur produit est la somme de deux carrés de deux manières (l'emme III, 19).

Se plaçant mi dane l'optique de la théorie des nombres Ábû Jaffar envisage dans l'ensemble des entiers naturels une série de jolies propositions (texte 35-41) dont certaines lui appartiennent probablement. Texte De $25 \pm 24 = \Box$ nous tirons $(\frac{5}{2})^2 \pm 6 = \Box$. Comme $54:24 = \frac{9}{4}$ nous aurons $25 \cdot \frac{9}{4} \pm 54 = \Box$ ou $(\frac{15}{2})^2 \pm 54 = \Box$.

Prenons a = 720, 720: 2 = 360 = 40.9, avec $40^a + 9^a = 41^a$. Done avec $41^a \pm 720 = \Box$, d'où par division par 9, $\left(\frac{41}{3}\right)^2 \pm 80 = \Box$. D'autre

Texte part 40:720 = 1:18 qui n'est pas un rapport de carrés, donc on ne peut, par cette voie, trouver x rationnel tel que $x^2 \pm 40 = \square$.

Autrement. Si a=40 if n'existe pas s et t (entiers) tels que st=20Teste et $s^2+t^3=\Box$. Pour savoir si s^4+t^3 est un carré quand on a st=a28 (s<t) on divise s^3 par 2t. Si le reste de la division égale le carré du quetient alors $s^4+t^4=\Box$. (En effet, $s^4=2tq+q^4$ d'où $s^4+t^6=(t+q)^4$) Exemple: $a=120=8\cdot15$, $360=9\cdot40$ etc. . . .

Si on n'a pas $s^a = 2tq + q^a$ alors la recherche de x^a tel que $x^a \pm a = \Box$ devient difficile ou impossible.

Il existe d'autres méthodes qui se ramènent toutes à la règle du nombre 25. $[(3^{9} + (2^{1})^{2} = 5^{5} \text{ soit la forme } x^{9} + (y^{8})^{2} = z^{3})]$. Par exemple, si nous trouvons (x, y, z) tel que $x^{2} + (y^{3})^{2} = z^{3}$ nous prenons le rationnel $\frac{x}{y}$. Alors $\left(\frac{x}{y}\right)^{2} \pm 2x = \frac{z^{3} \pm 2xy^{3}}{y^{2}} = \frac{x^{9} + (y^{3})^{3} \pm 2xy^{3}}{y^{3}} = \text{earré}$ de rationnel.

Ex.:
$$3^9 + (2^8)^9 = 5^9$$
 donne $\left(\frac{5}{2}\right)^2 \pm 2 \cdot 3 = \square$.

Ex.:
$$12^{8} + (3^{8})^{6} = 15^{8}$$
 donne $\left(\frac{15}{3}\right)^{2} \pm 2 \cdot 12 = \square$.

Pour trouver (x, y, z) tel que $x^2 + (y^2)^2 = z^2$, nous pouvons considé-Texte rer t^2 et $\frac{1}{4}t^2$ et poser $x^2 = (t^2 - \frac{1}{4}t^2)^2$, $(y^2)^2 = 4 \cdot t^2 \cdot \frac{1}{4}t^4$,

$$t^{a} = (t^{a} + \frac{1}{4}t^{a})^{a}$$
. Nous aurons $(\frac{z}{t})^{2} \pm \frac{3}{2}t^{a} = \Box$, $(\frac{5t}{4})^{2} \pm \frac{3}{2}t^{a} = \Box$, $\frac{25t^{a} \pm 24t^{a}}{t^{a}} = \Box$.

Ex.:
$$t^4 = 16$$
, $x^3 = 12^4$, $(y^3)^4 = 256$, $x^4 = 400 = 20^4$, $\frac{x}{t} = \frac{20}{4} = 5$, $\frac{3t^5}{2} = 24$, $5^2 \pm 24 = \Box$.

Texts Si l'on a un entier a tel que $\frac{2}{3}$ a $=b^{b}$, carré d'entier, pour trouver

Le problème est impossible si a ne décompose pas en facteurs s et s conjugués.

Observation: Comme il a été dit, ca problème tient une place importante dans les recherches du 6ème nècle H. Il apparaît en particulier dans les mémoires M2 et anonyme évaqués dans l'introduction. Dans les toutes pramères anutées du 5ème nècle, al-Karaji par une méthode qui n'exclut pas le tâtonaement résout $x^2 \pm 5 = \Box$. Le même question ou des questions analogues se retrouvent dans les nècles postérieurs. Ibn al-Hâ'im reproduit, en les séparant, les équations $x^2 + 5 = \Box$. $x^2 - 5 \approx \Box$. (Al-Ma'uma, écrit en 791 h. Ms Berlin 5984, pp. 290, 291) questions que l'on trouve antérieurement dans al-Fakhri d'al-Karaji (Ms Le Care V. 212, f. 36°, l. 13, f. 59°, l. 2). Ibu al-Khawām dans al-Fakhri d'al-bahd' 1970 (675 H.) cite $x^2 \pm 10 \approx \Box$ parmi les 33 questions impossibles, ''non. dit-il, que je prétende établir lew impossibilite, mais je déclare mon incapacité à les résoudre'' (Ms. British Mus., Or 5615, f. 44°). En Europe, la question $x^2 \pm 5 = \Box$ est étudiée vers 1220 C. par Leonard de Prie, dans Flos, lequel aboutit par un chemin différent à la même réponse qu'al-Karaji $x^2 = \frac{1681}{144} = 11 \cdot \frac{2}{3} \cdot \frac{1}{144}$

$$x = 3 + \frac{1}{4} + \frac{1}{6} = \frac{41}{12}$$
.

L'intérêt de $x^2 \pm a = \Box$, comme l'a déjà relevé Woepcke, est qu'il est lié à des questions difficiles et fondamentales de l'analyse indéterminée qui ont été truitées par Fermat. Euler, Lagrange et Lagendre (Asii dell' Accodemia Pont. N. Lincar, "Recherches sur plusieurs ouvrages de Leonard de Piso", p. 252). On trouvera une ample documentation et des résultats intéressants sur la question dans L. E. Dickson, History of the Theory of Numbers (New York, 1952), val 2, pp. 459-472. Relevors quelques énoncés : Conocchi a démontré en 1882 (ce qu'il avant énoncé en 1874) que $x^2 \pm a$ ne peuvent être tous deux des carrés de rationnels si a est promier de la forme 8k+3 ou le produit de deux nombres premiers de cette forme. si a est le double d'un nombre premier de la forme 8k+5 ou le double du produit de deux nombres premiers de cette forme. (Dickson, op. cit., pp. 470, 467). Collins prouva en 1858 que pour a < 20, 5,6,7, 13, 14, 15 sont les seules valeurs de a pour lesquelles le système a des solutions (Dickson, ep. cit., p. 465). Destourcelles prouva en 1881 l'impossibilité en numbres entiers du système $x^2 + y^2 = x^2$, $y^2 - y^2 = u^2$ (Dickson, ep. cit., p. 467).

Dans les mémoires M2 et anonyme déjà cités le problème était résolu au moyen de tables numériques et donnait lieu d'ailleurs à des remarques intéressantes. Utilisant les formules $z=s^2+t^2, z=s^2-t^2, \ y=2st,$ pour former les triangles rectangles numériques $z^2=z^2+y^2$ on a $z^2\pm 2xy=x^2+y^2\pm 2xy=(x\pm y)^2$. D'où les diffarentes valeurs possibles pour z et pour z telhs que $z^2\pm s= \square$ (1). Ici l'auteur s'engage dans une autre voie et il recherche une condition nécessaire que doit remplir a pour que (1) soit possible, asvoir a doit être de la forme 4m(2n+1) d'une part, d'autre part sa moitié doit être le produit de doux factures dont la somme des carrés est un carré. Ce qui constitue un critère commode pour les nombres relativement petits.

Tents Si a cut divisible par un curré m^2 , alors $x^2 \pm a = \square$ donne $\left(\frac{x}{m}\right)^2 \pm \frac{a}{m^2} = \square$, égalité de la forme $x^2 \pm a = \square$ où x est rationnel. Ex.: $289 \pm 240 = \square$ donne $\left(\frac{17}{2}\right)^2 \pm 60 = \square$. De même $\frac{289}{16} \pm 15 = \square$ ou $\left(\frac{17}{4}\right)^2 \pm 15 = \square$.

Texte Proposition: Si un nombre pair est la somme de deux carrés a = b¹+d¹,

21 sa moitié est une somme de deux carrés, et la moitié de sa moitié aussi,
et ainsi de suite tant que la moitié obtenue est un nombre pair.

Car
$$\frac{a}{2} = \frac{b^3 + c^2}{2} = \left(\frac{b+c}{2}\right)^2 + \left(\frac{b-c}{2}\right)^2$$
.

Observation: L'auteur se rend bien compte que l'égalité est volable même pour des nombres fractionnaires. Les élégautes propositions 20,21 vont trouver seur application immédiate dans le problème susvent.

Problème: a est un entier donné. Trouver x tel que $x^2 \pm a = \square$. (1)

Supposons, par analyse, l'existence de x, y, z tels que x² + a - z² (2),

Texte x²—a = y² (3). Evidemment y<x<z. Je dis que x² est une somme de

deux carrés, car par addition 2x² - y² + z², (4) donc x² est une somme de

deux carrés (proposition précédente) (z et y ont même parité d'après

(2) et (3)) et
$$x^3 = \left| \frac{x - y}{2} \right|^2 + \left(\frac{x + y}{2} \right)^2$$
. (5)

Par soustraction de (2) et (3) on a :

$$2a = z^2 - y^2$$
 $a = 2 \cdot \frac{z - y}{2} \cdot \frac{z + y}{2}$ (6)

Il en résulte que a doit être pair. Sa moitié $\frac{a}{2}$ est le produit de deux

facteurs $\frac{z-y}{2}$, $\frac{z+y}{2}$ qui ne peuvent être tous deux impairs ni tous deux de la forme 2^n sans quoi (5) ne serait pas satisfait (1 emmes 1 et 2).

Teste $\frac{x-y}{2}$ et $\frac{z+y}{2}$ sont ou pairs tous deux ou l'un pair et l'autre împair.

Dans tous les cas a est de la forme a = 4m(2n + 1). Si cette condition n'est pas réalisée le problème est impossible.

Texts Problème (suite): On danne a de la forme 4m(2n+1). Calculer x tel que 24 $x^2 \pm a = \square$.

Nous prenons les diviseurs s et t de $\frac{a}{2}$ tels que $\frac{a}{2} = st$, $s^{t} + t^{s} = \square$ s'il y en a.

Les nombres s et t sont alors dit conjugués (qurinan) $x^4 = s^2 + t^4$ car $s^4 + t^4 \pm 2st = \square$.

Le plus petit nombre a qui réponde à la question est a=24, $\frac{a}{2}=4\cdot3$, $3^2+4^2=\square$. Puis parmi les multiples de 24 vient 240, $120=8\cdot15$, $8^2+15^3=17^2$, $x^3=17^3$, $17^3+240=\square$.

(Cependant le mauvais choix de l'exemple numérique rend la règle difficile à saisir dans le texte).

Autre triplet (x, y, t). (C'est la première méthode particularisée)

Teate 16

อน

$$x^{3} = \left| \frac{a^{4}}{4} - a^{4} \right|^{2} + 4 a^{4} \cdot \frac{a^{4}}{4} = \left(a^{4} + \frac{a^{4}}{4} \right)^{3}$$
$$\left(\frac{3a^{4}}{4} \right)^{3} + (a^{4})^{2} = \left(\frac{5a^{4}}{4} \right)^{2} \text{ Prendre } a^{4} = 16$$

4ème méthode:

Teste Prenons $p=s^2+t^2$ et a un entier tel que $a:s^3-t^2$ égale un rapport de 2 carrés. $a(s^3-t^2)$ est donc un carré [inclus dans la démonstration d'Euclide IX, 2; ou réciproque de VIII, 26 ajoutée par Héron et rapportée par al-Nairizi (voir Heath, The Thirteen Baoks, vol. 2, p. 383)].

Donc
$$(ap)^x = (as^2 + at^2)^x = (as^3 - at^2)^x + 4 \cdot as^2 \cdot at^4$$
.
On posora $y^2 = as^2 - at^2 = x$ 2 ast et $z = as^4 + at^3$.

L'exemple cité par l'auteur est $5 = 2^2 + 1^2$, $12: 2^1 - 1^2 - 2^1: 1^2$. (Là encore de mauvais choix de l'exemple numérique rend la règle difficile à dégager).

Teste Prenons deux carrés a^a et b^a tals que b^a soit divisible par 4 et a^ab^a bicarré, Ex.: 9 et 144 = $(5^a)^a$,

$$\left|a^{3}-\frac{b^{3}}{4}\right|^{2}+4a^{3}\frac{b^{3}}{4}=\left(a^{3}+\frac{b^{3}}{4}\right)^{2}.$$

Teste Autrement: Soient a et b deux nombres tels que ab soit un bicarré.

19 Ex: 8 et 32, 32-8 = (16)³. Posons

$$\left(\frac{a}{4} + b\right)^2 = \left|\frac{a}{4} - b\right|^2 + 4 \cdot \frac{a}{4} \cdot b$$
$$(2 + 32)^2 = (32 - 2)^2 + 4 \cdot 2 \cdot 32.$$

Cependant, dit l'auteur, cette méthode ne présente pas la régularité de celle décrite précédemment. (Peut-être entend-il que le choix de a et b n'obéit pas à une los simple comme c'est le cas quand on opère sur des carrés a^a et b^a) (texte 18).

Teme Proposition: Si un nombre a est une somme de deux carrés $a = b^x + c^x$, son double est une somme de deux carrés.

Car
$$2a = 2(b^2 + c^2) = (b - c)^2 + (b + c)^2$$
.

Par suite 2ºa, 2ºa, ... se divisent en somme de deux carrés.

Six et y ont pour p.g.c.d. d. par division par d^2 l'équation (t) sera amenée à la forme $x^{(2)} + \gamma^{(2)} = (cx^{(2)})^2$, où c sera pris sans facteur carré.

Posent $cs'^2 = Z$ nous surces $x'^2 + y'^2 = Z^2$ d'où $Z = M^2 + N^2$ comme plus hant. $M^2 + N^2 = cs'^2$ dépasse tout à fait les moyens de l'époque. Elle admet des solutions s'il existe un entier A tel que c divise $A^2 + 1$. Il en resulte alors que c est une somme de deux carrés. $c = f^2 + g^2$. Su solution et cet:

$$M = \{ (cq^2 + p^2) \}$$
 , $N = \| p^2q + 2cpq + cgq^2 \|$, $\gamma = \| p^2 + 2gpq + cq^2 \|$

Vair Dickson, op. cit., p. 405 fm; Legendre, Théorie des Nombres (Paris, réimp. 1955), Toma f. p. 47 fin, Tome H, p. 203.

L'auteur oppolle $(a^2 - b^2)^2$ et $4a^2b^2$ respectivement: petit et grand nombre (a > b). En fait on peut avoir $(a^2 - b^2)^2 > 4a^2b^3$ on $a^2 - b^2 > 2ab$, $a^2 - 2ba - b^2 > 0$, $(a - b)^2 - 2b^2 > 0$, $(a - b)^2 + b\sqrt{2}$, $(a - b)^2 + b\sqrt{2}$, $(a - b)^2 - b\sqrt{2}$, (a -

Résolution de l'équation:
$$z^2 + (y^2)^2 = z^2$$
 (2)

Observation préliminaire: L'égalité $(a-b)^2 = (a-b)^2 + 4ab$ (3) montre que si on prend (a-b) ou ab égal à un carré l'équation (2) sera satisfaite. De même, si l'on part de $a^2 + b^2 = c^2$, en multipliant les deux membres par a^2 ou b^2 on satisfait à l'équation (2). Les diverses mêthodes de l'autour se remêment à des transformations de ce geure

lère méthode pour résoudre $x^1 + (y^2)^1 = z^2$ (2)

Texte 1# Prendre $x^2 = \left| \frac{b^4}{4} - a^4 \right|^2$ at $(y^3)^3 = 4 \cdot a^4 \cdot \frac{b^4}{4}$. On aura alors $\frac{b^4}{4} - a^4 \Big|^2 + 4 \cdot a^4 \cdot \frac{b^4}{4} = \left(\frac{b^4}{4} + a^4\right)^2$. On peut choisir $a^4 = 1$, $b^4 = 16$ et on aurait le plus petit triplet (x, y, z) vérifiant $(2) (4-1)^2 + 4 \cdot 1 \cdot 4 = (4+1)^2$.

2ème méthode:

Teste L'égalité $4ab+(a-b)^2 = (a+b)^2$ montre que l'on peut choisir a et b tels que;

1)
$$a = ks^a$$
 $b = kt^a$ alors $4ab = (2 kst)^a$,

2)
$$a - b = c^a$$

d'où

12 et 3 sont des exemples de tels nombres a et b:

$$12 - 3 = 3^{\circ}$$
 $12 = 3 \cdot 2^{\circ}$ $3 = 3 \cdot 1^{\circ}$
 $4 \cdot 3 \cdot 12 + (12 - 3)^{\circ} = (3 \cdot 4 + 3 \cdot 1)^{\circ}$.

Recherche de 2, 3, 4 ... nombres dont la somme des carrés est un carré.

Tinte Nous pouvons trouver 2, 3, 4 . . . nombres dont la somme des carrés est un carré.

Cas de doux nombres. Prenons a^a et b^a quelconques, a^ab^a et $\left(\frac{a^a-b^a}{2}\right)^a$ ont pour somme $\left(\frac{a^a+b^a}{2}\right)^a$: Démonstration par les segments.

Cette égalité vaut pour des nombres fractionnaires. Mais dans ce dernier cas, nous ne dirons pus carré, mais mâl, à la manière des algébristes.

Cas de trois nombres. Prenons $a^{1} > b^{2} + c^{2}$. Nous avons $a^{2}b^{2} + a^{2}c^{1} + {a^{2} - b^{1} - c^{2} \choose 2}^{2} = {a^{2} + b^{2} + c^{2} \choose 2}^{2}$.

Tente Démonstration par les segments. Par ce procédé nous pouvons 12 obtenir un grand nombre de triplets de carrés dont la somme est un carré.

Observation: Le procédé est généralisable et l'auteur s'en rand compte. Il n'explicite pas cependant l'égalité suivante. Si $a^2 > b^2 + a^2 + \dots k^2 + l^2$, alors:

$$a^{2}b^{2} + a^{2}c^{2} + \dots + a^{2}l^{2} + \left(\frac{a^{2} - b^{2} - c^{2} - \dots - b^{2} - l^{2}}{2}\right)^{2} = \left(\frac{a^{2} + b^{2} + c^{2} + \dots + l^{2}}{2}\right)^{2}.$$

Texte Trouver on triplet (x, y, z) tel que $x^2 + y^2 = (z^1)^2$. (1) Prendre 13 un triplet (a, b, c) tel que $a^3 + b^2 = c^2$. Poser $x^2 = (a^3 - b^2)^2$, $y^2 = 4a^2b^2$, d'où $x^2 + y^2 = (a^2 + b^2)$ $(c^2)^2$, z = c.

Observation: La solution donnée par al-Khāzia est partielle bieu qu'ingénieuse. Nous pensons que l'unteur avait les moyens de résoudre

$$x^2 + y^2 = (x^2)^2 \tag{1}$$

pour &, y, & premiers entre aux

Posona s2 - Z d'où

$$x^2 + y^2 = Z^2 (2)$$

Comme z et y sont promiers entre eux, donc promiers avec Z, alors:

$$x \leftarrow M^2 - N^2$$
, $y = 2MN$, $Z = M^2 + N^2$

(M et N premiers entre eux et de parités différentes).

Par suite: $s^2 = M^2 + N^2$ a pour solution

$$M = m^2 - n^2$$
 , $N = 2mn$, $z = m^2 + n^2$

(m et a premiers entre oux et de parités différentes).

Done
$$x = (m^2 + n^2)^2 - (2mn)^2$$
, $y = 4mn (m^2 + n^2)$, $z = m^2 + n^2$.

D'ailleura, quels que soient m et n, ces valeurs verifient (1) car

$$[(m^2-n^2)^2-(2mn_1)^2]^2+[4mn(m^2-n^2)]^2=(m^2+n^2)^4$$

L'évalité (1) donne :

$$a = (ac + bd)^2 + (ad - bc)^2$$
 (2)

$$z = (aa - bd)^2 + (ad + ba)^2$$
 (3)

déjà rappelées et immédiates.

On obtient de la même manière:

$$52 = [(ac + bd) (ac - bd) + (ad - bc) (ad + bc)]^2 + [(ac + bd) (ad + bc) - (ad - ba) (ac - bd)]^2$$

Dane

Puda

10

$$e^{1} = (a^{2}c^{2} - b^{2}d^{2} + a^{2}d^{2} - b^{2}c^{2})^{2}$$

$$+ (a^{2}cd + abc^{2} + abd^{2} + b^{2}cd - a^{2}cd + abd^{2} + abc^{2} - b^{2}cd)^{2}$$

$$e^{2} = [f(a^{2} - b^{2})](e^{2} + d^{2})^{2} + [2ab(c^{2} + d^{2})]^{2}$$

Ainsi pa a bien obtenu la solution dérivée

$$(e^2+d^2)(a^2-b^2)$$
 , $(e^2+d^2)(2ab)$ $(e^2+d^2)(a^2+b^2)$

proportionelle à :

$$a^2 b^2$$
 . $2ab$, $a^2 + b^2$, $(a > b)$

De même on verrait que

$$z^{2} = [(ac+bd)(ad+bc) + (ad-bc)(ac-bd)]^{2} + [(a^{2}c^{2}-b^{2}d^{2}) - (a^{2}d^{2}-b^{2}c^{2})]^{2}$$
shoutit à
$$z^{2} = [(a^{2}+b^{2})(2cd)]^{2} + (a^{2}+b^{2})(c^{2}-d^{2})]^{2}$$

solution proportionalle à

$$e^2 - d^2$$
 , $2ed$, $e^2 + d^2$, $(e > d)$

Si x, y sont pairs, on a vu que s = 2s' + x, s' + x nombre composé, Texte z' résidu (fagla), $x'+x=s^2$, $x'=t^3$, $\sqrt{(z'+x)x'}=\frac{1}{s}$, y=st(y) al-

murabbar al-akthar, x,y: al-murabbarayn al-awwalayn) (texto 10, 1.4). D'où la conséquence que l'auteur énonce en général: quand un carré d'entier z^a se décompose en une somme de deux carrés, se racine z se décompose en une somme de deux carrés s' et t' qui sont premiers entre eux ou admettent un diviseur commun ou bien z se décompose en deux nombres plans semblables (a-b et c-d sont plans semblables si

a:b = e:d. Euclide VII, déf. 21). Observation, $x = s^{2} - t^{2}$. y = 2at4 > 1

Si x of y sont premiers entre cux alors s2 of t2 sont premiers entre oux. [si s2 of t2 no sont pas premiers entre cux, a et i out un diviscur commun d'(conséquence d'Euchde VII, 27) et d diviserait x et y]. Plus généralement on peut avoit

1)
$$x = k^2t^2 - k^2t^2$$
 $y = 2k^2t^2$ $z = k^2t^2 + k^2t^2$
10 2) $z = Kt^2 - Kt^2$ $y = 2Kt^2$ $t = Kt^2 + Kt^2$

avec K non carré dans 2). Duns ce dernier cus, ku2 et Kt2 sont plans ensembles car ks.s et kt.t ont laurs côtés proportionnels Kars = Ki t,

Cette égalité devient
$$s2s/2 + t2t/2 - t2t/2 - t2t/2 - 4ts/tt/ = 0$$
 ou $(st/-tt/)^2 = (ts/+tt/)^2$. En posant $ts/>tt/$, $ts/=tt/=tt/+tt$ qui donne $t/ts/-tt/=tt/(s+t)$, $\frac{s}{t/}=\frac{s+t}{s+t/2}$. Ainsi pour $s=4$, $t=3$, on a $s'=7$, $t'=1$, 0 and $t=24$, $t^2=25$.

x/2 + x/2 = 50

2e't' = 14

On peut, par exemple, prendre s et s cousécutifa.

g /2 -- 1/2 -- 48

Taxte

Si on prend $s^0=4$ et $t^0=121$ lesquels sont premiers entre eux z=4+121=125 est un multiple de 5, sans que x=121-4=117 ni $y=2\cdot2\cdot11=44$ ne soient équimultiples de 4 et 3. Comment expliquer la chose? [savoir que dans les triplets (x,y,z),(x',y',z') solutions, z soit multiple de z', sans que x et y soient des équimultiples de x et y']. Cela tient au fait que 125 est le produit de deux facteurs (5·25) qui se décomposent chacun en une somme de deux carrés 5=1+4 et 25=9+16. Tout nombre produit de deux facteurs qui sont chacun la somme de deux carrés se décompose en une somme de deux carrés, de deux manières, comme nous le verrons plus loin. 125=100+25=4+121. D'où deux couples (s,t) différents pour un même z $125=10^2+5^2=11^2+2^2$. Quand z se décompose ainsi une des solutions (x,y,z) n'est pas primitive. Cela est comme le triangle primitif (3,4,5) qui donne naissance au triangle (dérivé) de côtés doubles (6,8,10).

Observation. Le couple (4,121) a fourni à l'auteur le triangle 1172 + 442 = 1252 qui s'associe dans sa peusée avec (25 3)2 + (25-4)2 = (25 5)2. Al-Khāzin a l'air de se demonder comment 1252 s'est décompasé ainsi de deux manières différentes, et pourquoi la solution (75, 100, 125) n'est pas primitive? Cela tient, dit il, au fait que si deux nombres sont la somme de deux carrès, leur produit est une somme de deux carrès de deux mutières

donne

$$u = a^2 + b^2$$
 $v = c^2 + d^2$
 $uv = (ac + bd)^2 + (ud - bc)^2$
 $uv = (ad + bc)^2 + (ac - bd)^2$ (Texto 38)

A mantrera dans le texte 41 que si un nombre est une somme de deux carrés de deux monières, son carré est une somme de deux carrés de quatre mamères (dont certains peuvent se confendre, c'est le cas pour 1252).

$$125^2 = 120^2 + 85^2$$
$$125^2 = 100^2 + 75^2$$
$$125^2 = 117^2 + 44^2$$

L'idée d'al-Khāzin est difficile à suivre. Il semble partagé entre doux préoccupations; Partage d'un carré en somme de deux carrés de plusiours manières, problème repris plus tard d'une façon si magistrale par Fermat [vou T. L. Heath, Diophontus of Alexandria (Cambridge Univ. Press, 1885; Dover repr.), pp. 106-110, 267-276] et la formation de triaugles dérivés c-à-d., de la forme ha. hp. hs.

Montrons, en nous aidant des égalités employées par el-Khâsin, que si

$$s = (a^2 + b^2)(c^2 + d^2)$$
 (1)

alors, parmi les solutions de x2 + y2 = 22, il y en a nécessairement qui sont dérivées.

Le système d'al-Khāzin out

$$\prod_{n=1}^{\infty} \begin{cases}
x = a^2 - a^2 & a > 1 \\
y = 2a & a^2 + t^2
\end{cases}$$

où e at t sont praniers autre eux. Pun pair l'autre impair. Il y a équivalence entre les deux avetèmes. On voit en particulier en égalant les valeurs de y puis celle de a:

$$p^{2} - q^{2} = 4st, p^{2} + q^{2} = 2s^{2} + 2t^{2},$$

$$p^{2} = (s + t)^{2} \text{ et } p = s + t,$$

$$q^{2} = (s - t)^{2} \text{ et } q = s - t.$$

On a bien $\pi = p_g = s^2 - t^2$,

Conclusion: Appelous triangle primitif (ast) on solution primitive one solution (x, y, z)de nombres premiers entre sux. Celle-ci sera fournie par le couple (*,t) où a et t sont premiers entre eux et de parités différentes. L'idée sers reprise dans le paragraphe 8. Dans le paragraphe 6, al-Khazin releve cependent que le système II, où s et s peuvent être quelconques, est ton-Jours solution de $x^2 + y^2 = x^2$.

Pour $t^3=2^2$ et $s^3=3^4$, $x=3^2-2^2=5$. $y=2\cdot 3\cdot 2=12$, et Texto $z = 3^{\circ} + 2^{\circ} = 13$. Le couple (5,12) est primitif (asl). Il engendre des couples de nombres proportionnels dont la somme des carrés est un carré [c-à-d, $(5k)^2 + (12k)^2 - (13k)^2$] De même $(t^2, s^2) - (1^2, 4^2)$ donne $(x,y) = (15.8), 15^3 + 8^3 = 17^2.$

Ainsi pour former (x^1, y^2, z^2) on prendra (t^2, s^2) les plus petits Texte B carrés dans un certain rapport, ils sont donc premiers entre eux comme (1, 4), (4, 9), (1, 16) et on opérera comme plus haut. On n'obtiendra pas deux fois le même couple (x^*, y^*) ni deux couples proportionnels (l'expression arabe est vague: 'ala şūrotihimā, à leur image).

Observation: En effet considérons deux couples générateurs (a,t), (a', t'). Il est facile de voir que si deux des trois rapports $\frac{z^2-z^2}{z'z-t'^2}$, $\frac{2zt}{2z't'}$, $\frac{z^2+t^2}{z'z+t'^2}$, nont égaux alors $\frac{z}{1}=\frac{z'}{1}$ Comme (s, t) et (s', t') sont des couples formés de deux nombres premiers entre eux alors $a = a^{\epsilon}, \ b = b^{\epsilon}$

 $\frac{4^{2}-1^{2}}{4^{2}-4^{2}}=\frac{44}{7/4}$ Ainsi dans le cae $x^2x^2t^2 - t^2x^2t^2 = xx^2t - xx^2t^2$ $a^2 a^2 t^2 - b^2 a^2 t^2 - at a/2 + at a/2 = 0$ 88. ss'(st' + ts') + tt'(st' + ts') = 0, 0B B $(aa_1 + ab_1) (ab_2 - ab_2) = 0,$ $4t^2 = 0^4 - \frac{4}{2} = \frac{4^4}{27}$ d'où

Les autres cas sont immédiats.

Cependant deux couples (s,t), (s',t') différents peuvent produire deux triplets (x,y,t) (x', y', z') tela que $\frac{x}{y_1} = \frac{y}{x'} = \frac{z}{z'}$. Il suffit que $\frac{x}{y'} = \frac{y}{z'}$ ou $\frac{z^2 - y^2}{2z' + 1} = \frac{2zt}{z'^2 - z'^2}$

Comme 12 et 3, $12:3-2^{z}:1^{z}$ d'où 12:3 et $12:3\cdot4$ sont des carrés; de même 8 et 2. Prenons z'+x et z' les plus petits possibles [donc premiers entre eux]. Nécessairement z'+x et z' sont des carrés. [Euclide, VIII, 9].

Posons $z'+x=s^2$ et $z=t^4$. Dès lors $z=s^5+t^2$, y=2st, $x:=s^3-t^2$.

Texte La règle qui donne (x, y, z) à partir de (s,t) est générale, [c-à-d. 6 même si aucune condition n'est posée pour s,t les valeurs $s^2 - t^2$, 2st. $s^3 + t^3$ vérifient $x^3 + y^2 = z^2$].

Pour
$$s = 2$$
, $t = 1$, $(x, y, z) = (3, 4, 5)$.
Pour $s = 3$, $t = 1$, $(x, y, z) = (8, 6, 10)$.

Remarquons que (8, 6, 10) sont doubles de (3, 4, 5). Plus généralement, si x = 4k, y = 3k, alors z = 5k.

Observatson: Al-Khūzia utilite un langage visiblement influencé par Euclide quaod il parle de x^2 impair et y^2 pair les plus petits possibles (texte 5, 1 2) [Euclide VII, 22, VIII, 2, 3, 4; IX, 15]. On trouve également chez Diophante. Etablissons donc maintenant deux triangles rectangles compris sous les mondres nombres, tels que 3, 4, 5 et 5, 12, 13 (Arithmétique, trad. Paul Ver Eecke Paris, 1959, livre III, 19, p. 109). Pour que l'expression d'al-Khāzin fût tout à fait claire, il eut falla dire: les plus petits possibles dans leur rapport. Nous pensons que c'est la pensée d'al-Khāzin, car si on devait prendre à la lettre l'expression les plus petits possibles l'équation $x^2+y^2=z^2$ n'aurait q'une solution (3, 4, 5) alors que l'auteur en donne plusieurs dans le paragraphe même. La même expression utilisée plus lom à propos de z'+x et z' dans (z'+x)x' ne présente plus le même inconvénient puisque le rapport des x'+x et x' est formé. L'expression correcte des deux plus petits nombres dans leur rapport est utilizée au début du texte 8. Pour la rigueur du raisonnement il nous resterant à établir que si x et y sont premiers entre sux (donc x et x le sont aussi) il en est de même de x + x et x', at réciproquement, se qui ne présente aucune difficulté.

Le texte de précise pas que s et l'douvent être de parités différentes (si s et l'étaient de même parité $x=x^2-t^2$ et $s=x^2+t^2$ resaiont pairs tons deux ce qui est contraire au texte).

$$z = mny$$

$$y = \frac{1}{2} (mnp^2 - mnq^2)$$

$$\epsilon = \frac{1}{2} (mnp^2 + mnq^2)$$

est solution de $\alpha^2 + y^2 = z^2$ (Eléments X, 29, lemme 1). Capandant Euclide ne doune que la synthèse et par là il manque d'établir que la solution proposée est générale. Pour estre raison, Bathet en donne l'analyse dans son édition de Diophaute (1621). L'est justement ce qu'al-Khazin a fait ioi.

Nows pouvous nows on tenir sux valeurs de (x,y,z) premières entre elles dans leux ensemble. Le système d'Euclide devient x=pq, $y=\frac{1}{2}$ (p^2-q^2) , $z=\frac{1}{2}$ (p^2+q^2) , où p of q sont première entre sux et imposes.

1. Jean Itard, Les livres arethmétiques d'Euclide, (Paris 1961), p. 163.

Construction en entiers de $x^2 + y^2 = z^2$

Propositions préliminaires

Lemme 1. Daux carrés impairs ne peuvent avoir pour somme un carré.

Texte Supposons que $x^2 + y^2 = x^2$, x et y étant impairs. Donc z est pair 2 (Euclide, IX, 22). De plus

$$x^{2} = (z-y) (z+y) = (z-y)^{2} + 2y(z-y).$$

$$[z-(z-y)] (z+(z-y)] + (z-y)^{2} = x^{2}.$$

Mais

If s'ensuit que
$$[x-(x-y)][x+(x-y)] = 2y(x-y)$$
.

Les crochets sont pairs tous deux. Dans le 2ème membre y et s—y sont impairs. Donc l'égalité est impossible.

Texte Lemme 2. Deux carrés de la forma 2ª no pouvent avoir pour somme un carré.

Si $x=2^p$ et $y=2^q$ (avec p< q) on ne peut avoir $x^1+y^2=z^9$. Il existe s tel que $\frac{x}{y}=\frac{1}{2^n}$ [Euclide IX, 11; voir observation de T. L. Heath,

The Thirteen Books, vol. 2, p. 396]. D'où
$$\frac{x^3}{y^3} = \frac{1}{(2^5)^3}$$
 et $\frac{x^3}{x^4 + y^3} = \frac{1}{(2^5)^3 + 1}$.

Or $(2^8)^3+1$ n'est pas un carré, car en ajoutant I à un carré on n'obtient pas un carré. Par suite x^3+y^3 ne peut être un carré [si x^2+y^3 était un carré, alors $(2^6)^3+1$ serait un carré d'après Euclide VIII, 24].

Texte Lemme 3. $(2m+2n+1)^2 = (2n+1)^2 + 4m(2n+1+m)$, [Euclide II, 8] $(2m+2n)^2 = (2m)^2 + 4(2m+n)n$

Observation. Les démonstrations dans les lemmes 1, 2, sont faites sur des segments comme dans les Eléments d'Euclide.

Formation de $x^0 + y^0 = x^0$

Nous voulons tronver deux nombres carrés l'un impair x^4 l'autre pair y^3 [premiers entre eux] (dans le texte: les plus petits possibles) tels que $x^3+y^3=z^3$. Supposons par l'analyse qu'ils existent. (Posons z-x=2s'). Appelons z'+x: nombre composé ('adad murakkab) et z': résidu (fadla). Alors s=(z+x)+z' et $x^3+4(z'+x)x'=s^3$ [lemme 3]. Mais $x^3=x^4+y^3$ d'où $4(z'+x)z'=y^3$. Il en résulte que (z'+x)x' est un carré, car le rapport de 4(s'+x)s' à (z'+x)z' est le rapport d'un carré à un carré et 4(z'+x)z' est un carré, donc (z'+x)z' est un carré (Euclide, VIII, 24). Par suite z'+x est un rapport de deux carrés (Euclide IX, 2, puis VIII, 26) et z'+x et z' sont des équimultiples des plus petits carrés qui ont le même rapport qu'eux.

est confirmé par l'histoire. 14 Un autre traité sur les triangles rectangles du mathématicien Abû'l-Jūd, 2° moitié du 4° siècle. H., vient d'ailleurs étayer toutes les vues précédentes. 16 Signalons également sur le même sujet un traité d'al-Sijzī (2° moitié du 4° s. H.): Risâla fi jawâb mas'ala cadadiyya wa hiya kaifa najid (murabbacyn yakūn) majmū'uhumā murabbaca (12 pages, Bibl. Hakim M. Nabî Khān Jamāl Suwayda, Téhéran). Nous devous à la courtoisie du Dr. Anton M. Heinen d'en avoir pris counaissance.

14. Wospeke, op. ak., p. 317.

15. Leiden Cod. Or. 168 (14), f. 116-134a.

Sommaire du traité d'Abu Ja far [al-Khazin].
Paris BN MS arabs 2457,49, ff. 2042 - 2152.

Ce sommaire n'est pas à proprement parler une traduction, cependant nous croyons qu'il ne laisse men échapper du texte. Les passages importants ou difficiles y ont reçu des développements plus grands. D'autre part, les démonstrations d'al-Khāzin bien qu'exposées sur des exemples numériques sont générales et entendues par l'auteur comme telles: nous n'exagérons donc pas leur portée en représentant les nombres par des lettres, ce qui a l'avantage de rendre les démonstrations plus claires. Des observations imprimées en petits caractères et précédées de la mention observations accompagnent certaines questions et sont étrangères au texte; de même en est-il des expressions placées entre crochets dans le texte même. Dans un souci de meilleure présentation et pour faciliter le travail de référence nous avons sectionné le mémoire en paragraphes.

Remarques

- 1. Nous avons mis en italique dans le texte certains mots ou phrases clés. Le nombre au dessous du mot saxe désigne le numéro du paragraphe.
- 2. Nous employous le signe : pour désigner un carré d'entier (ou parfois de rationnel: rapport d'entiers).
- 3. Les nombres dont il est question sauf mention expresse du contraire sont des entièrs naturels.
- 4. Certaines phrases insérées entre crochets n'appartiennent pas au texte et sont ajoutées en annotations.

ques mémoires qui nous sont restés sur $x^2 + y^2 = z^2$ nous font revivre les efforts conjugués, les erreurs commises, les insuffisances et les corrections successives. Nul donte qu'à cet effort collectif d'édification bien des mathématiciens célèbres ou obscurs n'aient participé dans les divers centres scientifiques: Baghdad, Chiraz, Rayy, Marw, Balkh, et autres. 18

La préface de M3 presente un détail historique qui confirme cette persistance dans l'effort. Motivant l'envoi de son mémoire. Abū Jacfar écrit: Frère je t'avais adressé un mémoire sur la construction des triangles rectangles. J'y avais énoucé, sans démonstration par les segments, que deux nombres dont la somme des carrés est un carré ne pouvaient être impairs (on aura remarqué la ténuité du résultat). Or cette proposition est absente du mémoire M2 et il est difficile de lui trouver là une place naturelle dans l'enchaînement du raisonnement. Il faut donc admettre qu'Abū Jacfar fait allusion à un 3° mémoire qu'il avait adressé également à cAbdallah b. cAlī. La chose n'a rien qui nous surprenne. Il est tout normal qu'Abū Jacfar, et les autres chercheurs creusant la question, aient rédigé au fur et à mesure bon nombre de notes brèves sur ce sujet alors à l'ordre du jour.

Nous possédons d'ailleurs sur les triangles rectangles numériques un fragment de traité anonyme, Paris MS 2457, ff. 81s-86a, dont la qualité montre un progrès sensible sur le mémsire M2 d'Abū Jacfar. Les deux traités M2 et anonyme, ne manquent pas d'ailleurs de points de ressemblance, ce qui avait fait dire à F. Woepeke, à une époque où les conditions de l'activité scientifique arabe étaient moins claires: "On ne pourra méconnaître l'uniformité que présente en général la marche suivie dans l'exposé de la théorie des triangles rectangles numériques, tant par l'auteur du fragment anonyme que par Abou Dja'far M. b. al-Hoçain, uniformité qui pouvait indique, une certaine tradition d'école, un certain cadre commun qu'il était d'usage de remplir, en enrichissant d'ailleurs le sujet d'autant d'observations et de découvertes originales que possible. F. Woepeke en venait à supposer qu'il existait des rapports plus ou moins suivis entre les mathématiciens d'Orient, ce qui

^{12.} De cette multiplicité d'afforts, bien naturelle d'affleure, nous donne une idée le bref chapitre des triangles rectangles numériques $(a^2=b^2+c^2)$, (3), qu'al-Samaw'el insère dans son livre al-Bahw cité en note l., al-Samaw'al y est représenté par $2(a-c)(a-b) = [a-(a-c)-(a-b)]^2$ coaté quence de(3). Al-Sipti par l'égalité bien connue et tres aucienne $a^2\pm 2bc$ sont des carrés:lbn al-Haytham par le construction d'un triangle rectangle dont un côté de l'angle droit est connu (al-Bâhw, op. cit., pp. 146-151). Dans un chapitre voisin, al-Samaw'al cite un nom obscur. Jaffar b. 'Ahdalláh al-Ḥarīri (pp. 155, 159, 117) auteur de l'identité b(a+b+c) + ac = (a+b)(b+c). D'autre part on doit à Ibo Yûnes une tote un la proposition. ''Deux carrés impairs n'out pes pour somme un carré'', Berlin 6008, £. 437a-438b.

^{13.} F. Whepcke a truduit et analysé remarquablement les traités, Parie MS 2457, & 81a-86a anonyme, et celui d'Abu Jaffar, Paris MS 2457, & 86b-92a, "Rocherches our plusieurs ouvrages de Leonard de Pisc...," Atts dell'Accademia Pontificia du Nuovi Lincus, 14 (1861), pp. 211-227, 241-269 (pour le traité anonyme): pp. 301-324, 343-356 (pour le 2º traité), cf. p. 31?

personnage qui a joué le rôle important d'intermédiaire et d'arbitre entre les savants de son temps et à qui sont adressés d'ailleurs les deux mémoires M2 et M3.º Cette discussion est intéressante car elle nous révèle l'existence d'une correspondance scientifique entre les mathématiciens – ce dont nous avons par silleurs de nombreux témoignages¹¹ – ainsi que les tentatives répétées entreprises par les Arabes, tôt dans la première moitié du 4° siècle H., pour résoudre $x^a + y^a = z^a$ (1) ou la difficile $x^a + y^a = z^a$ (2). Les quel-

11 La correspondance june un rôle important dans la vie scientifique de l'époque; alle supplée les déficiences de l'édition et épargne aux consultants des voyages longs et pleins de risques, an môme temps qu'elle assure aux consultés une plus grande notociété et aussi des sujets de recherche. Bien des écrite out vu le jour sur une sollicitation amicale. Dans l'Orient d'hier et de jadis où le temps n'aveit pas valeur de mounaie ces demandes ne semblaient pas déplacées. Citons les 15 lettres adressées par Abù Nasr b. Traq à son élève sl-Birant pour lever certaines de sea difficultes mathématiques et où il l'encourage dans la voie de l'étude (Hayderabad, 1948), la réponse d'al-Sijai à dix quastions que hi avait adressées un géometre de Chiras, Pane MS 2457, 181a 186h, la lettre d'al-Suzi (Ahmad b. Muhammad b. 'Abd al-Jafil) à Abu'l-Husayn Muhammad b. 'Abd al Jalil (son pere) et dont il dit être d'esclave, min 'abdih (Paris MS 2457, 1376-139a). Thu Tâwija (m. 664 H.) nous apprend dans Farsy of-makmam ff taribh "ulama" of-nujum (al-Najuf, 1368 H.), p. 127, que le pere d'al Sijzi, M h. "Abd al-Jalii était versé dans le screoce des astres et qu'il était l'auteur de livres comme à l'époque d'Ibn Tawiis Kutáb al-ziját fi intikhráj al-hylaj w'al-hadkhudd et Magalo fi fath al-báb (l'édition très factive porte al-Sinjari au heu d'al-Sinzi, erreur due au déplacement d'un point discritique. Citona autu la lettre d'ul-Signi à Abū 'Alî Nazif b Yumu en 970 A.D MS Paris 2457 f 136b-137a, la lettre d'al-Hashimî (vit en 320 ll) à l'émir Abû'l-hadl Je'for b. nl-Muktoff eur le colcul des radicaux, MS Paris 2457, 16, f. 76s-78s, la correspondance entre Abū Ja" far al Khaza et le geomètre Ibrahim b. Sinàn (296-335 H 908 - 946 A.D.) qui commença ra carrière de chercheur à l'âge de 15 ans (Ibn Cráq, Rusă'd: Tajhih nij al-Şafâ'ıh (Hı derabad, 1948), p. 45, Ibrahım b. Sının, Rasa'd: Kush fi haraksı al-shame (Hayderabad, 1948), p. 70 la correspondance entre si-Buzzám (m. 387 H.) et le cadi methématiclen Abū 'Alī al-lifubūbi (lba 'Irāq, Rasā'si Al-qusiyy al-falakiyya (Hyderabad, 1948), p. 2. l'aboudante correspondance d'Abû'l-Jâd Ibn al-Layth avec ses contemperains. Al Sijzi (Leiden Cod. Or 168, 13, 108b-113) nivec al-Buruni op cit., f. 45a-54a), avec (bu al-Chady? (op cit., f. 116-134a), ovec Abū Ja'far al-Khānu (op en , f. 102-108a), voir auns notre article "Tosbifal-dillira", JH 45, 1 (1977), 379 380, 373. Rappelone eusei le correspondance scientifique evec les pays musulmens de Fréderic II, (1194-1256 A. D.) qui conquissat l'arabe et auxi le grec, le latin, l'italien, l'allamand et le français (Amari, "Questions philosophiques adressées our sevents musulmans par l'empereur Fréderic II", Journ. As., 5° a., 1 (1853), 240-274. A. F. Mehren, "Correspondence du philosophe soufi thu Sah'in Abd oul-Haqq avec l'empereux Frédéric de Hohenstaufen sur l'immortalité de l'àme," Journ 4s., 7º 4. 14 (1879), 342-344, 347, Aldo Micli, La Scienca Arabe (Leiden, 1966), pp. 152, 209. G. Sarton, Introd., vol. 11, part 11, p. 600 et pp. 575-579. Al-Qaswinj, Athér al-bildé un akhbér al-sibéd (Gottingen, 1848), p. 310 (Voir sussi Ibn Khellikan, Wafeydt al-A'ydn, vol. 4, (Caire, 1948), pp. 396 et suiv., où us habitant de Dumes interessé par les muthématiques ecrit à Ibu Yûnus (Mossoul) et reçoit quelques mois plus tard la réponse à ses difficultés (en 633 II) Arrètant ses une énumeration que nous pourrions allonger considérablement disons la nécessité de la correspondance entre astronomes observant en des heux differents pour concerter leurs observations et remarquons que dans de nombreux manuscuta les su-tête des mémoires ont disparu cachaut ajust le caractère epistolaire des écrits. D'autre par t cette pratique est commune à toutes les branches du savoir. Ann Aqà Buzurg, dans sa Dari's, vol 2, (Najaf, 1355 H.), pp. 71-94, donne une longue énumération de 186 traités religieux, juridiques ou philosophiques composés en réponse à des quertions posées par des correspondants, et il considéra que la plus grande partie des mêmoires dus à la correspondance a dû se perdre.

la théorie des nombres en général. Diophante y est nommé expressément. Ce mémoire que nous désignerons sous le sigle M3 traite de la résolution en nombres entiers de $x^2+y^2=z^2$, de $x^2+(y^2)^2=z^2$, $x^2+y^2=(z^2)^2$ et d'un certain problème que l'on peut qualifier de diophantien, encore qu'il ne figure pas absolument dans l'Arithmétique de Diophante. Calculer x rationnel pour que x^2+K égale un carré de rationnel. Il existe un 2^n mémoire d'Abū Jafar M2 sur le même sujet: construction des triangles rectangles en nombres entiers. Paris M5 2457 fol. 86b-92b mais la méthode d'approche de la solution y est tout à fait différente.

L'auteur y construit un tableau numérique donnant tous les triplets (x, y, s) solutions de $x^2 + y^2 = z^2$ jusqu'à $s \le 461$ et y étudie diverses propriétés de ces triangles." Ce mémoire est apparemment antérieur à M3 si on en juge par les inadvertances et les erreurs qui s'y rencontrent. On sent que l'auteur n'a pas acquis la pleine maîtrise de son sujet alors que dans M3 la solution de $x^2 + y^2 = z^2$ se présente sous une forme élégante, presque classique, comme on le verra. La préface de M2 est intéressante du point de vue historique, elle nous apprend qu'Abū Ja°far avant été précédé dans sa tentative par Abū Muhammad al Khujandī, mais que la formule établie par ce dernier pour la solution de $x^2 + y^2 = z^2$ n'était pas générale. De même Abū M. al-Khujandī avant eru démontrer l'impossibilité de $x^3 + y^3 = z^3$ en nombres entiers, mais Abū Ja°far avait montré son erreur. Il en avait résulté une discussion entre les deux auteurs, discussion qu'avait suivie 'Abdallāh b. 'Alī l'arithméticien,

B. MS Paris 2457, ff. 213a, 214b.

9. Si x, y, z n'ont pas de diviseur commun **ni**ors la solution générale de l'équation $x^2 + y^2 = z^2$ est $z = a^2 + b^2$, $y = a^2 - b^2$, z = 2ab, où a et b sopt premiers sotre eux, l'un pair, l'autre impair. Par suite pour obtenir toutes les va-

| leurs possibles de s. Abû Jac'far čerit |
|--|
| dans une 1ère colonne, les nombres 1, 2, |
| 3,, 71; dans nue 2º colonne leurs car- |
| rés 17, 22, 32, . , n3. Il ajoute alors 12 à |
| 12, 22, , n2 et écrit les sommes obtenues |
| dans la ligne horizontale passant par l |
| Puls il ajoute 22 h 22, 32, n2, at |
| écrit les resultats dans la ligne horizon- |
| tale passant par 2. Il suffit de choisir |
| dans les lignes horizontales les s'impairs: |
| a2 et b2 en découlent d'où y et x. |

| 1 | 1 | 2 | S | 10 | 17 | 26 | 37 |
|---|----|----|----|----|----|----|----|
| 2 | 4 | 8 | 13 | 20 | 29 | 40 | |
| 3 | 9 | 18 | 25 | 34 | 45 | | |
| 4 | 16 | 32 | 41 | 52 | |) | |
| 5 | 25 | 50 | 61 | | | | |
| 6 | 36 | 72 | | | | | |

| Ams | $17 = 1 + 16 = 1^{2} + 42,$ |
|-----------|--|
| Pay auite | y = 42 - 12 = 15 at $z = 2.441 = 8$. |
| | $29 = 4 + 25 = 2^2 + 5^2$ |
| Dane | $v = 52 - 22 = 21$ et $z = 2.5 \cdot 2 = 20$. |

10. Les éteurdories ou les errours sont fréquentes, semble-t-il, dans l'enuvre d'al-Khâzin. Le mémoire M3 n'en mauque pas; et voir: Abu Nagr h 'Irâq, Tajáih sij al-safá'ib (Rasú'il Abi Nagr, Byderabad, 1948), Al-Birūnī, Tamhīd al-mustagur, (Rasá'il al-Birūnī, Hyderabad, 1948), pp. 77-78.

en même temps qu'il traduit l'Arithmétique de Nicomaque et revoit la traduction des Eléments d'Euclide² fait des propriétés des nombres l'objet de ses méditations et on lui doit des écrits qui restent parmi les œuvres mathématiques srabes les plus profondes en même temps qu'il frôle le raisonnement récurrentiel dans certaines relations numériques.⁸ A en juger par la liste de ses ouvrages, il ue semble pas que Thäbit se soit intéressé à l'Arithmétique de Diophante. De ce livre aucune trace non plus dans l'Algèbre pourtant si riche de Shujāc b. Aslam, qui d'après nous a fleuri autour de 265 H.⁸

Dès le début du 4° siècle H. l'influence de Diophante se fait cependant sentir et elle persistera jusqu'à la fin du siècle et bien entendu au-delà. Al-Būsjānī (m. 387 H.), venu de la Perse Orientale touche Baghdad en 348 H., à un moment où Baghdad vit des années relativement calmes sous le règne du bouyide Mu'izz al-dawla. Il écrit un "Commentaire sur le livre de Diophante" un "livre d'imitation à l'Arithmétique" (théorie des nombres ou livre de Nicomaque?), le "livre des démonstrations employées par Diophante et celles employées par l'auteur dans son Commentaire". Or, avant d'arriver à Baghdad il avant reçu son instruction sur la théorie des nombres. al-'adadiyyat, et les questions arithmétiques de ses oucles Abū 'Amr al-Maghazilī et Abū 'Abdallāb M. b. 'Anbasa, auteurs d'ouvrages perdus.'

Le mémoire que nous publions; Paris MS 2457, f. 204a – 215a, appartient à un auteur qui est également de la Perse Orientale: Abū Ja°far Muhammad b. al-Ḥusayn al-Khurāsānī al-Ṣāghānī al-Khāzm dont le nom et l'activité remplissent la première moitié du 4° siècle H.⁷

Objet du mémoire

Le mémoire d'Abû Jacfar relève de cette catégorie d'ouvrages nés sous le signe de l'activité qui règne autour de l'Arithmétique de Diophante et de

- La formule attribuée par Proclus à Piston pour la construction des triangles rectangles numériques était connue des Arabes, $[(m-1)\{m+1\}]^2 + (2m)^2 = (m^2+1)^2$. Elle ûgure, par ex., dans un mémoire aponyme dont il seru question plus tard (voir note 14).
- 2. Al-Fibrist, p. 385, Al-Qifti, Ikhbar, p.47; T. L. Heath, The Thirteen Books of Euclid's Elements (New York, Dover Publ., 1986), vol. 1, pp. 75-76.
- 3. F. Waepake, "Notice sur une théorie ajoutée par Thábit b. Korreh", Journ. As., 20 (1852), 4° s., 420-429 (sur les nombres smisbles). Voir le jugement de G. Sarton sur les quadratures de Thábit, Introd., vol. 1, p. 600.
- 4. Ibn Aslam, Al-Jabr w'al-muqdbolo, MS Qara Mustafa, 379. Adel Anbouba, Un algébriste arabe, (Beyronth, 1963), Horizone Techniques du Moyen Orient, nº 2, pp. 6-15. Adel Anbouba, "L'algèbre arabe sua 1Xº et Xº etècles. Aperçu général," Journal for the History of Arabic Science, 2(1978), 66-100.
 - 5. Al-Fibrust, p. 498; al-Oifti, p. 168.
- Voir les évènements des années 336-350 H., dans Ibn al-Jawzī, Al-Muntagim (Hyderabad, 1357-8H.), vols. 6 et 7.
- 7. Pour quelques détails biographiques sur Abû Jafar (et "Abdalláh b. "All dont il sera question plus lom) on vondra bien se reporter à l'article Anbouba, "L'algèbre arabe", pp. 89-90 Voir aussi pp. 98-100.

Un Traité d'Abu Ja far [al-Khazin] sur les triangles rectangles numériques

ADEL ANBOUBA*

Introduction

L'intérêt des Arabes pour la théorie des nombres a commencé aussitét que le 3ª siècle H. A la base de cet intérêt se placent les trois livres srithmétiques des Eléments d'Euclide, le Xème, l'Arithmétique de Nicomaque de Gérase, l'arithmétique de Diophante, certaines questions de quadratures et à n'en pas douter des traités ou fragments de traités grees obscurs qui ne nous sont pas parvenus, voir même des passages de philosophes grees. Th' ābit b. Qurra

* Institut Moderno du Liban, Fapar-Jdaidet, Beyrouth, Liban. Cet article envoyé à l'edition ausi tôt que mai 1978 a subì, comme on le voit, un retard accidental assez long. Entre temps nous avons appris que le Dr. Abgrad Saídan avait public dans la revue Dirását, de l'Univereté Jordanienne, (décembre 1978), le mémoire objet de gotre article (avec une anulyse en langue anglasse): Pans MS 2457, 49 (non 41), ff 2044- 215a. Nous nous sommes demandé alors si nous de renoucerions pas à notre publication. Mais outre qu'une variété d'éditions d'un même texte anneu peut être de quelque utilité pour les chercheurs, nous avous pensé que la partie française de notre article en justifiait l'appariting. Il est vrai que le Dr. Saidan écut "This is the text of the tract translated by Woopeke in Aui dell' Acc points d, maps Lincel 14 (1861). It is edited to form chapter two. . . " (op.est. p.?). Ea fait, Woepeke dont la vie fut, kélas, assez bràve, n'a pas traduit en français le texte concerné ici, mais Paris MS 2457, 19, ff 82-86a, fragment d'un trasté anonyme et MS 2457, 20, ff. 86b-92a d'Abū Ja'fer dont on tronvers l'analyse française dans Woepcke, op.est. pp. 211-227, 241-269, et pp. 301-324, 343-356 respectivement. Nous profitors de rette occasion pour remerciar ici le Conservatour des manuscrite orientaux à la Bibliothèque Nationale de Paris, Mile M.-R. Séguy dont nous avious sollicité et obtenu, su début de 1978, l'autorisation de publier le mémoire d'Abū Jaffar. Notze reconnaissance va également à Mile M.-T. Deharnot qui « la avec beaucoup de som le sommaire français de notre article et dout les remarques et les auggestions nous out permis de reprendre la rédaction de certains passages at d'y apporter des rectifications.

1 Nous ignorous si des commentaires de l'Anthmétique de Nicomaque furent traduits an arabe; la chose est plausible, les noms des commentatours Proclus, Jean Philopon, Jamblique n'étaient pas étrongers aux Ambes. (Al-Qift, Ibbár al-'ulamá' (Caire, 1326 II), pp. 44, 70, 232. G. Sarien, Introduction to the History of Science (Baltimore, 1927) vol. 1, pp. 253, 351 T. L. Heath, A Monad of Gresk Mathematics (Oxford, 1931), p. 62 Al-Qift cite de Proclus d'Alexandrie un ouvrage sur "la usture des nombres, en 6 livres" (Dans l'édition, Proctus pour Proclus). Ibn al-Nadim nous appraud qu'on avait écrit des abrègés du livre de Nicomaque (al-Fibrist, Carre, a. d. p. 391). On doit à al-Kindi (m. 257 H.) un mémoire sur les nombres amployés par Platon dans sa Palitique (al-Fibrist, p. 373). Al-Samew'al 6° c. H. cite un livre sur les nombres, apparemment apocryphe, attribué à Pythagore. (Al-Bāhir, éd. Ahmad et Rashed, (Damas, 1972), pp. 9, 120, 122, Que l'on compare les nombres évaqués comme bases de numération par al-Jāhig (al-Torbi" w'al-tadwir, éd. Pollat, (Damas, 1955), p. 31) et le nombre chous par Platon pour la population de la cité idéale (Les Lois, III, VI, coll. des U. de France. Tome XI, 2° p., trad. E. des Places, (Paris, 1951), p. 93).

ملخصات للفائحات للكيشورة في للميتشم للفاتب

المصدر الأصيل فيئة الكواكب المنسوبة الى قطب الدين الشيرازي جورج صليبا

لقد نُشرت قبل اثنتي عشرة سنة دراسة وصفت فيها هيئة الكواكب العليا كما ارتآها قطب الدين الشيراري . وفي تلك الدراسة اثيرت نعض الشكوك حول تلك الهيئة وحول كونها من ابتكار قطب الدين نقسه ام انه اخذها عن فلكي سابق له .

قي هذه المقال نثبت نصاً من مخطوط محفوظ في اكسفور د نحت رقم مارش ٢٧١ نبرهم فيه ان الهيئة المنسوبة الى قطب الدين الشيرازي كانت في الواقع من تأليف الشيخ الامام مؤيد الدين العرضي الذي صنف هيئته تلك قبل مجيئه الى مراغه وقبل ال يؤلف قطب الدين هيئته بحوالي ثلاثين سنة تقريبا . ولما كانت الهيئتان متطابقتان كان لا بد من اعتبار هيئة قطب الدين نسخة عن الهيئة التي ابتكره، مؤيد الدين العرضي .

والنص الذي يثبت عدم اصالة هيئة قطب الدين هو ما قاله هو بنفسه في كتابه و لهية الادراك و والذي الفه سنة ١٢٨١ م > حين قال :

« قال رمض افاضل المتأخرين من اهل الصماعة ههنا ان الشيء اللمي يجعل علامة لمبدأ حركة يحب ان يكون ساكناً بالنسبة الى المتحرك ليكون تباعد المتحرك عنه وتقاربه البه بحركة المتحرك وحده ...

هلا يمكن أن يكون قطب الدين يتكلم عن نفسه عندها يذكر « بعض أفاصل المتأخرين ا وعندما ينسب الى هذا المجهول رأيًا لا يوافقه عليه . أما المجهول هذا فيس سوى مؤلف المخطوط مارش ٦٣١ و هو مؤيد الدين العرضي المتوفي سنة ١٣٦٦ م أد يقول : و ان الشيء الذي يفرض علامة لمبدأ حركة متحرك يجب ان يكون ساكناً بالسبة الى المتحرك ليكون تباعله المتحرك عنه وتقربه اليه انما هو بحركة المتحرك وحده و (مارش ١٢٤ ص ١٣٤ ظ) .

ونظراً لاهمية هذا المخطوط (مارش ٦٣١) التاريخية فقد قمنا ياعداده للطبع في مكان آخر وافردنا هنا منحقاً عربياً يقتصر فقط على هيئة الكواكب العليا ترجماه الى الانكليزية كنموذج لعمل المعرضي وكبرهان على كونه هو الواضع لهذه الهيئة وليس قطب الدين الشيرازي .

اما اهمية هذه الهيئة لجديدة التي ابتكرها العرضي فيمكن في كونها اول هيئة تُكتشف الى الآن وفيها يستطيع العرضي ان يرد بشكل ناجع على عبوب هيئة نظلمبوس اليوناني . ولتبيان الفرق بين هيئة العرضي وهيئة بطلمبوس ارفقنا النص برسوم تبين هيئة الكواكب العلياكما توهمها كل من هذين الفلكيين .

اما الاشكال الوارد في هيئة بطلميوس والذي تمكن العرصي ال يتجنبه فيلخص في هيئة الكواكب العليا في ان بطلميوس جعل مركز فلك التدويريدور بسرعة مستوية حول مركز جديد غير مركز حامده سماه مركز معدل المسير . وهذا مستحيل كما بين ذلك الله أله في القرن الحادي عشر الميلادي .

اما مخطوط اكسفورد قلا يحوي سوى وصفا لهذه الافلاك وحركاتها . والرسم الوحيد المرفق بالبص اشير اليه على الهامش بعبارة لا هذا الشكل خطألا . لذلك رأينا ان تعيد رسم هيئة هذه الافلاك حسب مقتضيات النص واثبتناها تسهيلاً للقارىء الذي يود تتبع الوصف الهندسي لهيئة العرضي الجديدة .

تحلص الآن الى القول بان الملحق العربي يعطينا لمحة ولو وجيرة عن اعمال العرضي وعن الدور الذي لعبته هذه الاعمال في كتابات الفلكيين الآخرين من امثال قطب الدين الذين لم يذكروا هيئة العرضي فحسب بل رأو: ان يوردوها كاملة في كتبهم ويتبنوها حتى تحسب وكأنها من اعمالهم هم . اضف الى ذلك ان هذه الاعمال الفلكية للعرضي وغيره تشير الى نشاط لم يسبقه مثيل من حيث الاصالة العلمية طوال القرون الوسطى . ولن تتمكن من التعرف على هذه النصوص ودراستها دراسة علمية وافية .

أبر الوفاء البوزجائي ونظرية ايرُن الاسكندراني

ا. س. كندي و مصطفى موالدي

تحتوي مخطوطة المكتبة الطاهرية بدمشق ذات الرقم — ٤٨٧١ — على عدد من التحقيقات العربية للمقاطع الفلسفية من العصور القديمة ، وقد حقق ونشر العديد منها إن ما تبقى من المخطوطة نفسها يتضمن العديد من الاعمال العدمية والقسم الاكبر منها وحيد وله اهمية تاريخية كبيرة .

وهذه الدراسة تناقش احد نصوص المخطوطة ، وهي دراسة صغيرة تتناول الصفحة رقم / ٨٢ / من المخطوطة .

لقد ذُكر في بداية النص اسم شخصيتين هامتين وكلتاهما معروفة في تاريخ العلوم الدقيقة أولاهما أبو الوفاء البورجاني (٩٤٠ – ٩٩٨ م) المهندس والفلكي والرياضي (واضع البرهان للمسألة المبحوثة) ولد في بوزجان وعمل وتوفي ببغداد ، ثانيتهما الفقيه أبو علي الحسن بن حارث الحبوبي معاصراً للبوزجائي ، كما يؤكد ذلك النص المدروس وكذلك ابو ناصر متصور بن عراق حيث يشير الى رسالة ارسلها مع ابي الوفا الى الحبوبي تتضمن بعض التطورات في المثلثات الكروية .

وهذه المسألة استرعت اهتمام العديد من العلماء كأرشميدس وايرُن والديروني والحسازني وعيرهم وتناولوها بالبحث والدراسة وببراهين عديدة ومختلفة .

$$\sqrt{\left[\left(\frac{c+b}{2}\right)^i-\left(\frac{a}{2}\right)^i\right]\left[\left(\frac{c-b}{2}\right)^i-\left(\frac{a}{2}\right)^i\right]}$$

حبت (من اطرال اضلاع المثلث $c = \overline{AB}$, b = AG . $a = \overline{GB}$) حبث (

فقد الطلق البوزجال لبرهان مسألته من الفرضيات التالية :

خد مثلثاً مسا $\stackrel{\Delta}{AB}_G$ مدد الصلع \overline{AB} الى H بحيث يكون AB_G مدد الصلع AB_G ونصّت BB ي AB_G واسقط العمود AB على AB_G ورسم نصمي دائرة BB و BB قطر اهما BB ملى الثرتيب .

ورسم الأطوال التالية بحيث تكون على الشكل التاني :

 $B\bar{T} = B\bar{E}$

 $\overline{EL} = \overline{AZ}$

 $\overline{BY} = \overline{DE}$

 $\overline{BK} = \overline{AZ}$

والبرهان على مسألته اعتمد على مقدمتين وهما :

$$\frac{\overline{HB}}{\overline{BC}} = \frac{\overline{DE}}{\overline{AZ}}$$

المقدمة الأولى :

ولبر هان المقدمة الأولى اعتمد بشكل أساسي على العلاقة التالية .

 $\overline{BA}^{0} + \overline{AG}^{0} = \overline{BD}^{0} - \overline{DG}^{0}$ رعلی نظریة نیئاغورت

 $\overline{TZ}^{1} = \overline{YK}^{1} = \overline{AD}^{1}$

القدمة الثانية 🖫

وللبرهان على المقدمة الثانية فقد الطلق البوزجاني من العلاقة النالية :

 $\overline{BZ}^2 + \overline{ZA}^1 = 2 (\overline{BZ} \cdot \overline{ZA}) + \overline{AB}^1$

 $\overline{BZ}^1 = \left(\frac{b+c}{2}\right)^3 \cdot \overline{ZA}^1 = \left(\frac{b-c}{2}\right)^3$

حيث

أما البرهان الاساسي لمسألته التي يمكن أن تصاغ كالنالي :

 $(\overline{B}\overline{Z}^{0} - \overline{B}\overline{E}^{0}) (\overline{B}\overline{E}^{0} - \overline{A}\overline{Z}^{2}) = \overline{ABG}^{0}$

$$(\overline{BZ^2} - \overline{BE^2}) = (\overline{BZ^1} - \overline{TB^3}) = \overline{TZ^1}$$
 حبث لدينا وبالاعماد على $(\overline{BE^2} - AZ^2) = (\overline{BE^2} - \overline{EL^2}) - \overline{BL^2}$ خبث نظرية فيثاغورث

وانطلاقاً من المقدمة الاولى :

$$\frac{\overline{HB}}{\overline{BC}} = \frac{\overline{DE}}{\overline{AZ}} \implies \frac{2\overline{ZB}}{2\overline{BE}} = \frac{\overline{DE}}{\overline{AZ}} \implies \frac{\overline{ZB}}{\overline{BE}} = \frac{\overline{DE}}{\overline{AZ}}$$

وقلك بالاعتماد على

$$\frac{\overline{ZB}}{\overline{BT}} - \frac{\overline{YB}}{\overline{BK}} \quad (1) \quad (\overline{BE} = \overline{BT} \ \ \overrightarrow{YB} = \overline{DE} \ \ \overrightarrow{AZ} = \overline{BK})$$

 Δ Δ متشابهان ZTB ، YKB متشابهان

$$\hat{K} = \hat{T} = i \overset{\circ}{\mathcal{C}} \overset{\circ}{\mathcal{C}} \Rightarrow \overrightarrow{YK} / / \overrightarrow{TZ}$$

من تشابه المثلثين يمكن كتابة العلاقة التالية ;

$$\frac{TZ}{\overline{KY}} = \frac{\overline{TB}}{\overline{BK}} \implies \frac{\overline{TZ}^2}{\overline{KY}^3} = \frac{\overline{TB}^2}{BK^3} \implies \frac{\overline{TZ}^3 - \overline{KY}^3}{\overline{TZ}^3} - \frac{TB^3 - \overline{BK}^3}{\overline{TB}^3} \quad (2)$$

واعتماداً على العلاقات التالية :

$$\left\{egin{array}{ll} \overline{TZ^a}-\overline{KY^a}=\overline{AD^a} & (& \overline{BL^a}) \end{array}
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وبعد تعويض العلاقات الثلاث السابقة في العلاقة (2) ينتج لدينا

$$\frac{\overline{AD^{3}}}{\overline{TZ^{1}}} = \frac{\overline{BL^{3}}}{\overline{BE^{3}}}$$

رما ان $\widehat{BE}=rac{a}{2}$ الارتفاع ولدينا \widehat{AD} اذاً

$$\overline{AD}^{1}$$
, $\overline{BE}^{0} = \overline{ABG}^{2}$ $\longrightarrow = \overline{TZ}^{0}$, \overline{BL}^{3} (3)

 $egin{align} & \Delta \ & ZTB & DT \end{array}$ وبتطبیق نظریة فیثاغورث علی المئٹ $\overline{TZ}^{0} = \overline{BZ}^{0} - \overline{BT}^{0}$ ینتج

رِعا أن $\overline{BT} = \overline{BE}$ اذاً

 $\overline{TZ}^{\bullet} = \overline{BZ}^{\bullet} - \overline{BE}^{\bullet} \tag{6}$

وكذلك بتطبيق نظرية فيثاغورث على المثلث بتطبيق نظرية فيثاغورث على المثلث $BL^* = BE^* - EL^*$

ریا ان $\overline{EL} = \overline{AZ}$ بتنج

 $\overline{BL}^{3} = \overline{BE}^{3} - \overline{AZ}^{6}$ (5)

وبتطبيق (4) و (5) على (3) ينتج :

 $\overline{ABG} = \overline{BE}^2 - \overline{BE}^2 - \overline{BE}^2 - \overline{AZ}^2$

وبذلك نتوصل الى برهان مسألة مساحة المثلث بدلاله الأضلاع للبوزجافي وبشكل مختصر، بينما نجد في القسم الأجنبي من هذه المجلة البرهاد الكامل للمسألة مع مناقشة النص العربي وتحقيقه ومقارنة برهان البوزحاني مع حيول أخرى للمسألة نفسها داءاً من حل أرشميدس .

بقاء علم الفلك العربي في العبرية

ب. غوللستاين

إن المخطوطات العبرية مصدر هام للعلوم العربية ، وهي كثيراً ما تحتوي على نصوص لم تصنف المخطوطات العبرية مصدر هام للعلوم العربية أنواع للنصوص : ١ – نصوص عربية مكتوبة بالحرف العبري ، ب – ترجمات إلى العبرية ح – مقالات عبرية أصلية مبنية على الأصول العربية .

نجد في الفئة الأولى نسخاً عن المجسطي: ملخص لمؤلف مجهول للمجسطي، وإصلاح المحسطي جابر بن أفلح ، وكتاب التبصرة في علم الهيئة للخراقي ، والزيج الجديد لابن الشاطر .

ونجد في انفثة الثانية ترجمتين للمجسطي ، وكتاب البطروجي عن مبادىء علم الفلك : تم كتاب نور العالم ليوسف ب تحمياس ، والزيج ليوسف بن الوقار ، والزيح للملك ألفونسو، والزيج أو الغ يلق .

ونجد في الفئة الثالثة كتاب الزيج لابراهيم بارحبيا المستند على كتاب البدتي ثم كتاب الربج الشعبي المسمى بالأجنحة الستة لايمانوبل بونفيس من تاراسكون وقد ترجم هذا العمل فيما بعد إلى اللاتينية واليونانية البيزنطية ، ويوجد أيضاً في الفئة الثالثة كتاب الزيج مع لوائح لليوي بن جيرسون ، وهذا العمل يستند إلى نسخ جديدة وهو مأخوذ عن ارصاده الخاصة .

وثحة عملان لهما أهمية خاصة وهما ؛

 ١ ــ نص عربي مجهول مكتوب بالحرف العبري ، ومأخود عن النص اللاتيني لكاميانوس من نوڤارا (في ايطاليا) ، وهو مثال فريد للنصوص الفلكية المترجمة من اللاتينية إلى العربية .

 اللوائح الفارسية لشلومو بن الياهو من سالونيكي وهي مترجمة من اليونانية إلى العبرية ومستندة في الأساس إلى الزيج السنجري للخازني ، والزيج العلائي للفهاد.

السيمياء الاسلامية وولادة الكيمياء

سيد حسين نصر

ان السيمياء هي في آن واحد علم الكون ، وعلم الروح المقدس ، وعلم المواد ، وعلم ملواد ، وعلم ملواد ، وعلم متم لبعض فروع الطب التقليدي . وهي ليست الكيمياء الأولية بالرغم من انها تعالج المواد الطبيعية من وجهة نظر معينة ولا هي أيصاً أصل الطريقة العلمية الحديثة ، بالرعم من أنها اهتمت بأدى معاني التجربة والتجربب ، ذاك أن التجربة الداخلية وحدها هي التي تؤدي الى اليقين وتظل التجربة الحارجية ظلاً باهتاً لها . ويهدف السيميائي التقليدي الى تحويل الطبيعة بحيث يعيدها الى كمالها الأصلي الذي هو من صلب الواقع .

استطاعت السيمياء الاسلامية ان تحتفظ عبر القرون بصفة روحية متكاملة متحدة مع الصوفية ومدارس أخرى فمية ، إضافة الى أنه في الاسلام زُرعت أول بذور علم الكيمياء ، بالرغم من أن النظرة الرمزية للطبيعة السائدة لم تسمح إطلاقاً للنظرة الدنيوية نحو المواد المادية بان شهيمت .

ان ظهور الكيمياء مرتبط بولادة مدرسة فلسفية على هامش الحياة الفكرية الإسلامية وهي متجهة نحو تغيير في وجهة النظر الفكرية التي تتماثل مباشرة مع الفرق الشاسع بين وجهات نظر السيمياء والكيمياء . واكثر من ذلك فإن أحداث هذه المدرسة الفلسفية الهامشية وولادة الكيمياء تعود الى فترة مبكرة من التاريخ الاسلامي وتتملق بائنين من أشهر الشخصيات في العلوم الاسلامية وهما : جابر بن حيان المسمى باللاتينية جبر (Geber) والذي توفي في القرن الناسع الميلادي . ومحمد بن زكريا الرازي المسمى باللاتينية رازس (Rhazes) والمتوفي في القرن الرابع الهجري الموافق للعاشر الميلادي .

لم تعرف حوليات السيمياء الاسلامية شخصين ألمع من هدين الرجبين اللذين أظهران عبرية متعددة الجوانب ، كل منهما كان سيداً شهيراً في السيمياء وتعتقد الأجيال التالية في عالم السيمياء الغربي والاسلامي أن كليهما انتميا الى ذات المدرسة . لكن دراسة حول كتابات كلا الرجلين تظهر بوضوح أنه بالرغم من أن الرازي استخدم لغة السيمياء الحابرية لكنه كان في الواقع لا يعالج السيمياء بل الكيمياء . . . نستطيع أن نقول أن الرازي حول

السيمياء الى كيمياء بالرغم من بقاء السيمياء من بعده زماً طويلا واستمرار العالم الاسلامي. برحايتها .

إتبع الرازي بدقة مصطلحات السيمياء الجابرية ولم يتبن من جابر التسميات الفنية محسب بل تبنى أيضاً عناوين الكتب ، إن عدداً كبيراً من مؤلفات الرازي في هذا المجال تحمل ذات العناوين التي استعملها جابر بينما البعض منها ليس الا تعديلات لأسماء اعمال تعود الى مجموعة جابر الكاملة .

ومن ثم يمكن السؤال لماذا سميت اعمال الرازي بأول كتب الكيمياء في تاريخ العوم. لدينا عدة أعمال في السيمياء للراري كالمدخل التعليمي الذي خدم كأساس للقسم عن السيمياء في مفاتيح العسلوم . والأكثر أهمية هو كتساب سر الأسرار المعروف في العالم الغربي و Liber Secretorum Bubacaris وفي كل هذه الأعمال هنالك وصف وتصنيف للمواد المعدنية والعمليات الكيماوية والآلات وغيرها... بحيث يُستطاع ترجمتها بسهولة الى اللغة الكيميائية الحديثة. ليس هناك إهتمام بالوجه الرمزي للسيمياء في مناقشة المعادن وتحولاتها كرموز لتحولات الروح . فالتطابق بين العالم الطبيعي والعسالم الروحاني المعادن وتحولاتها كرموز لتحولات الروح . فالتطابق بين العالم الطبيعي والعسالم الروحاني المعادن أساس النظرية العامة للسيمياء قد اختمى معظمها وتركنا مع علم يعالج المواد الطبيعية التي تؤخد بعين الاعتبار من حيث حقيقتها الحارجية فقط علماً بأن لغة السيمياء ويعض أفكارها ما زالت ياقة .

يجب أن نفتش عن سبب خروج الرازي عن النظرة السيميائية في موقفه الفدسفي الخاص كما أنه نعام في الكثير من المراجع اللاحقة من ضمنها البيروني الذي كان يؤيده علمياً ، نعلم بأن الرازي كتب العديد مسن الاعمال ضد الدين النبوي وحتى أنه رفض النبوة على هذا الشكل بمفهومها العام وعندما تحلل المواقف الدينية والفلسفية المقتضية في موقف الرازي نجد السبب واضحاً في تحويله للسيمياء اجابريسة الى الكيمياء وفقاً للمفهوم الاسلامي المعد لفئة معينة فقط ان علوم الطبيعة مرتبطة بعلم الوحي. فالوحي له مظهر ظاهر ومطهر باطن وعملية التحقيق الروحي تفتضي البداية من الطاهر والوصول في النهاية الى الباطن. فهذه العماية تسمى بالتأويل، وإذا طبقنا هذا التأويل عنى الطبيعة فإنه يعين إختراق ظواهر الطبيعة لمكشف عن كنه الأشياء وهذا يعيى التحويل من الحقيقة الى الرمز لرؤية الطبيعة ، ليست الرؤية الى ترمز لرؤية الطبيعة ،

فالسيمياء هي تماماً علم "كهذا مبني على اساس الظواهر الطبيعية ونصورة خاصة مملكة المعادن وليس كحفائق بحد ذاتها بل كرموز لمستوى أرفع للحياة .

فجابر بينما كان لو يهتم أيضاً بالحوادث الطبيعية لم يفصل ابداً الحقائق في عالم الطبيعة من محتواها الرمزي الروحي وميرانه الشهير لم يكن محتواها لقياس مقادير دراسة الطبيعة في مفهومها الحديث بل « لقياس ميول عالم الروح » ان اسماكه بالرموز الأبجدية والرقمية في دراسة الظواهر الطبيعية كتحديد عالم الروح برموز السيمياء بصورة خاصة كلها تشير الى أن جابر كان يطبق عملية التأويل على الطبيعة لكي يفهم معناها الباطن .

فالرازي عند رفضه للتنبؤ وعملية التأويل التي تعتمد عليه يرفض أيضاً تطبيق هذه الطريقة على دراسة الطبيعة ، وبهذا حوّل السيمياء الجائرية الى كيمياء ، هذا لا يعني أنه توقف عن استعمال المصطلحات أو الافكار السيميائية ولكن من وجهة نظره لم يكن هناك بعد أي ميزان لقياس ميول عالم الروح أو أي رموز تصلح كجسر بين عالم الظواهر وعالم الأشياء حيث مفاهيمها كما هي في ذات نفسها .

تمت دراسة حقائق الطبيعة كما هي من قبل ولكن كحقائق وليست كرموز وتمت دراسة السيمياء ليس كدراسة السيمياء الحقيقية بل بدراسة كيمياء بدائية فلذلك ارتبط موقف الرازي الديني والفلسفي مباشرة بوجهات نظره العلمية وكان مسؤولاً عن هذا التحول . في الواقع ان حالته تظهر احدى أوضح المثل حيث الأمور الفلسفية والدبية لعت دوراً في الكثير من التطورات الهامة في العلوم وتاريخ العلوم بصورة عامة، وهي تظهر العلاقة الوثيقة بين وجهة نظر المرء نحو علوم الطبيعة ورؤيته عن الحقيقة كما هو في حدداته .

لكن الحضارة الاسلامية رفضت الآراء الفلسعية للرازي وأمثاله وظلت مخلصة لروحها الشعبية الخاصة وعبثها الذي اثقلتها به الأيدي الإلهية أي حمل رسالة القرآن للإنسانية حتى نهاية العالم. سمحت هذه الحقيقة للإسلام بأن يحتفظ الى يومنا هذا بالرغم من كل تغيرات الزمن يمعرفة ومزاولة السيمياء اللماخلية التي تجعل من الممكن القيام برعابة الدهب الذي هو هدف الحياة الإنسانية والذي يسمح للإنسان بأن يلعب الدور المرسوم له وأن يعمل كالجسر الواصل بين السماء والأرض وكالعين التي من خلاها يرى الله خلقه وكالمنفذ الذي تعبر الرحمة السماوية من خلاله الى الارض فتخصبها.

مثال حاسم على تأثير مباحث علم النفس في العلوم والحضارة الإسلامية : بعض العلاقات ما بين علم النفس عند إن سينا وفروع أخرى لفكره والتعالم الإسلامية ووبرت هول

كانت نظرية علم النفس، هي محور الإهتمام في العالم الاسلامي في العصور الوسطى وكان سينا الشخصية الرئيسية في تاريخ الفكر الاسلامي . ومن ثم نستطيع القول ان علم النفس كان مركز اهتمام الى سينا و « واسطة العقد » في أعماله حتى أن نظرياته نالث أهمية عظيمة في تاريخ علم النفس . وفي الحقيقة لم يكن لإن سينا منافس في العصور الوسطى الإسلامية والغربية (وأضف قولي : وحتى في عصر النهضة) لم يكن له معافس سوى ان رشد (١١٢٦ – ١١٩٨ م) . وأعتقد ان كنت على حق ، أن علم النفس عند ان سينا أخذ معان ودلالات أعد في تاريخ المكر الإسلامي . لأن النظام الفلسفي الذي أبدعه كان نقطة تحولً كلي في تاريخ الفلسفة والعلوم والتحقيق النظري – وحتى في التحقيق الديني – في العالم الاسلامي اد دار معظم تفكير ان سينا حول تحليل العواقب النصية . لذلك يجب أساساً وقبل كل شيء فهم تعاليم ان سينا ومذاهبه النفسية فهماً صحيحاً من أجل تحليل تاريخ الفكر الإسلامية .

وكان كتاب الشفاء لإن سيا أطول عرض نظامي متكامل للفلسفة (وأعني بالفلسفة الفسفة الإسلامية فقط للمفهوم الملي وضعه اليونان) في الفترة الكلاسيكية . ولكن بالرغم فمن من ذلك الممكن أن نقول (حسب وجهة نظر بعض الباحثير المعصرين) أن كتاب الشفاء والأعمال الفلسفية الأخرى لإن سينا احتوت على تحول جوهري في تقاليد الفلسفة الإسلامية والشاهد على ذلك النهم التي صبتها إبن رشد على إلى سينا لتخليه عن المبادىء الأرسطوطليسية البحتة والفلسفة الروحية البحتة التي إستطاع بصير الدين الطوسي (١٧٠١) المهادىء الأرسطوطليسية المبحتة والفلسفة الروحية المرحة التي إستطاع بصير الدين الطوسي (١٧٠١)

إن السياق الفسفي الذي ضم في القرنين التاسع والعاشر المنطق والرياضيات والفلسفة الطبيعية والدوم الطبيعية على المبدأ الرياضي وعلم ما وراء الطبيعة وعلم الأخلاق والسياسة إن هذا السياق إحتفظ بشيء من نظرية أرسطو الأصلية البحث والتطور التصاعدي للمعرفة ولكن فيما بعد أصح ذلك دراسة تمهيدية بحتة ولو أنها أساسية لنوع من المعرفة

الإستشراقية المماشرة وعلى وجهه الإفتراض أكثر قيمة وأصبحت في آخر الأمر تفسر في المدارس الإيرانية الحديثة بالمعرفة الروحية بالرغم من كوفي لا أستطيع أن أكشف عن مذهب باطني حقيقي لا في أعمال إبن سينا – وبالتأكيد – ولا في الفصل المستشهد منه مراراً عن مقامات العارفين في كتاب الإشارات مع ذلك كانت المقومات الإشراقية باررة بوضوح وكانت الأرض ممهدة تماماً للتطور الروحي بفضل فلسعة إبن سينا .

وأنا متأكد أن القوة المحركة وراء هذا التحول للفلسفة مستمدة من البحث الفسفي عسن الروح أو بالأحرى عن المعاني المتضحة التي تعطيها مبادىء عدم النفس في كل عالات التحقيق الفلسفي تقريباً. إن ذات النائح النفسية الأساسية ذاتها أدركها في المهاية المتكلمون (علماء الدين الأسلامي الخين يحثون وفق البراهين العقلية) كما كابوا يسمون بعض الصوفيين دوي المبول الفكرية وبالفعل كل المسلمين المثقفين في ذلك المصر إن المهمة الأساسية في تطور الفكر الإسلامي الكلاسيكي كانت توسيع السمط النظري بلحضارة الدين المقات المتصادة للمفكرين المسمين كالمقضاة العصميين ، وعلماء الدين (المتكلمون) ما تقع بين المقات المتصادة للمفكرين المسمين كالمقضاة العصميين ، وعلماء الدين (المتكلمون) والفلاسفة والصوفيين والإسماعيليين وإن لهذه المناقشة تأثير توجيهي عظيم على الحضارة المفاسفة والصوفيين والإسماعيليين وإن لهذه المناقشة تأثير توجيهي عظيم على الحضارة ومشاكل المعرفة الصحيحة والإيمان الحق ووثيقة الإرتباط بهعدا الإهتمام الرئيسي ورنما ومشاكل المعرفة المصحيحة والإيمان الحق ووثيقة الإرتباط بهعدا الإهتمام الرئيسي ورنما الأساسي الأكبر للمفكرين المسلمين .

(شم يتابع المؤلف في توضيح طريقة إبن سينا ونتائجه بالفحص المصل بدقة لما لحة لكنا المشكلة الأساس المنفصلتين ، مشكلة عم الأجنة ومشكلة الأساس التجريبي للمعرفة . إن حل المشكلة الأولى هو تعديل للحل الذي قدمه أرسطو وأما حله للثانية فهو حل يتعار صحدريا مع حل أرسطو .وإن عرض هذه الأمور يأخل معظم البحث وهو مدروس بدقة وفنية إلى درجة عالية غير ملخص هنا . فرجو من قارئنا المهتم أن يعود إلى الأصل الإنكليزي. أما الإستنتاجات فهي فيما يبي .

لا تستطيع أن تذكر ذكاء أو على الأقل دقة التأليف الفلسفي الذي أنجزه ابن سينا . لقد قدم حلولا للمسائل النفسية الأساسية التي كانت تواجهه وحتى إذ أنه ترك مجموعة من الأسئلة الثانوية في علم الوجود دون جواب . بإستخداهه لطريقة عرض غير مباشرة ممتازة قدم إبن سينا تفسيراً لا يتوافق مع تعاليم أرسطو عن إكتساب المعرفة وها التفسير ترك إبن سينا في تمام الموقف الإشراقي المعتدل الذي أراده . لقد كان تحليل التجربة في كتاب البرهان خطوة حاسمة في تثبيت مبادئه النطرية للمعرفة . من الممكن ان تكون التجربة ذات قائدة ولكن كان لها دور محدود جداً ولم يكن هناك مثال حيث لا يستطيع تجنبها في النهاية . التجربة تعود إلى القدرة الاستناجية والمعرفة إلى الفكر ، والأساس الفعال للتفكير المحدود عدود العلاقة التالية للعلوم اليونانية وأنصارها مع أتباع المطرق حسماً ، ولقد ناقشت في تحديد العلاقة التالية للعلوم اليونانية وأنصارها مع أتباع المطرق الأخرى للمعرفة في الأسلام ،

لقد نست موقف إن سيما من المعرفة التجريبية إلى إعتماد المسلمين الحوهري في الحلاص الشخصي . وإلى هذا أيضاً نست تفسير نفخ الروح في الجنين الأنساني المعروض في كتاب الحيوان . أخيراً وبما أن الفردوس كان سيقدم التفكير الحالد كأعظم مكافأة كان من هذا المضمار ولادة مشاكل علم الوجود الرئيسية . لقد قام إن سينا بخطوات محتلفة ليوفق ما بين التفكير الواقعي مع التمييز الروحي ولكمه لم ينجح نجاحاً حقيقياً .

إن المناقشات في هذا البحث يجب أن تكون قد وضحت العلاقة الكبيرة بين فلسفة ابن سينا وعلم النفس عنده والإعتماد الحاسم لنظامه على تطوير نظرية الروح العامة المستقيمة علاوة على ذلك إن العالم الفكري الإسلامي في القرن الناسع المتقدم والعاشر وبداية القرن الحادي عشر يصبح القول أن نسبة عالية من انتثاج الرئيسية كمنت في نظريات علم النفس أو المأخوذة عن مبادئها مباشرة وإن هذا إصرار يحب أن تزود له قائمتين الأولى حالة ظاهرية كافية . لقد قدمت في وبدون إثبات تحليل لتطور الحضارة الفكرية الإسلامية حيث العملية الأساسية هي حوار بين فئات متعددة للمفكرين المسلمين وإحداها ضمت الفلاسفة وآخرين يجدون العلوم اليونائية . ويعتقد هنا أنها كانت مناقشة دينية في الأساس وكان السؤال الذي يشكل الأساس هو نوع العلم الذي كان يقبل بأنه صحيح وكان بذلك يؤمن الفهم الصحيح لدين . إن الفحص الكامل للتجربة والأمور المتعلقة بها فيما سبق كان

مقصوداً من ناحية لتوضيح هذه الصورة للمناقشة العامة ولعرض مثال جديد بالذكر لما استنجت أنه كان متعلقاً به . وإذا كان هذا التفسير صور الوضع التاريخي بشكل دقيق عندئد يصح الفول التاني : أن من خلال هذا الحوار مارست نظرية علم النفس قوة رئيسية على التشكيل النهائي للحضارة الفكرية الإسلامية .

لا يشت أحد في أن ابن سينا كان شخصية رئيسية في تاريخ الفكر الاسلامي . والمهمة الحقيقية هي معرفة بأي وسيلة إستطاعت فلسفةا سينا تغيير مسلك العلوم اليونانية في العالم الإسلامي وبذلك غيرت تطور حضارة الإسلام ككل . وهنا جواب غير لهائي ممكن بعد لتحويل الفلسفة بحد ذاتها الى عملية مباشرة نسباً وأمر يعتمد في الاساس على الإجابات المبدئية وعندما أصبح تركيز الفلسفة على علوم ما وراء الطبيع والعلوم الرياضية أقل بكثير . ولكن فكرة ابن سينا كأول مثال لهذه الفلسفة كانت قد إستطاعت أن تلمب دوراً رئيسياً إلى جانب الفروع القديمة في الحوار الديبي العام التي إفترضتها . وإذا كان الوصف صحيحاً حتى الآن نستطيع أن نؤكد أن علم النفس النظري لإبن سينا مارس تأثيراً حاسماً على تاريخ العلوم اليونانية في الإسلام عامة . وهذا الإستناج هو ما كان قلقاً على إليابي بلغ بالمكن إعطاء الإثبات الكان بلغ بالمكن إعطاء الإثبات الكان بلغ عامد أن قلط ذات الأهمية الكبرى لنتائجه العامة .

ولأضف ملاحظة نهائية : إذا كأن هذا التخميل التاريخي تخميناً دقيقاً كان الفلسفة وكل العلوم اليونانية الصدارة في مركز الحضارة الإسلامية بحد ذاتها وليس على أطرافها كما كان يعتقد غالباً. بالفعل إن الفاسفة وأخواتها الفروع الأخرى ستحتاج أن تعتبرها تطوراً في طرق وعمليات مألوفة في معظم المجالات والمساعي العكرية في العصور الوسطى الإسلامية وتمييزاً في الحضارة الإسلامية .

مقالمه قصيرة واغلانات

الاشارة الى مخطوطة أخرى لكتاب المنصوري للوازي

غادة كرمي

أحد أشهر كتب الراري (أي بكر محمد بن ركريا الراري) هو كتابه الشامل عن الطب السذي أهداه الى الامير الساماني أبسي صالح المنصور أي اسحاق والذي عرف فيما بعد بكتاب المنصوري. وكان عملا مشهورا في العالم اللاتيني الغربي خلال العصور الوسطى وترجم لى العربية والمونانية واللاتينية وقد ترجمه الى اللاتينية جيرارد أوف كريمون في عام ١٩٨٦ وأعيدت طباعته مرات عديدة فيما بعد. وهناك الكثير من المخطوطات اللاتينية الاخرى الموجودة عن هذا الكتاب، وهي دليل آخر على شعبية هذا الكتاب، وهي دليل آخر والمقالة الناسعة أو الكتاب في الغرب. أن كتاب المصوري ينقسم الى أمحاث أو مقالات والمقالة الناسعة أو الكتاب لمنصوري التاسع الذي يبحث في الامراض من الرأس الى الكعب كانت وبصورة خاصة شائعة الاستعمال في القرن الخامس عشر وعلى عليها في القرن الخامس عشر والسادس عشر. أشهر هذه التعليقات كانت الصياغة الحديدة الأندرياس فيزاليوس التي تشرت في عام ١٩٣٧ .

ولقد كان كتاب المنصوري شائعاً وهاما في الشرق العرب . لقد قال أبو العباس المجوسي مؤلف الموسوعة العلمية : كامل الصناعة في القرن العاشر قال في مقدمته أن الرازي قد تجاور كل الاخربن بتفوق في كتابه هذا . قاليوم لا توجد أقل من ٤٧ مخطوطة عن هذا العمل الموجود وهي مشتتة موزعة على المكتبات الشرقية والغربية المختافة . فالعدد الكبير والامتداد الزمي الواسع للمحطوطات الباقية هو دليل آخر على شعبية هذا الكتاب ومع ذلك لا يوجد تحقيق باللغة العربية لهذا العمل في العصر الحديث ما عدا تحقيق رايسكي بالعربية واللاتينية في عام ١٩٧٦. ان المقالة الاولى حققت وترجمت الى الفرنسية من دو كونيج في مطلم هذا القرن .

ان كتاب المنصوري متوسط الحجم (فطول المخطوطة يتراوح عند ال ٢٢٠ ورقة) وهو يعالج كل المواضيع الكبرى دات الاهمية الطبية كما تبير مواضيع مقالاته العشر :

> شكل الاعضاء ومظهرها معرقة مزاجات الحسم والاخلاط الراجمة فيها

مقانة قصيرة 118

وظائف الطعام والدواء
الاحتفاظ بالصحة
الاحتفاظ بالصحة
المستحضرات التجميلية والامراض الخارجية
ادارة المسافر
تجبير العظام والجروح والقروح (التقرحات)
السموم ولسع الحشرات
الأمراض من الرأس إلى الكعب
الحميات ، المغليات ، النوبات ، البول والنبض

ومن ضمن المؤلفات الطبية كانت مخطوطة كتاب المنصوري فالنسجة الوحيدة لهذا الكتاب والتي عرفنا بوجودها في حلب ه كانت النسخة المدكورة في قائمة الاب بول سبات والمؤلفة من ثلاثة علمدات للمخطوطات الموجودة في المجموعات الحاصة في حلب الهيد رودولف بوخي . ان التلوين في كتاب سبات مختصر على نحو مميز ولا يعطي اي وصف للمخطوطة ان التحقيق الدقيق أثبت ان مخطوطة القمصل الحولاندي هي ذاتها المهداة الى معهد الراث لقد انتقلت من ملكيته الى ملكية آخرين ومن ثم الى آخر مشتري وهو الذي اهداها الى معهد الراث . ومع المخطوطات جاءت أيضاً قائمة مكتوبة بحط المد فيها عناوين الكتب المخطوطة وأسماء مؤلفها ووصف قصير كل هذا موجود في تمارين صغير ويقال ان يول سبات كتبه في الثلاثيبيات من هذه القون كتحضير لقائمة أشمل لم يقم بها ابداً . وكتاب المنصوري يؤرخ نسخة بالقرن الثالث عشر ميلادي ، ولا يعطي اي شرح آخر ، ان وجود هذه المخطوطة بالرغم من آبا ذكرت في قائمته لايشار الى وجوده في اي من كتب بروكان او سيزكين او اولمان .

المحطوطة

(الرقم : الطاكي ١)

الغلاف الجلدي بهت لونه وتعرض للتلف لقد انفصل التجليد ومعظم الاوراق منفصلة ولكن ما عدا ذلك فالمخطوطة محفوظة بصورة جيدة . صفحات عليها بقع تقريبا بلون ملاحظات على الهامش . الصفحة الاولى تحتوي خط المالك وأربع تدوينات بأيد مختلفة احداها وهي تبدو أحدث في النص تقرأ كما يلى : ۵ كتاب المنصوري في حفظ الصحة ومعالحة الامراض لمن يحضره الطبيب تأليف
 الشيخ الحكيم أني بكر محمد بن زكريا الرازي . ٥

١٨٧ صفحة كاملة . مرقمة باخير تنتهي عند الصفحة ٣٦٤

فر۱۸ × ۱۹٫۵ سم ۲۲ سطر

الحط نسخي وأصح مشكل جزئيا . العناوين بالحبر الاحمر - لا يوجد اسم الناسخ . ندون تاريخ ربما القرن السابع / الثالث عشر (كما عند سباث)

وهي تبدأ :

و بسم الله الرحمن الرحيم ،

بسم ألله الرحمن الرحيم رُب يسر وأعن برحمتك مجدا كتاب الله « محمد بن زكريا » للمنصور بن اسحاق اسمعيل بن احمد فقال أي جامع للامير أطال الله بقاه جملا وجوامعاً و نكتاً وعيونا من صناعة الطب ومتخذ في ذلك الاختصار والإيجاز وذاكر ما لا يحدث ... و تنتهى :

فَلْيُوخَدُ لَهُم رَطِلَ مِن وَزَنَ دَرَهُم مَصَطَكَي وَدَرَهُم سَبَلَ قَصِيرٍ فِي خَرَقَةَ وَتَلْقَى عَند الطبخ فيه ان شاء الله تعالى وادا اتين على جميع المقالات والقصول المذكورة في صدر هذا الكتاب فقد كُمُل كتابنا هذا والله المعين والموافق للصواب وهو حسبا ونعم الوكيل ولا حول ولا قوة الا بالله العلى المظيم ثم الكتاب والجمد لله حق حمده وصلو الله على سيدنا محمد وآله وصحبه وسلم تسليما .

باطع انه من المفيد دائما ان لكشف عن مكان مخطوطة علمية عربية ولكنه من الاهمية الخاصة في هذه الحاة ترجع الى سببين :

اولا : لأنه لا توجد طبعة حديثة لكتاب المنصوري . ثانيا أن هذا الكتاب ذو أهمية عظيمة لتاريخ الطب العربي وتاريخ العلم في العصور الوسطى . بالاضافة الى ذلك ان هذه المخطوطة ذات قيمة خاصة لاجا كاملة وبحالة جيدة ويبلو الها متقدمة ، ان الكثير من المخطوطات (المتبقية) لكتاب المنصوري ليست كاملة وفي بعض الاحيان تفتقد الى نصف او ثاث النص الاصلى .

من حسن الحظ تحلت الملكية الخاصة عن هده المخطوطة وأصبحت متوفرة لاستعمال الباحثين

برعاية السيد الرئيس حافظ الاسد انعقدت في جامعة حلب الندوة العالمية الثانية لتاريخ العلوم عند العرب

عت رهاية السيد الرئيس - حافظ الأسد - رئيس الجمهورية احتفل يافتتاح الندوة العالمية الثانية لتاريخ العلوم عند العرب ، وقد ناقشت لندوة وعلى مدى خمسة ايام عشرات الأبحاث الأصبله التي قدمها حوالي ١٢٧ - عالماً وباحثاً شاركوا في الندوة كما نظمت الندوة حلقة علمية حول تاريخ الجبر العربي واخرى حول انتقال العلم العربي إلى العرب اللائيي بالإضافة الى عدد من المعارض هي : معرض الأدوات الفلكية والصناعات الحربية ، معرض مسح المنشآت الماثية في القطر ، معرض النباتات والمواد الطبية ، معرض منشورات معهد التراث العلمي العربي ومطبوعات جامعة حلب ، معرض لبعض القطع الأثرية التي يعمل معهد التراث على احداثه . كما تم خلال تشكل ثواة متحف العمم والتكنولوجيا الذي يعمل معهد الراث على احداثه . كما تم خلال العقاد الندوة عرض فيلم سينمائي عن مدينة (ايبلا) وفيلم آخر عن ابن النفيس ، وبعض الأعلام الأخرى عن العلم في العالم الإسلامي ، ونظمت الجامعة لمضيوف الندوة برناجاً تضمن اطلاعهم على الثروة الأثرية العربقة للقطر .

وسيصدر معهد التراث العدمي العربي عدداً خاصاً من رسالته يخصص لدندوة العالمية الثانية لتاريخ العلوم عند العربيد .

فوز الدكتور فؤاد سزكين يجائزة الملك فيصل للدراسات الاسلامية



قاز الاستاذ الدكتور فؤاد سرّكين في جامعة فرانكمورث في المانيا الاتجادية ومرشح معهد النراث العلمي العربي بجائزة الملك فبصل لدر اسات الاسلامية بعام ١٩٧٩ عن مؤلفه ٥ تاريخ التراث العربي ٥ .

وتجلس الاشارة لبيان قيمة هذا المؤلف المشرو باللغة الالمانية ان ندكرما قاله احد المستشرقين في مؤتمر عقد بمدينة وورز برغ في المانيا الاحادية عام ١٩٦٨ عاداكان كتاب بروكلمال قد حول الانطار ليه سنوات طويعة فان كتاب ٥ تاريح النراث العربي ٤ سوف يكون كتاب القرن العشرين في الثقافة العربية وتصنيف التراث العربي الضخم ٨.

ويعلق الدكتور فهمي ابو الفضل على المؤلف فيقول « ان هذا السفر لبس سفراً للعلوم فقط ، ولكنه سفر لعمل متواصل ومحهود ضخم و ادا قلما ان فرداً واحداً قد قام بعمله ، فربما تطرق الشك الى نفوسنا ، لأنه يحب ان يكون عملاً جماعياً ، ولكن الواقع غير دلك فهو عمل فردي ، بدل صاحبه اكثر من عشر بن عاماً في جمعه وتسيقه وترتبه حتى ظهر في الصورة التي بين ايادينا ، »

وُلُد الدكتور فؤاد سركين في مدينة استنبول عام ١٩٢٤ وحصل على دكتوراء في العلوم الاسلامية والدراسات الايرانية . ومارس التدريس في جامعة استنبول سنوات عديدة عكف خلالها على الاطلاع على كنور الراث الاسلامي . انتقل عام ١٩٦٠ الى المانيا الغربية حيث تولى التدريس بمعهد الامات السامية في جامعة ماربورغ لمدة سنتين ثم انتسب الى معهد تاريخ العلوم الطبعية في جامعة فرانكمورت كاستاذ زائر . ثم اصح استاذاً بكل احقوق المعترف بها للأسائدة الألمان رغم احتفاطه بجنسيته الدكية الى اليوم .

ومن اهم مؤلفات الدكتور سزكين بالاضافة الى موسوعته ؛ تاريخ النراث العربي » ، كتاب ، تاريخ البراخ الله الله المركة » (باللغة النركية) عام ١٩٤٨ و ، مجاز الفرآن » لأي عبيدة معسر بن المثنى (مجلدان) نشر بالقاهرة عام ١٩٦٣ و » دراسات حول مصادر الجامع الصحيح البخاري » (باللغة النركية) طبع باستنبول عام ١٩٥٣ .

هدا وقد منحت الحائز ة للدكتور سزكير في احتمال رسمي كنير اقيم في الرياس في السابع والعشرين من شباط ١٩٧٩ . وقد دعي لحضور هدا الاحتمال الاستاذ الدكتور أحمد يوسف الحسن رئيس جامعة حلب ومدير معهد التراث العلمي العربي .

وتنكون الجائزة من شهادة تحمل اسم الفائز وملخصاً للعمل الذي أهله ها ومن ميدالية ذهبية ثمينة ومبلغ لنقدي قدره ٢٠٠ ألف ريال سعودي .



حفسلة تكريم الأستاذ الدكتور محمد يعيى الهاشمي

درج معهد التراث العلمي العرب محامعة حلب على تكريم العلماء والباحثين وحصوصاً العرب معهم . فاقام المعهد حفلة لتأون الاستاد الدكتور احمد شوكت الشطي اثناء الندوة العالمية الثانية لتاريح العلوم عمد العرب واصدر عدداً حاماً من نشراته جمع فيه الكلمات التي ألقيت خلال تلك الحملة وكذلك اقام معهد التراث العلمي للعرب والجمعية السورية لتاريح العلوم ي جامعة حلب مساء الحميس ٧ – ٦ – ١٩٧٩ حملاً تكريماً للاستاد الدكتور عمد يحيى الهاشمي احد علماء حلب المعروفين تقديراً لحهوده واعماله ومحوثه العلمية ومساهمته الفعالة في المؤتمرات الدولية العديدة وتأليفه الكثير من الكتب والفاء المحاصرات وغيردك من الكتب والفاء المحاصرات

وقد حضر الاحتفال عدد كبير من رحال الفكر والثقافة واعصاء الحمعية اسورية لتاريخ لأملوم وافراد اسرة الدكتور الهاشمي .

ولد في حلب سنة ١٩٠٤ من عائلة حلبية عريقة بالمصل والعدم .

- درس في ألمانيا ونال صها شهادة في الكيمياء والفلسفة ، وحصل على الدكتوراه في الكيمياء بتقديمه
 دراسة عن لاكتاب الاحجار لليبروني ٤ .
 - درس في مدارس حلب الثانوية ومن ثم في جامعتها انى أن أحيل الى التقاعد .
 - كانت حياته نصالاً مستمراً في سبيل احباء علوم العرب و الاسلام و نعريف النرب بها .
- كتب الكثير من المقالات ، واشترك في كل مؤتمرات تاريح العلوم ، ونشر العديد من الكتب .
 منها كتاب الامام جعف الصادق ، ملهم الكيمياء في طبعيته الاولى والثانية .
- ومن أمرز أعماله تأسيسه في حلب سنة ١٩٥٧ ، جمعية الإبحاث العلمية ، التي كان ها أثر كبير في سورية ولا سيما في البلاد الغربية بفضل منشور إنها وابحائها .

مراجعات اليكييب

مراجعة « كتاب الحيل » لبني موسى بن شاكر

الترجمة الانكليزية مع التعليق والشرح دونالد هيسل شركة رايدل المشرح دولنده ١٩٧٩

عاش بنو موسى في القرن الثالث الهجري / الناسع الميلادي عندما كانت الحضارة العربية الاسلامية في أوجها. وقد لعب الأخوة الثلاثة محمد واحمد احسن بناء موسى بن شاكر في عهد المأمون ومن تلاه من الحلفاء دوراً بارزاً في تطوير العلوم وبصورة خاصة العلوم الرياضية والفلكية والميكانيكية من خلال مؤلفاتهم ومن خلال تأثيرهم الفعال على حركة الترجمة من اليونانية الى العربية . ورغم كثرة ما الفه بنو مسوسى الا ان اهم ما كانوا يتميزون به هو كتاب الحيل . ولم يرد ذكر لبني موسى الا وكان كتاب الحيل ابرز ما يوصفون به .

وفي مفاتيح العلوم (٢) نجد ان الخواررمي يعتبر علم الحيل واحداً من العموم الثمانية الرئيسية ثم انه يقسم هذا العلم الى فرعين : الأول جر الأثقال بالقوة اليسيرة والثاني حيل حركات الماء وصنعة الأواني العجيبة وما يتصل بها من صنعة الآلات المتحركة بذاتها . وفي التقسيمات المتأخرة لتفرعات العلوم اصبح علم الحيل احد فروع علم الهندسة ليس بمعناه الرياضي (geometry) بل بمعناه التكنولوجي (engineering).

وعلى اي حال وبغض النظر عن تقسيمات العلوم وتباينها من عصر الى عصر فان علم الحيل يدخل في نطاق الهندسة الميكانيكية اذ أنه يبحث في الآلات والادوات والتجهيزات الميكانيكية والهيدرولميكية .

^{*} بالنسة للاسماء الأجنبية ؛ ارجع الى النسخة الانكليزية

٤ - محمد بن أحمد بن يوسف الحوارزي . مثاتيج العلوم (القاهرة، ادارة العباهة المديرية، ١٩٤٧هـ)، ص ١٩٦
 ٢ - أحمد الشقشمي . صبح الأعشى (القاهرة ، المطبعة الأميرية ١٩١٣)، ج. ١ ص ٤٧٦ .

والى عهد قريب اشتهر كتابان فقط في علم الحيل عند العرب احدهما كتاب الحيل لبني موسى والثافي كتاب الجامع بين العلم والعمل النافع في صناعة الحيل لمديع الزمان بن الرزاز الجزري (٢٠). ثم اضيف اليهما كتاب ثالث هو كتاب الطرق السنية في الآلات الروحانية لتقي الدين بن معروف الراصد الدمشقي (٤٠). وبذلك اصحت هذه الكتب الثلاثة التي تعود الى عهود متباعدة : كتاب بني موسى في القرن الثالث الهجري / التاسع الميلادي . وكتاب تقي الدير وكتاب الجزري في القرن السادس الهجري / الثاني عشر الميلادي ، وكتاب تقي الدير في القرن السادس عشر الميلادي تشكل حلقات اساسية في سلسلة من نقاليد الهندسة الميكانيكية في الحضارة العربية الاسلامية . وربما اكتملت حنقات هذه السلسلة باكتشاف ونشر كتب اخرى في هذا المجال (٠٠) .

تبدأ اذن التقاليد العربية الاسلامية في علم الحيل بكتاب بني موسى الذي اكتسب شهرة كبيرة في المراجع العربية . ومن حسن الحظ ان كتاب الحيل هو من الكتب القليلة الي وصلت الينا من اعمال بني موسى ولكن رغم شهرة الكتاب فان المخطوطات المتنقية منه قليلة . وماك الآن ثلاثة مخطوطات رئيسية منه فقط هي مخطوطة طويقاني سراي . احمد الثالث 1848 ومخطوطة الفاتيكان رقم ٣١٧ ومخطوطة ثالثة مورعة بين مكتبة غوتا في المانيا المديموقراطية وتحمل الرقم ١٣٤٩ - أ (ع 1349) وبين مكتبة برلين في المانيا الغربية وتحمل الرقم ١٣٤٩ . والمخطوطة الاولى (طويقاني) لم تكتشف الا مؤخراً (٧٠).

با أ اهتمام مؤرخي العلوم بكتاب الحيل لبني موسى منذ نهاية القرن الماضي ولكن اللاراسات الجادة حوله بدأت في مطلع هذا القرن عندما قشر كل من ڤيدمان وهاوسر مقالات حول اواني الشراب وشرحا الاشكال ٨٥ ــ ٨٧ من كتاب الحيل(٧) . ثم نشر

٣ -- صدر النص المريبي مؤخراً : الجامع بين العلم والعمل النافع في صناعة الحيل لابن الرراز (فجرري ، تحقيق الدكتور الحسن ورملاؤه (معهد التراث العلمي العربي ١٩٧٥) وسقته الترجمة الانكتيزية لد دونالد هيل ١٩٧٣.
 ٤ -- صدر النص العربي لأحمد يوسف الحسن » الطرق السبية في الآلات الروسامية » ، معهد التراث العلمي العربي - حلم ، ١٩٧٧

ةً – 'تشر لـ درنائد هيل في محمة تاريخ للعلوم العربية ١ (١٩٧٧) ، ٣٣ – ٤٦ . مقالة عن كتاب الأنسي في الآلات يعود الى القرن الحاس الهجري / الحادي عشر الميلادي ، وثبت فيها بعد انه السرادي .

٣ - أنظر عجلة هيل الجزري ترجّمة دائيد أ. كينغ 8 الحيل المصور الوسطى ٤٥ تدريخ الداوم٤٣٤ (١٩٥٧).
 ٣٨٩ - ٩٨١ .

۷ -- اینهارد فیدمان و ف. هاوسر ۱۱ الجزري و بنو موسی ، في مجلة الاسلام ، ۸ (۱۹۱۸) عس ۱۵۵-۹۲ م ۲۹۸ – ۲۹۹ . هاوسر كتاباً موسعاً ادرج فيه بقية اشكال كتاب الحيل (^). وبذلك اصبح كتاب الحيل معروفاً باللغة الألمائية وقد استند فيدمان وهاوسر الى مخطوطة الفاتيكان بصورة رئيسية والى مخطوطة غوثا — برلين بصورة ثانوية . ونظراً للنواقص الكثيرة والاخطاء الواردة في هاتين المخطوطتين فقد بذل هاوسر جهداً كبيراً في محاولة تفسير الاشكال ولم يتقيد بسبب ذلك بايراد ترجمة حرفية للكتاب بل اعاد الصباعة بالالمانية بالاسلوب الذي يجعل النص مفهوماً من الباحية الفنية .

وكان العمل الاخير والهام الذي تباول كتاب الحيل هو الترجمة الانكليزية الكاملة التي صدرت هذا العام والتي قام بها دونالد هيل . وهيل بعمله هذا يكمل ما كان قد ندأه عندما أصدر الترجمة الانكنيزية لكتاب الجزري في عسام ١٩٧٥ بالاضافة الى اعمال اخرى قام بها ونشرها (أو هي في سبيل النشر) عن التكنولوجيا الميكانيكية العربية الاسلامية.

ويتميز كتاب الحيل لبني موسى الذي اصدره هيل بالانكليرية بانه اول كتاب يصدر مشتملاً على كامل كتاب الحيل باية لغة كانت بما في ذلك اللغة العربية , وقد كان لاكتشاف مخطوطة طوبقاني في استاذول اهمية كبيرة زادت من قيمة كتاب هيل وجعلته متميزاً عن كتاب هاوسر الصادو باللغة الإلمانية ,

قسم هيل كتاب الحيل الى قسمين ، القسم الأول هو المقدمة واهم ما اشتملت عليه هو : ١ – حية بنى موسى واعمالهم ٢ – محطوطات كتاب الحيل مع تحليل مفصل قارن فيه بين المخطوطات الثلاثة الرئيسية ، ٣ – الابحاث السابقة التي تناولت كتاب الحيل ، والوسائل \$ – تحليل تاريخي لكتاب الحيل والاعمال المماثلة ، ٥ – شرح للمبادى، والوسائل الاساسية التي استخدمت في تصميم تجهيزات بني موسى في كتاب الحيل . والقسم الثاني من الكتاب يحتوي على الرجمة الكاملة للاشكال (Devices or models) المائة لكتاب الحيل مع الملاحظات والتعليقات في جاية كل شكل .

واورد هيل بعد ذلك ملحقاً يحتوي على ثلاثة اشكال لم تثبت نسبتها الى كتاب الحيل وقد ورد احدها في مخطوطة الفاتيكان والثاني في مخطوطة طويقابي والثالث في مخطوطة ليدب (Or 168). واورد هيل بعــد دلك قائمة بالمراجع ثم اورد معجماً «Clossery بالمفردات العربية ومعانيها باللغة الانكليزية.

٨ - ف. هارسر د عن كتاب الحيل ، (ارلونشن ، ١٩٢٧) .

وقد استخدم هيل مخطوطة طوبقاني بشكل رئيسي وحيثما كان البص موجوداً في هذه المخطوطة فقد كانت هي المعتمدة وقارنها مع مخطوطة الفاتيكان ولم يجد صرورة للمقارنة مع مخطوطة غوتا – برلين . وفي حالات اخرى كانت الهاتيكان مي المخطوطة المعتمدة ودلك بالنسبة للاشكال المفقودة من مخطوطة صوبقاني . وفي الاشكال العشرة الاخيرة أصحت مخطوطة برلين هي المخطوطة الوحيدة نطراً لفقدان هذه الاشكال من كل من محطوطةي طوبقاني والفاتيكان .

وقد اورد هيل في نهاية كل شكل Model الصورة الفوتوغرافية للرسم الحاص مالك الشكل كما ورد في المحطوطة ، ثم اعاد رسم ذلك الرسم من جديد مهملاً التفاصيل غبر الضرورية كايدي الابارق والزخارف وغيرها ودون على هذه الرسوم (التي اعاد رسمها) الحروف اللاتيبية المرادفة للحروف العربية . وفي بعص الحالات اورد ايضاً رسومات توضيحية حليثة واقتبس بعضاً من هذه الرسوم التوصيحية من كتاب هاوسر مشيراً الى ذلك في جميع الحالات .

واورد هيل في نهاية كل شكل الملاحظات اللازمة لشرح الافكار الغامضه او لتوضيح المبادىء التي يستند اليها عمل ذلك الشكل . ولكنه احتصر الكثير من الشرح عندما اورد في مقدمة الكتاب فصلاً خاصاً شرح فيه المبادىء والوسائل التي استحلمها بنو موسى في تصميم اشكالهم والتي تكررت في تلك التصاميم .

ان هذا العمل الذي قام مه هيل جدير بالاحترام والتقدير . ويدرك ذلك كل من حاول تحقيق كتاب من هذا النوع . ههو يحتاج الى خبرة ودراية بالفن داته كما انه يحتاج الى معرفة جيدة باللغة العربية . ولقد تخصص هيل بابحاث انفرد بها واكسبته شهرة استحقها بحدارة عندما ركز اعماله على ترجمة المخطوطات الحاصة بالتكنولوجيا الميكاليكية العربية العربية باللغة الانكليزية قبل ان تصدر الاسلامية . واصدر حتى الآن أهم كتب الحيل العربية باللغة الانكليزية قبل ان تصدر هذه الكتب باللغة العربية ذاتها، وفي عمل عدي صعب من هذا النوع لا يخلو الأمر من ورود بعض الاخطاء ، ولكن هذه الاخطاء تصبح ثانوية وغير ذات قيمة نسبية امام الاهمية الكبيرة لهذا الانجاز . لقد اعطى هيل بني موسى حقهم كاملاً بعمله هذا ولم يعد كتاب الحيل اسطورة نتداول نشأنها ما اورده ابن التديم والقفطي وحاجي حليفة بن اصبح الآن كتابًا علمياً هندسياً نفهمه و نتمتع بقراءته ، والمرجو الآن ان يصدر الآن النص العربي الكامل كمرادف لا بد منه المترجمة الانكليزية .

أحمد يوسف الحسن

معهد التراث العلمي العربي جامعة حلب

المشاركين في العدد

- عادل انبوبا: حول تاريخ ابحبر والهندسة وقد درس تاريخ الرياضيات والعلوم العربية في الجامعة اللبنانية وفي كلية الاقتصاد الفرنسية ، وتضمنت مؤلفاته دراسات حول الرياصيين المسلمين مثل الكرجي وشجاع من اسلم وشرف الدين الطوسي والسموءل بي على وغيرهم .
- برناره ر. غولدستاين: درس تاريخ العلوم الدقيقة في العصور الوسطى ، من
 بين انجازاته القيمة اكتشافه ونشره وترجمته عن العربية ودراسته التحليلية للجزء الأكبر
 من فرضيات بطيلمة في الكواكب السيارة ،
- روبرت إ. هول: ١هتم بتاريخ العموم الاسلامية وفلسفتها بشكل عام ويعلم النفس
 واليصريانة وعلم الحركة بشكل خاص.
- احمد يوسف الحسن: رئيس جامعة حلب ومدير معهد البراث العلمي العربي
 هو مؤرخ عن التكنولوجيا عند العرب. ويقوم حالياً ببشر كتاب عن بني موسى وفن
 الحيل.
- عادة الكرمي: طبيبة و ورخة عن الطب العربي اهتمت بوجه خاص بالكناشات
 وهي كتب تطبيقية في ممارسة الطب.
- ا. س. كندي : ركز جهوده حول علم الفلك الإسلامي ودرس بتركيز عال معظم اعمال البيروقي والكاشي .
- مصطفى موالدي: من موظفي معهد التراث العلمي العربي كتب مقالات اقتصادية
 واحصائية ، ويحضر حالياً لقداً لكتاب النجريد للنسوي وهو مقدمة في الهندسة .
- سيد حسين نصر : مؤلفاته المدرسية العديدة والتي تنوعت مواضيعها شملت عدم الأبراج والدين والتصوف والقانون وكذلك تاريخ العلوم .
- جورج صليها : إنضم حديثًا الى كلية جامعة كولومبها وشمل اهتمامه دور السوريين
 في نقل العاوم الاغريقية الى الاسلام .

ملاهظات لمي يوغب الكتابة في العالة

- ١ تقديم نسختين من كل بحث أو مقال الى معهد الراث العلمي العربييي طبع النص على الآلة الكاتبة مع ترك فراع مزدوج بين الاسطر وهوامش كبيرة لأنه يمكن أن تجرى بعض التصحيحات على انتص ، ومن أجل توجيه تعليمات الى عمال المطبعة . والرجاء ارسال ملحص يتراوح بين ٣٠٠ ـ ٧٠٠ كلمة باللغة الانكليزيمة إذا كان ذلك ممكناً وإلا باللغة العربية .
- ٢ طبع الحواشي المتعلقة بتصنيف المؤلفات بشكل منفصل وثبعا للارقام المشار
 البها في النص . مع ثرك فراغ مزدوج أيضا ، وكتابة الحاشية بالتفصيل ودون
 أدنى اختصار .
- أ بالنسبة للكتب يجب أن تحتوي الحاشية على اسم المؤلف والعنوان الكامل الكتاب والناشر والمكان والتاريخ ورقم الجزء وأرقام الصفحات التي تم الاقتباس منها .
- ب- أما بالنسبة للمجلات فيجب ذكر اسم المؤلف وعنوان المقالة بين أقواس صغيرة
 واسم المجلة ورقم المجلد والسنة والصفحات المقتيس منها.
- ج أما إذا أشير الى الكتاب أو المجلة مرة ثانية بعد الاقتياس الأول فيجب ذكر اسم
 المؤلف واختصار لعنوان الكتاب أو عنوان المقالة بالاضافة الى أرقام الصفحات.

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 انسويا ، و قضية هندسية ، ، ص ٧٤ ,

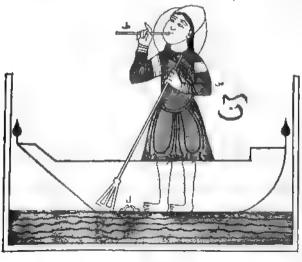
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« الجامع بين العلم والعمل الناقع في صناعة الحيل » الجزري (١١٨١ ــ ١٢٠ هـ)

تحقيق الدكتور أحمد يوس**ف الحسن**

- هذا الكتاب نقد ودراسة للنصر العربي الكامل لم ٥ مغطوطات انتشاعا المحقق من
 الم ١٥ مغطوطة التي ذكرت في المقدمة ٠
- ــ تم رسم الاشكال بعد دراستها وانتقاءها من بين العديد من الاشكال المتوفى، في مجموع المخطوطات •
- _ يمش النص بتغاصيل دقيقة آلات ميكانيكية ومائية متنوعة استعملها العائم الاصلامي
 قبل المقرن الرابع دشر *
- مناك معجم تضمن جميع الالفاط التكنولوجيمة المستعمسلة في النمسوس الاصلية
 وما يقابلها باللعتين الانكليزية والمربية الماسرة ٠
- هذا المعل سيخدم مؤرخي علم التكنولوجيا والعلوم الاخرى وبعدورة عامة كل من يهتم بناريخ الشرق الاوسط •
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 - _ كل مدًا يه ١٠٠ له س / ٢٥ دولار؟ قتيد ٠



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In the transliteration of words written in the Arabic alphabet the following system is recommended:

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The diphthong aw is used for , and ay for ,

NOTES ON CONTRIBUTORS

Adel Andouba works on the bistory of algebra and geometry. He has taught the history of Arabic smence and mathematics at the Lebanesr University and at the French Faculty of Economics. His publications include studies on al-Karaji, Shuja* b. Aslam. Shurof al-Din al-Jusi, al-Samawai h Yahyā al-Maghribi and other Islamic mathematicians

Besnard R. Goldstein studies the history of the medieval exact sciences. Among his notable scheevements was the discovery, publication, translation from the Arabic, and analysis, of a major portion of Ptolony's Plantary Hypotheses

Rebert E. Hall is interested in the history of Islamic science and philosophy in general, and in psychology, optics, and mechanics in particular.

Ahmad Y. al-Hassan, Rector of Aloppo University and Director of the Institute for the History of Arabic Science, is a historian of Arabic technology. He is currently preparing a text edition of the book by the Band Müsä on mechanical devices.

Ghada Karon is a physician and historian of Arobic medicine. She has been particularly interested in the Kunnāshāi, medical compendis used as manuals by medieval practicioners.

E. S. Kennedy has centered his efforts upon the history of Islamuc astronomy, having studied intensively several of the works of al-Birūni and al-Kāshī.

Mustafa Mawalds, of the staff of the Institute for the History of Arabic Science, has written articles on economics and statistics. He is preparing a critical edition of al-Nasawi's Kitāb al-tojrīd, an introductory manual of geometry.

Seyyed Resear Near 16 a scholar whose very numerous publications range over a wide gamut of subjects, including cosmology, religion, mysticism, and law, as well as the history of science.

George Saliba has recently joined the faculty of Columbia University. His interests include the rôls of Syriac in the transmission of Greek science to Islam

this field his achievements have won him well deserved fame. So far he has published English translations of the most significant Arabic books on ingenious devices, even before these treatises had been printed in the original. Naturally, any detailed work of this sort will be found to contain occasional errors. However, in view of the importance of his accomplishments, such errors are insignificant, almost negligible. By his labors Hill has paid the Banū Mūsā their full tribute. Thanks to him, the Kutāb al-Hiyal is no longer a shadowy work concerning which the non-specialist must speculate on the basis of the remarks of Ibn al-Nadim, Ibn al-Qiftī, and Hājī Khalifa. It has taken its rightful place as a book of science and engineering, a work which we comprehend and onjoy reading. It is to be hoped that the complete Arabic text will soon appear, to complement Hill's English translation.

AHMAD Y. AL-HASSAN

University of Aleppo Institute for the History of Arelia Science published by him on Islamic-Arabic mechanical technology.

The distinctive feature of this English version is that it is the first in any language (including Arabic) which presents the *Kitāb al-Hiyal*) in its entirety. The discovery of the Topkapi MS in Istanbul has been of great value, giving Hill's work notable precedence over the German version by Hauser.

Hill's book comprises two sections, the first being the Introduction. Among other important matters dealt with in this part are: (1) the life and work of the Banu Müsä, (2) manuscripts of the source, (3) earlier information on The

Book of Ingenious Devices, (4) historical context, and (5) motifs.

The second part of the book contains a complete translation descriptive of the hundred devices or models which occur in the Kutāb al-Ḥiyal. Following each model are notes and commentary.

Hill's book ends with an appendix comprising three models whose relation to the Kitāb al-Hiyal is challengeable. One occurs in the Vatican MS, another in the Topkapi version, the last in Leyden MS (Or. 168). There is a list of references consulted, and a glossary of Arabic terms and their English equivalents.

In his research, Hill depended basically on the Topkapi MS. Wherever a passage occurs in this MS. Hill relied on it primarily, comparing it to that Vatican copy. He deemed it unnecessary to collate it with the Gotha-Berlin MS. Elsewhere, the Vatican MS was taken to be the primary document, that is, in relation to those models missing in the Topkapi MS. Insofar as the last ten models are concerned, the Berlin MS is the only source available, since these are missing in both the Topkapi and the Vatican copies.

Following the translated description of each model. Hill provides a photographic reproduction of the drawing of that model as it occurs in one of the MSS. Then he displays a simplified version of the same drawing, omitting unnecessary details, such as the handles of pitchers, decorations, etc. He also puts, on these redrawn sketches, the Latin letters corresponding to the Arabic of the original. Occasionally he also provides a modern illustrative drawing, sometimes adapted from Hauser's book, with due acknowledgment. Finally, Hill inserts, following most of the drawings, appropriate remarks elucidating obscure ideas, or illuminating the fundamentals on which the particular model relies. Much repetition in these places has been saved by devoting a special section in the Introduction to an explanation of the common principles and recurrent methods used by the Banū Mūsā in designing their models.

Judging by any standards, the work undertaken by Hill is stimulating; it is to to be highly esteemed. Whoever attempts to edit a book of this nature realizes the amount of experience and the mastery of technique needed for such work. It also presupposes good knowledge of Arabic. Researches by Hill stand almost unique. For some time he has concentrated on translating and annotating works pertaining to Islamic Arabic mechanical technology, and in

The Sublime Mothods of Spiritual Machines, by Taqi al-Din ibn Macrif al-Räsid al-Dimashqi. These three books, separated as they are by long intervals of time (respectively, the 3rd 9th, 6th, 12th, and the 10th/16th centuries) constitute three major hoks in the chain of mechanical engineering achievements, a component of Islamic-Arabic civilization. It is to be hoped that the recovery and publication of other books will supply the missing links to the chain.

Thus the Islamic-Arabic legacy in the field of ingenious devices begins with the work of the Banu Musa, a book which won resounding fame in the Arabic literature. Fortunately, this is one of the few books by the Banu Musa that have survived. However, in spite of its being widely known, the extant MSS are few. Today there are only three major copies: Topkapi Saray Ahmet III 3474; Vatican MS 317; and a third MS, divided between the Cotha library (No. 1349) and Berlin (No. 5562). The Topkapi MS has only recently come to light.

It was towards the end of the last century that historians of science began to devote their attention to the Kuāb al-Hiyal by the Banū Mūsā. Serious studies ou this book, however, were not conducted before the first decades of this century, when Wiedemann and Hauser published articles on the drinking pitchers, and described figures 85-87 of the Kitāb al-Hīyal." Hauser later published a lengthy book into which he incorporated the remaining figures. Thus the work became available in German. Wiedemann and Hauser depended primarily upon the Vatican MS, and, in a secondary sense, upon the Gotha-Berlin version. Because the texts in these MSS were sadly truncated and seriously defective. Hauser exerted much effort in attempting to interpret the figures. In consequence he had to take liberties with the translation, recasting the German in such manner as to render the text intelligible from the technical point of view.

The latest and most important research on the Kitâb al-Hiyal is the book here reviewed, the English translation of the complete text by Donald Hill. He thus continues an important project commenced in 1973 with his English translation of the book of al-Jazari. This is in addition to other research

The Arabic toxt has been edited by Ahmad Y. al-Haraan, Al-Turnq al-sanitys ft al-didt al-rikiniya (Alappo, IHAS, 1976).

⁵ For word of an additional link, see Donald R. Hill, "A Trentise on Machines...", Journal for the History of Arabic Science, 1 (1977), 33-46.

See the review of Hill's al-fuzari translation by David A. King, "Medieval Mechanical Devices", History of Science, 13 (1987) 284-289.

⁷ Eithard Wiedemann and F. Hauser, "Über Trinkgefätere und Tofelaufeätze nach al-Gusaff und den Bang Müs?". Der Islam, 8 (1918), 58-93, 268-291.

B. F. Unuser, "Uher das Kitäh nl-Hiyal. . . ", Abhandl. zur Gesch, der Naturwissenschaften und der Medezin (Erlaugon, 1922).

^{9.} See Note 3 above.

Book Review

Donald R. Hill (Translator), The Book of Ingenious Devices (Kitāb al-Ḥiyal) by the Bonā (sons of, Māsā bin Shākir, Translated and annotated by Donald R. Hill. Dordrecht, Holland: D. Reidel Publishing Co., 1979, x + 267 pages. Dfl. 130 / \$63.

The Banu Musă lived in the 3rd (H.)/9th (A.D.) century, when Arabic civilization had reached its zenith. In the reign of al-Ma'mun and the caliphs who succeeded him, the three sons of Musă bin Shākir-Muḥammad, Aḥmad, and al-Ḥasan - played a prominent part in promoting the sciences, particularly mathematics, astronomy, and mechanics. This they did through their writings, as well as by their pervasive influence on the translation movement from Greek into Arabic. But while the writings of the Banu Musā were voluminous and varied, the work which stands out as distinctive is The Book of Ingenious Devices (Kitāb al-Ḥiyal). Wherever mention is made of the Banu Musā, this ingenious piece of work stands as their greatest achievement.

In the Mafatth al-cUlum, al-Khwarizmi sets down al-hiyal (the science of ingenious devices) as one of eight fundamental disciplines. He then divides it into two parts: one pertains to the moving of weights by application of mechanical advantage; the other deals with ingenious devices for moving water, and the making of curious vessels, along with the related art of automata.

In later classifications of the sciences, al-hypal found itself categorized as a branch of al-handasa, not in the mathematical sense (geometry), but rather in the technological (the engineering)² sense.

In any case, and apart from classifications of the sciences, so widely different from age to age, the science of ingenious devices, or al-hiyal, falls within the scope of mechanical engineering, as it doals with machines, instruments, and hydraulic and mechanical equipment.

Until recently, only two Arabic books on the subject had been widely known, one, The Book of Ingenious Devices by the Banu Müsä, the other A Compendium on the Theory and Practice of Ingenious Devices by Badic al-Zamān ibn al-Razzāz al-Jazarī.³ To these two have now been added a third,

Muhammad b. Ahmad b. Yilasf ul-khwarizmi. Mafault al-Uhim (Cauro, idarat al-Tibaf at al-Muninya, 1342 H.), p. 191.

² Ahmad al-Qalqashandi, Subh al-I'sha (Cairo, al-Matha at al-Amiriya, 1913), vol. 1, p. 476.

^{3.} The Arabic text has recently been published Al-Idmic bayn al-cilm w'al-camal al-nafic fixed al-hayol, by Ihn al-Razzaz al-Issari, edited by Abroad Y al-Hassan, Institute for the Ristory of Arabic Science, hereafter IHAS, (Aleppo, 1979). This was preceded by the English translation. The Book of Knosvilsage of Ingenious Mechanical Devices by Ihn al-Razzaz al-Juzari, translated and annotated by Dougld Hill (Dordrecht, Reidel, 1973).

TEACHING POSITIONS AVAILABLE AT THE

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University of Aleppo, Aleppo, Syria

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etc.

Candidates: Should be holders of the doctorate,

prefecably able to teach in Archie.

Salary:

Depends upon the appointer's qualifications

(Travel of appointee and family paid).

Professor al-Haschmi Honored

On June 7, 1979, the Institute for the History of Arabic Science held a ceremony in honour of Professor Muhammad Yahya al-Haschimi. The program included a poem in praise of this noted historian of science by 'Omar Abu Qaws. Drs. Taha Ishaq Kayali, 'Abd al-Salam 'Ujeili and Mr. Fuad Aintabi delivered speeches dealing with Professor Haschmi's life and work. His books were on display during the ceremony, and he was nominated for the Syrian Order of Merit. His book on plants, which Dr. Nazir Sankari is presently revising, will be published in the near future.

Professor Haschmi was born in Aleppo in 1904. He studied chemistry and philosophy in Germany, and took the doctorate for his study on al-Birūnī's Kitab al-Ahjār. During his long professional career he has taught in secondary schools in Aleppo, and lectured at the university. His special interest has been the history of Arabic and Islamic science and its transmission to the West. He has published a number of articles and several books, His most important achievement was the establishment of the Syrian Society for Scientific Research in 1957. Professor Haschmi has retired from teaching, but is still pursuing his scientific activities, in addition to being an active member of the Syrian Society for the History of Science.

Professor Sezgin Winner of King Faisal International Award

Professor Fuat Sezgin, the candidate of the Institute for the History of Arabic Science for the King Faisal International Award, won the award for Islamic studies, bestowed in recognition of his six volume work, Geschichte des arabischen Schriftiums. Professor Sezgin has already spent twenty years collecting and compiling his source material for this monumental publication, and two further volumes are still in preparation.

One of the orientalists present at the congress held in Würzburg (FRG) in 1968, said in praise of this great schievement, "Brockelmann was the centre of attention for many a year, but the Geschichte des arabischen Schriftums will become one of the 20th century's most important contributions to Arabic literary culture and the classification of the immense Arabic heritage".

In the introduction to the first volume of the Arabic translation from its German original, Dr. Fahmi abu al-Fadl says, "This is not only a book or science, but also a proof of great achievement if we consider that such a work is usually compiled by a group of scholars. Yet the Geschichte des arabischen Schrifttums is entirely the work of Professor Sezgin".

Professor Sezgin was born in Istanbul in 1924 where he studied, taking his doctorate in Islamic Science and Persian Studies. For a number of years he was on the faculty of the University of Istanbul.

The History of Rhetoric written in Turkish (1947), and Studies on Bukhari's Compendium of Sources, published in 1956, are only two of Professor Sezgin's numerous works. In 1960 he moved to Germany, where he lectured for two years at the Institute for Semitic Languages of the University of Frankfurt. Subsequently he was named a visiting professor at the Institute for the History of Natural Science at the same institution. He then obtained a chair at the University of Frankfurt with all the rights of a German professor, although he retained his Turkish nationality.

He was granted the award on February 27, 1979, in an official ceremony held in Riyad under the patronage of His Majesty King Khaled ihi Abdul Aziz. Dr. Ahmad Y. al-Hasan, Rector of the University of Aleppo and Director, Institute for the History of Arabic Science, attended the official celebration.

The award consists of a certificate bearing the name of the prize, a valuable medal, and a sum of money equivalent to 200,000 Saudi Rials.

The Second International Symposium for the History of Arabic Science

The opening ceremonies were convened on Thursday, 5 April, 1979, before an audience of seven hundred people. The scientific meetings commenced on the same day. These continued through Monday, 9 April, being held in various auditoriums of the University of Aleppo.

The meetings included three semmars, having the following themes:

The Place of Science and Medicine in Medieval Islamic Civilization

The History of Algebra

and The Transmission of Arabic Science to the Latin West

Each seminar was addressed by a group of from two to four invited speakers,

after which the meeting was thrown open for general discussion.

In addition to the seminars, there was a total of seventeen sessions for the presentation of some 114 short papers on topics chosen by the participants, opportunity being given for questions and remarks from the floor after each paper. These sessions were organized by fields of study, with two or more running simultaneously. The history of medicine was by far the most popular subject with thirty-four papers. Next was mathematics with eighteen, thence lesser numbers of presentations involving astronomy, the earth sciences, technology, astrology, alchemy, physics, agriculture, and so on.

Interspersed with the scientific sessions were lectures and film showings of general interest, notably of the excavations at the famous nearby site of

ancient Ebla.

The Institute for the History of Arabic Science prepared exhibits of publications of the University of Aleppo and of the numerous objects which make up the first acquisitions for the Institute's future history of science and technology museum.

The last day of the Symposium concluded with a general meeting of par-

ticipants, for the adoption of resolutions, and a final banquet.

On Tuesday, 10 April, those of the departing visitors who so chose were escorted on tours to Ebla and the Krak des Chevaliers via Homs, or to Lattakia and Ugarit.

Scholars resident in a total of twenty-seven different countries were present. Naturally, the twenty-three from Syria, the host country, made up the largest group. There were twenty-seven from the other Arab countries, about a third of these being from neighboring Iraq. The eleven participants from the USSR made up the largest single delegation, with West Germany, France, the U.S. A., and the United Kingdom not far behind

Many of the participants expressed gratification at the level of the material presented, and with the arrangements in general. The organizers of the Sym-

posium may congratulate themselves upon a job well done.

by Shath in his published catalogue, is not noted by either Brockelmann, Sezgin, or Ultmann in their hibbographies.9

The Manuscript

(Number: Antaki 1)

Damaged and faded leather cover. The binding has come apart and most of the pages are loose, but otherwise the manuscript is well-preserved. Stained pages. Almost no marginal notes. The first page contains one owner's seal and four entries in different hands. One of these, which appears to be more recent than the text, reads:

كتاب المنصوري في حفظ الصحة ومعاجة الأمراض لمن يحصره الطبيب تأليب الشيخ الحكيم أني يكر محمد بن زكريا الم ازى

182 ff. Complete. Paginated in ink. Ends on p. 364.

 18.5×11.5 cm. 22 lines.

Legible naskhi script, partly vocalised. Red ink headings. No scribe's name. Undated. Probably 7th/13th century (as Sbath).

Begins:

بسم الله الرحن الرسيم دب يسم وأعلى برحمتك بجدا كتاب "للمه [aic] محمد بن ركريا الوازي للسلسور بن اسحاق اسمبيل بن أحد فقال اني حامع للامير أطال الله بقاء جملا وجوامعا ولكتا وعيون من مساعه الطب بيتمد في ذلك الاختصار والايجار ولأاكر من ما لا يحدث ...

Ends:

طيوحه طم رطل من وزد درهم مصطلح يزدهم قرمتل ردرهم سبل قصير في حرقة ونتقى عبد الطبخ هيـه انه شاه أنه تمالى واذ اتيما على جميع المقالات والعصول المذكورة في صدر هذا الكتاب فقد كل كتاب هد ونة الممين والموفق للصواب وهو حسيد ونعم الوكين ولا حوب ولا فوة لا ناقة ألملي العظيم ثم الكتاب والحمد أنه حق حمله وصلو أنة على سيدتا محملة وآله وصحيه وسلم تسديا

It is of course always useful to discover the whereabouts of an Arabic scientific manuscript. But it is particularly useful in this case for two reasons: firstly, there is no modern printed edition of K. al-Manyari, and secondly, the book is of great importance to the history of Arabic medicine and mediaeval learning. In addition, this manuscript is especially valuable because it is complete, well-preserved, and appears to be early. Many of the surviving manuscripts of K. al-Manyari are incomplete, sometimes lacking as much as a half or a third of the original text.

It is fortunate that this manuscript has been released from private owner-ship and is now available for scholarly use. 10

⁹ C. Brockelmann, Geschichte der grabischen Litteratur (Weimar: Felber, 1898-1902), Vol.1, pp. 233-5 (nin would not of course expect the Shath manuscript to be mentioned in this edition), Supplement, (Leiden, Brid, 1937-42), Vol. I, p. 417, Sezgin, op. cu., Vol. III, pp. 281-2; M. Ullmann, De Medizin im Irlam (Leiden Brid), 1970), p. 132.

^{10.} In this connection, it should be mentioned that I am currently preparing an edition of Book 9 for publication by the III 4S. This MS will be one of those used to the preparation of this edition.

scripts of the work extant, dispersed in various castern and western libraries. This large number and the wide temporal span of the surviving manuscripts is further testimony to its popularity. Yet, spart from Reiske's Arabic and Latin edition of 1776, there has been no Arabic edition of the work in modern times. The first maqāla was edited and translated into French by de Koning in the early part of this century.

K. al-Manşūri is moderately large, (the manuscript length averages at 200 ff.). It deals with all the major topics of medical importance of the time,

as the subjects of the ten magalat indicate:

The Form and Appearance of Organs
Knowledge of the Temperaments of Bodies and the Preponderant Humours in Them
The Faculties of Foods and Medicines
The Preservation of Health
Cosmetics and External Diseases
The Management of the Traveller
Bonesetting, Wounds and Ulcers
Poisons and Insert Bites
The Diseases from Head to Toe

Fevers, Cotton, Crism, the Urms and the Pulse

In 1977, the Institute for the History of Arabic Science at Aleppo received a gift of 255 manuscripts from a well-known art collector of Alepno. Mr. George Antaki. Among the medical works was a manuscript of K. al-Mansari. The only copy of this book previously known to have been in Aleppo was the one mentioned by Father Paul Shath in his 3-volume catalogue of the manuscripts held in private collections in Aleppo. Here, he refers to a manuscript of K. al-Mansari in the collection of the consul for Holland, M. Rodolphe Poché. The entry in Sbath's book is characteristically brief and gives no description of the manuscript. B Careful inquiry has established that this manuscript of the Dutch consul is the same as that donated to the IHAS. It had passed from that owner into the posession of others and thence to the final purchaser who donated it to the IHAS. With the manuscripts came also a hand-written list of their titles, authors, and brief descriptions. This is contained in a small exercise book, said to have been written by Paul Shath in the 1930s in preparation for a fuller catalogue (which he never undertook). The entry for K. al-Mangari dates it as 13th century (A. D.) and marks it as 'précieux'. No other description is given. The existence of this manuscript, although it was listed

^{6.} There are manuscripts of this work dating from the 5th/11th century until the 12th/18th century. For details, see F. Sezgin, Gaschichte des arabischen Schriftums (Leiden: Brill, 1967), Vol. 111, pp 281-2.

^{7.} P. de Koning, Trais traités d'anatomis arabe (Leiden: Brill, 1903), pp. 2-98.

^{8.} P. Shuth, al-Fibritt, catalogue des manuscrits arabes, 3 volumes plus supplement, Cairo, 1938-49, Vol.I., p.99. Elsewhere (Introduction, p.vii), Shuth says that this Consul had a large collection of Arabic manuscripts.

NOTES AND CORRESPONDENCE

Notice of Another Manuscript of al-Razī's Kitab al-Mansurī

GHADA KARMI*

ONE OF THE MOST FAMOUS of Abū Bakr Muhammad b. Zakarıyya al-Rāzī's books was the comprehensive book on medicine which be dedicated to the Samanid prince. Abū Ṣāhih al-Mansūr b. Ishāq. (after whom it was known as the K. al-Manṣūri). It was an extremely celebrated work in the Latin West throughout the Middle Ages, and was translated into Hebrew, Greek and Latin, the last by Gerard of Cremona in 1175. It was printed in Latin in 1481, and was reprinted many times thereafter. There are also many Latin manuscripts of the book extant, further proof of its popularity in the West. K. al-Manṣūrī is divided into ten treatises, or maṇālāt. The 9th maṇālā, or Liber Nonus (alternatively known as the Nonus Almansoris), which deals with the diseases from head to toe, became especially important in Latin translation. It was printed many times, particularly in the 15th century, and was extensively used and commented on in the 15th and 16th centuries. The most famous of these commentaries was Andreas Vesalius' paraphrase, which was published in 1537.

K. al-Manşūri was also popular and important in the Arabic East. Abū'l'Abbās al-Majūsī, the 10th-century author of the medical encyclopaedia, Kāmil
al-Ṣinā'a, says in his introduction that al-Rāzī had surpassed all others in the
excellence of his book, K. al-Manşūri. Today, there are no less than 47 manu-

^{*}The Wellcame Institute for the History of Medicine, 183 Fusion Road, London, N.W 1, U. S. 1. See M. Steinschneider, Die europäischen Ubersetzungen aus dem Arabischen bis Mutte des 17. Jahr. hunderts (Vienna, 1904-5), p.25.

See L. Thorndyke and P. Kybre, A Comlogue of Incipits of Mediannal Scientific Writings on Latin, revised and augmented edition, (Medianval Academy of America, 1963), pp. 272, 471, 1053, 1375, 1538, 480, S. Punsier, "Catalogues des manuscrits medicaux des bibliothèques du France". Sudhoffs Archiv, 2(1908), 36-7.

See H. Schipperges, "Bemerkungen zu Rhazes und seinem Liber Nonus", Sudhaffs Arche, 47(1968), 373-7.

^{4.} Andreus Vesalius, Paraphrasis in Nonum Librum Rhazas (Basle, 1537).

^{5.} Al-Majūsī, Kāmil al-sanā'a (Cairo, Bulaq, 1294/1877), Vol. I, p. 5, 1, 1-3

En collaboration avec René R. J. Rohr, "Deux astrolabes-quadrante turcs", Contaurus, 19(1975), 108-124.

1976

"Un cadran solaire juif", Centaurus, 19(1976), 264-272,

"Un compendium de poche par Humphrey Cole (1887)". Annali dell'Istitusa e Museo di Storia della Scienza di Firenze, 1 (1976), 1-11.

1977

"Quelques aspects récents de la gnomonique tunisienne", Revue de l'Occident Musulman et de la Méditerranée, (Aix-en-Provence, France), 1977, 207-221.

"Un cadran de hautour", Annali dell'Istituto e Museo di Storia della Scienza di Firenze, 2 (1977), 21-25.

En collaboration avec D. A. King: "Ibn al-Shātir's Şandūq al-Yawāqīt: An Astronomical Compendium", Journal for the History of Arabic Science, 1(1977), 187-256.

1978

"Un cadrau solaire grec à Aî Khanoum, Afghanistan", L'Astronomie (Paris), 92 (1978), 357-362.

En collaboration avec D. A. King: "Le cadran solaire de la Mosquée d'Ihn Tülün au Caire", Journal for the History of Arabic Science, 2(1978), 331-357.

"Un texte d'ar-Rudani sur l'astrolabe sphérique", Annalı dell'Istituto e Museo di Storia della Scienza di Firenze, 3(1978), 71-75.

1979

"Astrolabe et cadran solaire en projection stéréographique horizontale", Centaurus, 22(1979), 298-314.

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tan. Toutes ses recherches furent brutalement interrompues par son décès en décembre 1978, alors que deux articles étaient encore sous presse.

On trouvera ci-après une liste de ses publications.

1969

"L'histoire du cadran solaire", La Suissa Horlogère, (1969), 93-101.

1970

"Note sur le cadran solaire de Brou", L'Astronomie, Paris (1970), 83-85.

"Les cadrans solaires polyédriques du musée du Pays Vaurais", Bulletin de la Société des Sciences, Arts et Belles-Lettres du Tarn, N. S., 29(1970), 357-365.

1971

"Les méridiennes du château de Versailles", Revus de l'Histoire de Versailles, 59(1971).

"Un cadran solaire astronomique", L'Astronomie, Paris (1971), 251-259.

1972

- "Le cadran polyédrique du cloître de Brou", Bulletin de la Société des Naturalistes et Archéologues de l'Ain, Bourg-en-Bresse, France, (1972), no. 86, 77-82.
- "Le cadran aux étoiles", Orion, (Schaffhouse, Suisse), 30(1972), 171-175.
- "Un cadran solaire de hauteur", Sefunim IV, Bulletin 1972-1975, (Haifa), 60-63.
- "Le cadran solaire de la mosquée Umayyade à Damas", Centaurus, 16 (1972), 285-298, reproduit dans E. S. Kennedy, and I. Ghanem, eds., The Life and Work of Ibn al-Shiper: an Arab Astronomer of the Fourteenth Century, (Alep: Institute for the History of Arabic Science, 1976), pp. 107-121.

1973

"Le monument solaire de Bagneux", Histoire Archéologique, Bulletin de l'Association des Amis de Bagneux, (Bagneux, France), 1973, 521-529.

1974

- "Le cadran solaire multiface de l'Abbaye Sainte-Croix de Bordeaux", Revus Historique de Bordeaux et du département de la Gironde, (France), 1974, 31-41.
- "Le cadran solaire analématique, histoire et développement", Centre Technique de l'Industrie Horlogère, (Besançon, France), no. 74. 2057, 1974, 1-37. Il existe une traduction allemande due à René R. J. Rohr parue dans Uhren Technik (U. T.), 2 (1974), 1-15.
- "Le cadran lunaire", Orion, (Schaffhouse, Suisse), 32(1974), 3-11.

1975

"Un cadran solaire oublié", Orion, (Schaffhouse, Suisse), 33(1975), 179-182.

Éloge

LOUIS JANIN



17 OCTOBRE, 1897 - 29 DÉCEMBRE, 1978

Par C. Nallet*, René R. J. Rohr, et D. A. King

DIPLOMÉ des Hautes Etudes Commerciales, Docteur en Droit, M. Louis Janin a fait toute sa carrière dans le commerce international en tant que Directeur d'une grande banque parisienne. Il a cu six enfants, dix-huit petits-enfants et de nombreux amis.

Au cours de sa vie professionnelle, M. Louis Janin a travaillé en Algérie et a eu de nombreux contacts avec les pays arabes.

Ce n'est qu'après avoir pris sa retraite, en 1965, à l'âge de 68 ans, qu'il s'est intéressé à la gnomonique, et c'est à partir de cette date là qu'il lui a consacré son temps et ses efforts. Son intérêt pour la gnomonique arabe remonte à sa découverte de l'absence de publication sur le splendide cadrau de la Mosquée Omayyade à Damas. Par la suite, il a visité le Caire pour examiner tous les cadrans médiévaux que l'on peut y trouver, et il y a appris que le plus splendide de ceux que l'on connaît était celui de la Mosquée d'Ibn Tülün qui n'existe plus que dans une reproduction fidèle préparée par les savants qui accompagnaient Bonaparte en Egypte. Une de ses publications les plus récentes traite d'un cadran extraordinaire, d'origine grecque, qui a été découvert en Afghanis-

^{*12,} evenue Carnot, 75017 Paris, France.

primarily of doctrinal responses; and when philosophy became focused upon illuminationist metaphysics, the desirability of natural philosophy and the mathematical sciences of nature was seriously reduced. But Avicenna's thought, as the foremost exemplar of falsafa, would also have played the leading part on the side of the ancient disciplines in the general 'religious dialogue' that I have posited. If the description is essentially correct this far, then one may affirm with confidence that Ibn Sina's theoretical psychology exercised a decisive influence upon the history of the Greek sciences and upon the evolution of Islamic cultural history in general. This is the conclusion that I have been the most anxious to substantiate; but even in a longish paper adequate support can be produced for only a part of the necessary argument. I hope, though, that I have treated primarily those points which have most significance for the broader issues.

Let me add a final observation. If this historical assessment has been an accurate one, then the career of philosophy and of all the Greek sciences was pressed forward in the very centre of Muslim culture, not at the periphery as is often supposed. Indeed philosophy and her sister disciplines will need to be regarded as having developed in ways and by processes which were common to most fields of intellectual endeavour in the Islamic middle ages and which seem to have been among the most characteristic and important features of Muslim civilization.

^{45.} All the natural sciences were burned in this way, including psychology itself. But psychological theory escaped to a considerable extent, because it was able to direct its inquiries towards the ontology of intellects and related subjects; having thus been itself transformed, it came to occupy a positive midway between 'physics' and metaphysics.

of the acquisition of knowledge which left him in exactly the moderate illuminationist posture he wanted. The analysis of 'experience' (tapriba) in the Burhān was a crucial step in securing his epistemological doctrines. Tapriba could be useful, but it had a strictly limited rôle, and there was no instance in which it could not, in the end, be avoided. 'Experience' belonged to the estimative faculty, 'knowledge' to the intellect; and the active principle of intellection resided in a celestial being. Avicence's establishing of this external-intellection theory of knowledge was what was most decisive, I have argued, in determining the subsequent relationship of the Greek sciences and their proponents to the followers of the other ways of Muslim knowledge.

Ibn Sina's attitude to empirical knowledge I have mainly attributed to so ultimately Muslim belief in personal salvation. To this, too, I have credited his interpretation of the ensoulment of the human embryo presented in the Kitab al-Hayauan. Finally, since paradise was to offer eternal intellection as its highest reward, it was in this connection also that the chief ontological problems were generated. Avicenna took various measures to reconcile actual intellection with incorporeal individualization, but he had no real success.

The discussions in this paper were designed to show how very much of the philosophy of Ibn Sinā was connected to his psychology and how crucially his system depended upon the elaboration of a consistent general theory of the soul. In the Islamic intellectual world of the late math, tenth, and early eleventh centuries, moreover, it is correct to say that a very large proportion of the leading issues lay within psychological theory or derived immediately from doctrines there - an assertion for which my earlier list will have to provide a sufficient prima facie case. In passing, without proof, I have offered an analysis of the development of Islamic intellectual culture wherein the fundamental process is seen as a 'dialogue' among the several groupings of Muslim thinkers, one of which comprised the falāsifa and other adherents of the Greek sciences. Conceived here as basically a religious debate, it had as its underlying question the sort of "ilm that was to be accepted as true and was thus to supply the proper understanding of the religion. The full examination of tajriba and related matters above was intended in part to clarify this picture of a general debate and to present a notable example of what I conclude was involved in it. If this interpretation represents the historical situation properly, then the further statement may be made, that through the medium of this 'dialogue' psychological theory exerted a major force in the final shaping of medieval Islamic culture.

Probably no one doubts that Ibn Sina was a key figure in the history of Muslim thought. The real task is to learn by what means Avicenna's philosophy came to change the course of the Greek sciences in Islam and thus to alter the development of Muslim culture as a whole. A tentative answer is now available. The transformation in falsafa itself was relatively direct, a matter

But if Ibn Sinā was not mystical in his outlook, neither was he empirical. He had arrived at a position where he hoped to have the best of both worlds. The practical result, in fact, was almost to gain neither. The salvaging of his philosophy did not begin until two centuries later, and then only in the Iranian schools; there it was made something wholly mystical, with logic and the sciences as pure propaedeutic.

Avicenna's illuminationism rendered tajriba superfluous and left falsofa impotent to serve as a basis for the progressive investigation of nature. The epistemological foundation of philosophy was made exactly the same as that of the traditional religious sciences in Avicenna's system, viz., revelation from the Active Intellect; but of course philosophy could be given neither the direct authority of a God-sent Message nor the social support available to the Qur'anic disciplines or even to katim. Yet the illumination accessible to the philosopher had little of the bliss and ecstasy of the union with God claimed by the soft's. Without saving the sciences of nature, without gaining the felicity of the mystics, and without capturing any of the social might or religious authority of the jurists or even the lesser strength of the theologians, Ibn Sīnā failed his side badly in the general Islamic cultural debate over the nature of proper Muslim 'ilm.

His was, to be sure, an extraordinarily difficult task, and one cannot deny the brilliance, or at the very least the thoroughness and competence, of the philosophical synthesis achieved by Avicenna. He provided solutions to the primary, psychological problems with which he had been faced, even if he left unauswered a set of derivative questions in ontology. Using an exceptionally oblique method of presentation Ibn Sīnā produced a non-Aristotelian account

esp. to the notes), pp. 129-131, and ch. 5 (pp 145-196; published separately as La Connessance mystique..., also cited in note 34). Gardet and Massignon bad viewed Avicenus's system as ultimately 'mystical', whether Platinian or sife; but in the next year appeared Shlomo Pines's 'La "Philosophis orientale" d'Avicenne et se polémique contre les Bagdadens', Archives d'histoire dictivitale si litissus du moyen-dge, 27 (1952), 5-37, which found Avicennanism to be an esoteric Peripateticism of essentially the sort that has been described in this paper. A rejounder came from Henry Corlim, in his Account et le récit visionnoire (2d ed., Paris, 1954), Eng. tr. by W. Trask as Avicenna and the Visionary Recital (New York, 1960), pp. 271-278, there he examined both the article by Pines and one by Massignon ('La Philosophie orientale d'Ilai Sinà et son alphabet philosophique', pp. 1-18 in Mémorial Auccome, 1971 Miscellanen (Cairo, 1954)) before pressing an aven more mystical resding than that of Massignon Pines's 'La Conception de la conscience de soi . . . ' (see note 34 above) is also pertinent here; and cf., finally, Louis Gardet and M. Anawati, Mystique Musulmone (2d ed., Paris, 1960), passim.

The present paper has relevance to the problem of mysticiam in Ibu Sinā only if Pines's side of the argument is largely correct. I am gratified in this respect by the support received from the conclusions of the careful avestigator of Ah-Rissid al-Adhamiyya, Francesca Lucchetta, who in her introduction to that work (ed. cit., note 4 above, pp. Iv-Ivi) says abe has found no evidence for imide of any kind, for itsial with entities other than the Active Intellect, or for direct contemplation, intellectual or otherwise, of the One. Avicanna's philosophy seems to have held within it only that modurate illuminationism of an intellective kind which has been presented above.

But such knowledge is still intelligible, not more, and is logically – syllogistically – ordered, although all interrelationships among the intelligibles are known at the same time. I have not found any passage in the Shifa', nor in the Ishārāt the Adhawiyya, nor elsewhere, that suggests the least possibility that a human soul or intellect, in this life or the next, may become conjoined to a being higher than the lowest of the celestial intellects, or, in other words, that it may participate in any knowledge or mode of being higher than that of the Active Intellect. Ibn Sinā's whole cosmological system demonstrates, and is in part designed in order to demonstrate, the impossibility of the uniting or conjoining with the One by any finite being, even the highest celestial intellect. Moreover, far from proving mystical fanā' (extinction of self) in the state of 'conjunction', Avicenna commits his efforts to preserving individual identity there.

One may talk of more than one sort of spiritual union: the mystic may say 'I am God', in which case there is ittihād ('unification') unqualified, and the identity of the mystic has been lost in that of God himself (or of the One); or he may claim that he is within or joined to God, a qualified ittihād, wherein his identity is retained; a thinker of Avicenna's persuasions, however, may only assert that he is within or joined to a celestial intellect, where his condition is the intellective ittisāl that has been discussed. This state is nothing like the 'light' (nūr) or the 'tasting' (dhawq) described by the sifi's nor the kind of union with the One that Plotinus claimed to achieve. In the Ishārāt and other places Ihn Sīnā makes use of the language of the sūfi's; but it is not their doctrines he proceeds to expound. So, although he is unquestionably an illuminationist in a certain precisely restricted sense. Avicenna cannot be considered a mystic of either a sūfi or a Plotinian kind. Nor, it seems to me, can be be termed a mystic in any other significant way.

pp. 190-209 and 214-215, ed. cit. in note 4.

The notion of eternal, or prophetic, intellection as timeless, or simultaneous, syllogizing is reasonably clearly expressed in the Kitāb al-Nafa passage (Eng. tr., p. 36 in Aucenna's Psychology, cited above is note 10, in the Arabic text of the Najdi, p. 167, ed. cit in the same note); timeless syllogizing seems also to be the petivity that Aristotle attributed to the Prime Mover at the end of Metaphysics XII. 9.

^{45.} Avicenna's cosmology is fully expanded in the Shifa', See al-lithiyyöt Vill 7 aut IX. 2, 3, and 4, esp. (X: 3 and 4, ef. Nast, Introduction... (cited in note 35 above), pp. 202-207 - but use this account with care, for much of it is based on a raidio that is almost serteinly apurious.

^{44.} Ibn Sinà's 'mysticism' and the associated issue of his 'restance philosophy' have been taken up by nearly every Avicancian scholar active same World War II, and for good reason, as the solutions to these problems must form a fundamental part of any general interpretation of Avicanna's thought. I shall mention here only enough writings to furnish the basic information and make clear the main potots of view. The state of opinion at the end of 1950 was compactly exhibited in the special issue of La Revas du Caire for June, 1951, which had articles on the subject by Louis Massignon and (two) by Louis Cardet, plus two more on related topics by Ahmad Fu'id al-Ahwa'ol and M.M. (G. C.) Answati, Gardet's views were more fully explained in his La Pensés religieuse. (vited in note 34 above) published the same year; see pp. 23-29 (which follows the text of the first. Cairo article. but with additions.

a potential intellect, how can it be genuinely a component of the soul, which ought to subsist at a different outological level? If, again, it really is an intellect, how can it have been individuated for a given matter (i.e., its body) in the first place? Why should the rational soul (whether truly soul or truly intellect) be supposed able to return to the dator formarum as something self-subsistent when it has left it fit only to be joined in a necessary connexion to one particular body? What, principally and finally, is a 'soul' doing in a celestial intellect qua soul, or, if it is there as an intellectual entity, how can it have retained its individuality? Ibn Sina by no means avoids these questions, but he does not answer them cogently. He seems to exploit the intrinsic ambiguity of designations such as 'rational soul' and 'individual intellect', using them equivocally in senses that are in fact incompatible.

This is but one place, although a principal one, to be sure, where the philosophical structure erected by Ibn Sinā reveals large cracks in its fabric. The source of many of them lies in psychological theory, as has already been said, but of these, most emerge to view only as flaws in his ontology. The outological problems that are created by basic psychological doctrines like the external-intellection theory of 'ilm often may be traced further back, to the basic Muslim belief in individual immortality, in particular. Many of the difficulties in the outology of Avicenna he himself fails to isolate, and not a few he covers over; they remain largely unsolved. Like the intricate Christological enigmas of Patristic theology they are most obvious in what may be called, rather pedantically, outological anthropology. These faults in the ontology of Ibn Sina must be rapked among the intrinsically most damaging in his entire system; some of them, moreover, relate to doctrines meant to replace traditionally interpreted Our'anic dogmas. It is not surprising that the ontological failings as a group become particularly injurious to the reputation of Avicenna's philosophy in the Islamic world.

Since relevant information is now to hand, it is perhaps excusable to turn briefly aside to the issue of Ibn Sinā's mysticism. Certainly it is the teaching of Avicenna that authentic knowledge comes to the human mind only through conjunction (itijāl) with a celestial intellect. Prophets, and some others, at least in their moments of greatest insight, grasp the whole or most of the intelligible world of the Active Intellect simultaneously; and continuous, or rather timeless, existence in this condition of complete understanding is the highest felicity in Avicenna's paradise. This state of being is an immaterial and eternal possession of conscious, self-aware, and necessarily actual knowledge of the sort just described.

^{42.} The main theoretical treatments of the higher human intellectual (or psychical) states are At-Shifa'. Kitâb al-Nafs. V 6, esp. pp. 249-250, ed. cit in note 8 above, and al-Hāhnyyāt IX-7, pp. 425-426 and 429 (in vol. II), ed. cit. in note 13, and At-Risála al-Adhamyya, ch. 7, passam, usp.

individuation and has indeed evolved the fundamentals of an ego-doctrine. His 'ego', I believe, may be described by the formula 'individual rational soul' = 'intellect' + 'ego'; that is to say, the rational soul comprises an intellective faculty and an unanalysed immaterial principle of individuation, which may be called an 'ego' (literally, and in the standard philosophical sense, if not precisely in any of the technical meanings of the term in modern psychology). It also seems that the potential intellect, in the narrowest sense, does, when actualized, become identical to the intelligibles which the rational soul is 'borrowing'. But even so little as this is never made explicit. Some negative conclusions may be confidently drawn, however: that there is little real influence here from the Plotinian 'we', or the Stoic 'attention', and none from an 'attentive' (prosektikon) faculty (even though it was conceived as a part of the rational soul) of the logically abominable type adopted by John Philoponus (Yahyā al-Naḥwī; ca. 490 - ca. 570).

Avicenna, as I mentioned above, is aware of his failure in the Shifā' to cope fully with the individualizing of a 'resurrected' intellect. But the treatment in Al-Risala al-Adhawiyya goes little further; the discussion may be 'esoteric', but it is scarcely more 'demonstrative' than that in the Shifā'.' In the Adhawiyya the carrier of human individuality is considered to be the rational soul, which also is the element of a person that is saved at his death. How, though, is it to retain its intellective capacity, to become, indeed, an eternal intellect-in-act? If the rational soul or any essential 'part' of it is really

³⁹ Rahman's well-known views on Ihn Sînâ's ides of the 'ego', expressed in Artenna's Psychology (sted in note 10 above), pp. 12-19, 102-104, and 109-114, were necessarily tentative, for he was speaking there only in relation to Ihn Sînâ's remarks in ch. 15 of the psychological part of the Najâ (Eng. tr., pp. 64-68 in the same work, pp. 189-192 in the Arabic text, ed. vit. above in note 10). In this place Avicenna marely sudicates that the ultimate substrate of experience is in one sense the soul as a whole. The more developed doctrine of the 'ego' is found in the Shījā', Kitāb al Najā V· 7, ed. Rahman (cited in note 8 above), pp. 256-257, see especially p. 250, ll. 9-11, a passage that follows upon the analysis of the 'Boating man' (see preceding note). 'The referent (magnāt: 'object referred to') in the knowledge I have about myself, that I am the "I" whom I mean in my saying that I have seemed [something] and that I have performed [some] act and that I combine these characteristics [within myself], in another thing, which is what I call the "I" (and).'

Of also note 34 above, are especially the Shifit, al-Hillary at 111 8 and VIII. 6 (for harkground), el-Risillo al-Adhamyya, ch. 4, and Pines, 'La conception de la conscience de soi ', among the references there.

^{40.} Rahman, Auczenna's Psychology (cited in note 10 above), pp. 111-114, presents an English translation of Philoponus's remarks on the 'attentive faculty', of Inhannes Philoponus, In Arssistelis He Anima librar commentaria [Commentaria in Aristotelem Gracca, XV], ed. M. Hayduck (Berlin, 1897), p. 464, 11, 12 et seq. (on De An. 11; 2, 425b125).

^{41.} See above, p. 74 and note 34. The seeming best ancy of Ibn Suñ over his doctrines of individuation of immaterial things appears in the Shift in Kitab al-Nafs V 3 and al-Hahiyyāt IX 7 and N I, in al-Hahiyyāt X: 1 (and to some extent in IX 7) his dubiety is due at least in part to a desire to keep the discussion exoteric (with, of course, hints to the wise), but in the Kitab al-Nafs the doubt seems whally unfeigned.

reduces to ontology. The problem of knowledge comes to be examined mainly through discussion of the ontological status of intelligibles and intellects. And to this same topic the study of the higher functions of the soul leads also at the sud.

The ideas of the 'essential definition' (hadd) (cf. note 13), the species, and the genus are treated the most interestingly not in the logical books of the Shif's' but in the Hähiyyät: for it is their mode of being that is principally at issue, and this is an outological matter. Avicenna's rejection of Platonic Ideas on ontological grounds has already been noted; the ontological content of the problem of intelligible memory, too, will have been evident. Finally, it is in ontology where the problems of psychological theory as such, having been averted earlier, now reappear to do battle.

How can a rational soul be said really to become an eternal intellect-in-act? Would this not require a change from one hypostasis into another, a change of a single subject from one level of being to an entirely distinct one? And would not such a change be cuttrely inexplicable in anything like Avicentian concepts? It is true that Ibn Sinā speaks of a child as entering a different species upon gaining its capacity for intellection, but this is simply a case, although a peculiar one, in which a properly prepared matter receives an entelectry that is common to all members of its (new) species. (Scholars who seek to make Avicenna Plotinian must be especially careful on these matters: he never speaks of an individual 'undescended' intellect, and the realization of a rational soul as an eternal intellect-in-act, however grotesquely it may distort Peripatetic views, is simply inconceivable in the cosmology of the Ennsads).

The rational soul qua individual is not an intellect, whereas qua intellectin-act it cannot be individual. Is the rational soul of a person, however, supposed to be identical with his intellect, and is this in turn to be identical with
the intelligibles it receives? If so, there are grave problems here, surely insuperable ones. But in fact, as has been remarked above, Ibn Sīnā often speaks
as though the potential intellect is merely a capacity for intellection inhering
in something non-passive, namely the rational soul, which in one aspect is
the hispanonikon, the 'controlling faculty', of the individual. One should note
also the self-awareness that Ibn Sīnā attributes even to the so-called 'floating
man' (i.s., someone conceived as deprived of all sensory information whatever). Thus be has binted in several places at an immaterial principle of

^{37.} Shifa', Cairo ad , al-Hayanda XVI. 1, p. 403, 11. 7-8. 'If a child (yably, lit., 'hoy') [duly] andowed with sensation (hasda an, becomes [fally] human (insta an, through reason (nusq == Gk. logos), be progresses by this perfection (istikudi, 'satelechy') from one species (nuse') to another'. (Because, according to Peripatetic philosophy 'man' is the 'rational (nusqi) animal', differentiated from all other species by his reason). The present passage is part of a longer one discussed above (p. 52) in connection with the ensouling of the embryo.

^{38.} Kitáb al-Nufs, 1: 1, ed. cit in note B above, p. 16, and V. 7, ibid., pp. 255-256; also, differently expressed, in the Ishardi (Le Livre des théorèmes et des avertissements, ed. J. Forget (Leiden, 1892), p. 119).

Whatever the reasons and motivations of Avicenna, and whatever the nature of his mystical tendencies, his theory of the acquisition of knowledge through 'conjunction' with the Active Intellect thoroughly undernance natural philosophy and the sciences, for his solid and integrated account effectively obviates empirical investigation. The examination of tarriba in the Shift' may well be intended to save the disciplines traditionally based on experience -Avicenna's own intellectual biography very strongly suggests as much; but the epistemology developed by Ibn Sina moves so far in the opposite direction as to become a form of illuminationism. One cannot avoid the impression that the hardships of tajriba are really for the intellectually unlucky. Individual immortality has been sayed, but empirical research has been made superfluous. at least in essence. Direct intellectual insight can be effective anywhere that toiribe can be but is also able to go further and deeper. Avicenna will rightly be understood as saving. Logic and mathematics supply good mental training: noetics, epistemology, and outology are important for their actual content The rest of the Greek theoretical disciplines, especially natural philosophy and the mixed sciences, have a lesser value and are perhaps triffing to the best minds. Such is the eventual significance of Ibn Sina's treatment of emperria for the Greek way of knowledge in the Islamic world. There are strong intellectual and social forces against which the falasifa are obliged to make themselves felt, but Avicenna's philosophy turns too much towards illuminationism, and keeps too httle of Peripateticism to provide a healthy environment for science. This is the cost that the successors of Ibn Sina in falsafa and the natural and mathematical sciences will have to meet in order to pay for his success in constructing a system of logic, biology, and metaphysics that gains its coherence through these distinctive theories in psychology.

There is also a price that is exacted within Ibn Sinā's own philosophy for this triumph. The various problems of his noetic, both psychological and spistemological, have largely been solved; but the solutions that have been teached create further difficulties. The new complications cluster together in the area of ontology. They are taken up in the Shifā', then, in the Ildhvyydt (mesning, '[science of] things divine', but of course equivalent in meaning to 'metaphysics'), not in the Kutāb al-Nafs, which is a physical investigation of the soul, nor in the Burhān, the mainly opistemological work placed, however, in the logic jumla.

Ibn Sina's psychology in general has a tendency to merge into metaphysics. 'How do we think?' and 'how do we know?' are primary questions in his psychological enquiries, and they clearly presuppose the basic epistemological inquiry into the nature of knowledge. But the connection to metaphysics is much more intimate than that, for Avicenna's epistemology in turn largely

CAuceans [Mémorial Avicenae, III] (Cairo, 1952) or W. E. Gohlman, ed., The Life of Ibn Sind (Albany, NY., 1974).

I have not meant to imply that Ibn Sina has no other motives in adopting his intellective theory of 'ilm than to save individual salvation, although I have maintained that this is much the weightiest one. But there are indeed further advantages to his account of the external active principle of human intellection. For one thing, all the benefits of a pure, Platonic epistemology are preserved without having the Ideas themselves self-subsistent, which was surely something outologically objectionable (see Shifa', Hāhiyyāt, VII: 3. and the prelimmaries in III: 8; al-Fărăbi has already made these pointal: the Ideas become the conscious contents of the more credibly self-subsistent celestral intellects (which were posited even by Aristotle; see especially Metaphysics XII: 8). Furthermore, intelligibles are necessarily immaterial and cannot be retained in a corporcal medium. (What, Avicenna asks, would half a spatially extended abstract man be?) The Active Intellect, however, provides a suitable storehouse from which they can be borrowed conveniently; otherwise, intelligibles would actually have to be abstracted anew each time from remembered images or intentiones. The solution of the problem of intellectual memory must be one of Ibn Sina's chief grounds of a purely philosophical sort for making the active principle of abstract human knowledge something external.

Finally, the intellection theory of Avicenna allows a quasi-mysticism to be present in his philosophy, and he lives in a period when mystical thought is beginning to pervade Islamic cultural life. Talk of separated intellects and abstract contemplation will help to attract followers and will make the introduction of neophytes to his thought easier to accomplish. It is also very likely that Ibn Sīnā himself finds this aspect of his philosophy satisfying. Certainly he believes it, for he says that he prays (intellectually) for middle terms. It is probable even that he views what I have just called his 'quasi-mysticism' as the only legitimate mysticism. In any event, it comes to be regarded by others as an altogether essential feature of his system.³⁴

Syed Hason Burani in 'Ibn Sins and Alberani. A Study in Similarities and Contrasts', Aucenna Commemoration Folume [A H 376-A.H 1370] (Calentta, Iran Society, 1956)). I find the tone authoritie.

The poem is also quoted by Seyyed Hassein that in An Introduction to Islamic Cosmological Decirines (Cambridge, Mess., 1964), p. 183, and again in his Three Muslim Sages (Cambridge, Mess., 1964), p. 41, each time in a discussion of Ibn Sind and Islami, either will provide an interesting preliminary account

36. In a positive same, by the Iranian philosophers beginning with Nagir al-Din al-Tusi and his nee-Avicentianism in the mid-thirteenth century, and culminating with Mulla Sadrá (5adr al-11th al-Shiraxi, ca. 1573-1640) and his synthesis of Jim Sinā's philosophy and the theoretically developed suffers of Mulyi nl-Din Ibn 'Arabi (1165-1240). On the modern controversy over Avicenta's mysticina see below.

Ibn Sinā menticos praying for middle terms in his antobiography, and his ideas on the nature of prayer are expressed compendiously so the cessay 'On Prayer', both are conveniently accessible in English in A. J. Arberry, tr., Automa on Theology (London, 1951). There is no critical Arabic text for the Riadiat al-Şaldı, but for the antobiography see A. F. al-Abwani, ed., Aperça sur la biographic

Avicenna's doctrine of individual salvation, although far removed from Qur'ance teachings, is in the end a conviction that springs from religious rather than philosophical motives. Responsibility for his ideas lies here with his thoroughly (if not always stringently) Muslim surroundings, not with his reading of the philosophers.

The examples from embryology and epistemology considered in this paper attest the fundamental importance of personal immortality to Avicenna's philosophy. They should help to confirm my introductory remarks concerning the dialogue in medieval Islam between the more traditional groups of religious intellectuals and the Mushm philosophers. I trust they will also begin to show why it may be asserted that these philosophers, even Ibn Sinā, who is more difficult to analyse than some, consider their thought not merely to be acceptably Muslim but to be the one true interpretation of their religion. 36

4 above). The Najäi offers nothing of real interest, except where it repeats the Shifa', but a hit may be gleaned from Rahman, tr., op est in note 10 above, the 11 and 12, passim (= pp. 182-184 of the Arabic text, ed. est in the same note).

Certain modern studies may also be consulted. Lome Gardet, La pensie religieuse d'Aucenne (Ibn Sinā, (Paris, 1951), pp. 88-94 and 98 195 in ch. 3, pp. 129-131 in cp. 4, and .45-183, passim, in ch. 5, when, La commissance mystique che: Ibn Sinā et ses prosuppuses philosophiques [= Memoriel Articenne, II] (Caro, 1952), which is a preliminary version of ch. 5 of the proceeding, but with certain passages in Arabie included in the noise = pp. 7-49, Shlome Pines, 'La Conception de la conscience de soi ches Avicenne et ches Aba'l-Barakāt al-Barbdād.', Archives d'histoire doctrinale et littéraire du moyen-âge, 20-2. (1953-54), pp. 20-99, one of the few really excellent studies on any aspect of Ibn Sinà's thought; and Francesca Lucchetta, 'Introduzione' to the Adhavitya, ed ett in noise 4 above.

Cf. also note 39 below. It should be pointed out that the Adharmy a presents doctrines that are consistent with what the sophisticated reader of the Shift, would expect, hodily resurrection is dropped, individual solvation is kept, and utihad is still rejected—there is only intellectual contemplation-in-act of the One as duly 'reflected'.

The aspects of ma²dd that relate to moral purification are not taken up in this paper, nor is the question of the original individualization of the rational soul for its body considered (but it should be noted that this is done on the basis of the material attributes of the embryo), although both topics are important and are treated in both the Shifd' and the Adkannyya.

As regards the traditional Peripatetic doctrines in this area of ontology, it must be said that Assistate nowhers provided an adequate examination of the 'governing' part (or aspect) of the soul, or gave a focused analysis of the relationship of the rational soul to the intellector of the intellect to the intellector. For the Amstotchian view that a noise as such is identical to its noise, see, passin, De in. III. 4, 5, and 7, and Mass, XII. 7 and 9.

35. Virtually all the foldsifa (a notable exception being Muhammad shi Zakariyyà al-Rāsī, Lat. Rhases, ca. 854 - ca. 930) feel their philosophy and their religion to express the same Trath; a more fracise statement than this, however, would require lengthy elaboration. Many of the consequences of that helief are expressed in their political philosophics, on which see, first, the Islamic part of Ralph Lerner and Muham Mahdi, eds. Medicual Political Philosophy A Sourcebook (New York, 963). The rolle of Islam in the life and thought of the Sinā is peculiarly hard to assess, not least because of his ability to be 'all things to all people' Louis Gardet in La pensie religiouse d' fraccine (cited in the proceding note) has devoted a book essentially to this subject, for his conclusions see esp. pp. 201-200-

There is a Persian poem attributed to 1bi. Sinh that ends, "I am the unique person in the whole world and if I am a heretic/Then there is not a single Muslim anywhere in the world' (Englished by

which enters the embryo, and the 'acquired intellect') are necessary in the philosophy of Ibn Sina in order to explain personal intellectual immortality. Many of the contortions in Avicenna's psychology, his metaphysics, and even his biology are in fact introduced to this same end.

The Sina claims that the 'saved' human intellect remains individual in its eternal state of 'conjunction'. The only possible way for him to justify this assertion philosophically is to elaborate his conceptions of the rational soul and of the passive intellect. The two seem to me to be effectively identical, but let me for the moment call the entity which reduces 'resurrection' and immortality the 'rational soul' and let the passive intellect be simply the capacity for intellection which is attached to it. The rational soul, first of all, is very 'active' in certain respects, even if its most important function is to be conscious of the intelligibles of which it is receptive qua intellect; it serves the same purpose, indeed, as the hegomonikon of Aristotle (and in this rôle is less ambivalently described than was Aristotle's 'governing power'). The Avicenman notion of the 'ego' is closely connected with the idea of the individual rational soul (which in essence has the logically difficult attribute of being an individuated intellect). Unlike Aristotle's nous, the rational soul of Avicenna has the faculty of receiving or sharing, but not simply of becoming, the intelligibles; the human faol, when Avicenna means by it, as he very often does, either the rational soul or at least something more than a pure intellective faculty, never is identical to its macquilât. The preserving of the identity of the 'resurrected' rational soul cum intellect is a major requirement of his authentic teachings on salvation and not (in contrast with his remarks in the Hahry at of the Shifa' on the miraculous resurrection of the body) a view put forward for the sake of religious expediency. But, in my opinion, Ibn Sinā m able to make only a start on the necessary analysis. He does seem more confident about his doctrines in Al-Risala al-Adhauryya fil-Macad than in the Shifa', and in the Adhawiyya he speaks primarily in terms of the (rational) soul rather than the intellect. Now it is certainly true that the Active Intellect as dator formarum is also the source of the rational soul as the form of the individual human being, and thereby as the form of those other, intelligible forms that he will receive - as Aristotle said, the mind is a 'form of forms' (De Anima III. 8, 432a2). The obvious ontological difficulties are not solved in a demonstrative way, however, in any of Avicenna's writings that I know."

^{54.} On the problems in ontology, and especially the individuation of intellects, the following are among the principal discussions: in the Shifa', al-Hahyydt 111. 8 (on the intellect as substrate for 'quiddities', māhyydt), VIII 6 and IX 5 (beckground), IX 7, and X 3 (eslevant but disappointing), and in the Kudh al-Nafa, V 3 (naticularly), and also V 7, possion - but note Avicenna's warring (p. 238, ed. cii. un note 8 above) that the condition of the soul after death does not belong to the simplect-matter of natural science (but rather to metaphyvics), and in Al-Risála al-Adhomyya (an esoteria but rearcely apodectic work), chs. 1, 4-6, and parts of ch. 7 (pp. 190-209 and 214-223, ed. cii. in note

ported by a general view of Aristotle's ontology and epistemology based upon passages found in De Anima III: 5, Metaphysics II: I and XII: 7 and 9, Nicomachean Ethics X: 7, and elsewhere (not excluding the 'Theology of Aristotle'), as well as in the works of Aristotleian commentators such as Alexander of Aphrodisins and Plotinus (for so he was regarded). Ibn Sīnā beheves that this tradition of thinking, supplemented by various Islamic meights, has the Truth. But for individual tenets within that structure he feels no real need (I am persuaded) for particular textual justifications. Indeed in pressing his own views Avicenna usually finds the specific texts of others simply convenient props or annoying barriers.

Apart from their deviation from the purer Aristotelianism, however, what has been learned of general significance about the doctrines in Book III, chapters 5 and 8, and Book IV, chapter 10, of the Burhan? Tajriba, one has been told, develops through the products of estimation as they are retained with increasing orderliness in the memorative faculty. This 'experience' is 'illuminated' by the Active Intellect in such a way that the corresponding intelligibles are made present to the human potential intellect - which thereupon becomes an intellect-in-act, the 'agl mustafied or 'acquired intellect'.

The careful noetic built up in the Kitāb al-Nafs is consistent with the last of the accounts in the Burhōn, which indeed smoothes the way for it. The essence of Avicenna's explanation when it has finally been consolidated is simple: through the workings of sensation and imagination and the formation, ultimately, of 'experience', the grasping of true, intelligible knowledge 'from without' is occasioned; but this knowledge can be conserved only in the separate Active Intellect, and whenever an individual person shares in these intelligibles his intellectual faculty must be conjoined to the higher intelligence. The absolutely intellectual and incorporeal nature of human knowledge has thus been upheld, while a rôle in acquiring knowledge has nevertheless been found for man's sensory faculties.

The main consequence of keeping true cognition independent of things hodily, as Ibn Sin intends it, is the possibility of immortality for the individual intellect. It is his belief, already examined briefly above, that a person's soul eventually can reach a point where it no longer depends at all upon corporeal faculties in attaining the intelligibles, but is in fact prevented by the body from prolonging its periods of intellectual contemplation. This independence is to be achieved by constantly actualizing the rational faculty as an intellect – through 'conjunction', and in most cases, at least at first, from a basis of 'experience'. To a soul thus elevated the death of the body is to come as a release that will allow it to enter the supremely happy condition of eternal intellection.

The rejection of purely empirical theories of knowledge and the postulating within each human being of two entities from above (the rational soul itself,

(6) involve direct intellectual tastiq. Tajrība enters explicitly into (5), but also, implicitly by way of tasticular, into (2) and (3). It scarcely need be added that in every case the unexpressed phrase 'from the Active Intellect' is to be understood after the verb 'receive' or its equivalent.

Much has thus been said about 'experience' by Ibn Sina in those chapters of the Burhan But however helpful tairiba may be, in the end it does nothing that is absolutely essential. This conclusion is already implied clearly enough. except in one case; but it holds, as one learns elsewhere, even for tardio in respect of propositions like 'scammony purges yellow bile'. Tajriba cannot serve as a proper originative source for "ilm. Here in Avicenna's system with regard to the acquisition of knowledge through experience, even more than earlier on with regard to the ensoulment of the human embryo, there ts a lesson to be drawn concerning Ibn Sina's attitude to Aristotle. The greater part of the Shifa', as was said above, follows the standard arrangement of the Aristotelian corpus. Yet within this minutely structured framework of topics, Avicenna is his own man: it is the questions and not their treatment that are routinely taken over. Ibn Sinā philosophizes in a well-defined tradition, but departs from his predecessors, from Aristotle himself, not merely in details but in major doctrines. In the accounts of tairiba that have just been examined, the First Teacher's opinions are first twisted, then ignored. The radical dichotomy between the sensible and intelligible worlds is stoutly maintained. Regardless of his esteem for Aristotle, Avicenna refuses to allow the senses or anything that is at all corporeal to create genuine, intellectual comprehension. Despite the soothing words of the preliminary discussion in III: 5, empeiria/ ingriba is allowed only to lead towards, not actually to produce authentic knowledge. Notions from 'experience' cannot have any actual connection with abstractions proper. In some instances 'experience' may become a necessary cause of the acquisition of intelligibles; but it is never, as it was for Aristotle in the Posterior Analytics, the stuff out of which true knowledge is refined, the actual origin of the arts and sciences, which is continuous with them. The real source of 'tilm as conceived by Ihn Sina is something entirely different, the intelligibles subsistent in act in an eternal higher intellect. Although not at all an unprecedented rewording of Aristotle, in the context of the [Kuib] al-Burhan this is a boldly consistent one. The empirical theory of knowledge is effectively destroyed in a chapter that protends to save it! The rational soul, which comes to the embryo 'from without', does indeed require that second entity 'from without' to make it think; only with the 'acquired intellect' is it really rational.

The un-Aristotelian treatment of the Aristotelian topics is itself very coherent, as the reader of Avicenna gradually discovers. Not that Ibn Sina would regard his own philosophy as anti-Peripatetic; quite the contrary. The liberties taken with Posterior Analytics II: 19 and Metaphysics II: 1 may be sup-

in IV: 10 one does not possess an integral, esoteric presentation of the theory of how the human mind obtains knowledge (although Ibn Sinā goes well beyond the professed goal of the chapter, which is only to describe the acquisition of primary premisses). What one does have is an accurate delineation of the main tenets.

Reflection on the whole of Ibn Sina's handling of the acquisition of knowledge in the Burhān leaves the impression that all is not well, even when allowance has been made for the peculiarities of the method of presentation. Inconsistencies remain between the discussions in III: 5 and IV: 10. There is no hint in the earlier account that tajriba may be considered a cognitive state, nor is this a matter which can be corrected by a simple elaboration. Again, there is no indication in III. 5 that 'experience' has a rôle to play in tajawwar, despite the not inconsiderable discussion there of tajawar and the senses. The earlier conceptions of istigra' and of the tajriba that generates 'assent' (tajdiq) to premisses about the physical world (e.g., that 'the lodestone attracts tron') Ibn Sinā does not revise, and the necessary modifications are left implicit. Nor, as was said, does he carry out a frank examination of the necessity of the sensory and 'estimative' preparations for intellection that he has described.

There is a further, more general shortcoming. Avicenna's analysis really amounts to little more than a mere exhausting of logical possibilities, for he pays scant attention to conditions which actually may determine the occurrence of the processes that he has identified. (This of course is also an obvious flaw in Aristotle.) Especially to be noted is the case of taidiq with regard to composite universals, where it is unclear which of the two possible routes is to be followed in any particular instance – whether sensory (including 'estimative') combination of 'images' is to give rise to taidious of the compound intelligible, which is then subject to taidiq; or whether sensory processes are to lead to taignour of incomposite intelligibles, which are afterwards combined intellectually into the compound intelligible.

From the material that Avicenna does present, however, one is able to extract a list of six intellectual processes which he believes operate to acquire 'ilm. The intellect by its nature may, he says: 1) receive unimmattered, incomposite intelligibles; 2) pare the 'images' of immattered forms and grasp the corresponding incomposite intelligibles; 3) receive primary premisses by way of abstraction from compounded 'images'; 4) acquire primary premisses through the combination of two intelligibles which it knows directly by innate disposition (fitra); 5) gain secondary premisses through tapiba and the recognition of certain conjunctions as essential rather than accidental; and 6) obtain derivative premisses (in what Aristotle designated 'epistêmê', in the narrowest sense) by syllogistic combination of intelligibles. Processes (1) and (2) relate solely to tasawour, the rest to both tasawour and tastiq; (4) and

khayd to prevent his statements from seriously misleading the reader. The explanation was not complete, but neither was it actually wrong, he would claim; moreover, he would certainly say that it was the proper and most appropriate way to present the material at that stage in the exposition. After all, to mention only the most difficult point, the intennones are still sensory and bodily as compared with the radically different intelligibles.

The treatment of tajetba and 'ilm in the Kutōb al-Burhōn is not a wayward example; on the contrary, it actually represents Ibu Sinā's regular manner of handling a difficult subject. No more theoretical armament than necessary is brought to bear in a given situation. Hence it is clear that to glean a theory from Ibu Sinā's explanations where it is not the main subject at hand is a very dangerous course indeed, and to find contradictions between such subsidiary accounts is simply illegitimate.

But how can the reader know that in IV: 10 he has come to an essentially complete portrayal of the rôle of experience in the attainment of knowledge? A preliminary answer is that when compared with the presentations in III: 5 and III. 8, at least, this one immediately can be judged preferable simply because it is fuller and fits better with the rest of Avicenna's philosophy. The decisive condition which is met here, however, is that the last account finally reproduces the entire psychological scheme as it appears in the main analysis of the workings of the soul, by which I mean the description of the intellect and its subordinate faculties found in the Kitāb al-Nafs in the physics jumla of the Shifā'. (Conversely, from his knowledge of the Burhān the reader can see immediately that the summary of the functions of injriba in the Kitāb al-Nafs, V: 3, reproduced in chapter 11 of the psychological part of the Najā, provides nothing more than a glimpse of the subject in a special context and should be accorded virtually no weight (see note 10 above).)

The more delicate question arises whether even in the principal discussion of psychological theory certain esotene doctrines are being suppressed. But there must be a discernible motive on the part of Ibn Sinā before the historian may allow himself to entertain that suspicion: for example, that the intended readers of the treatise are insufficiently advanced or religiously too unenlightened to understand Ibn Sinā's real views. In this case no such considerations seem to apply. Therefore, since the treatment of empirical knowledge in Burhān IV: 10 is fully compatible with the system expounded in the rest of the Shifā' and, moreover, in the Ishārāt and elsewhere it should indeed portray his doctrines in a reliable way. This is not to say that one finds here a straightforward, closed, or exhaustive explanation. The actual positions of Avicenna have to be teased out of the text, which superficially aims to 'save' Aristotle's opinions. No overt alterations are made to the assertions in IH: 5, although more than one is implied. The embarrassing but essential question of the necessity of sensory information and of 'experience' is not explored. So even

estimative and retentive faculties is a new, intermediate level of cognitive object, the ma^āni (intentiones). More abstract and analytically powerful than the sensory images even of the cogitative faculty, they are nonetheless corporeal and only quasi-universal; so the ma^āni count ultimately as 'sensible', not 'intelligible'. 'Experience' (tajriba) results from the accumulating and sorting of the ma^āni by the soul. It now transpires, moreover, that mere sensible forms normally need to be refined into intentionss for intellection to occur. Only then are the intelligible species and their relationships clearly enough 'reflected' (if a neo-Platonic term used in the Adhauryyo may be borrowed) that individual human intellects may be stimulated to the grasping of the actual intelligibles. This again accords with the Kitāb al-Nafs (q.v., Bk. 1V, ch. 3).

Let that suffice for 'experience' as it is explained in Burhān: IV:10. A comparison with certain features of what was said on the same subject in Book III will provide a striking illustration of a particularly important characteristic of Avicenna's expository methods. It must be stressed first that 1bn Sînā does not intend to describe a different doctrine of the acquisition of knowledge via experience in Book IV of the Kuāb al-Burhān from what he has done earlier on; he has not changed his theory, nor would he admit to being gravely inconsistent in his presentations – despite the fact that it would be difficult to infer a rôle for combinative imagination from the earlier accounts and impossible to do so for 'estimation'. It is the case, rather, that Avicenna customarily deploys only as much of his full theory as is absolutely requisite for the immediate objective.

His practice in this respect is partly a matter of instructional method and to some degree of mere convenience; it is also a natural correlative of his policy of gradual disclosure (in religiously sensitive or highly abstruse topics) of a fully 'esoteric' doctrine to an increasingly restricted audience of the philosophically élite. Consequently, the works of Avicenna are fraught with difficulties for any one who wishes to learn about his views on some specific subject without studying his system as a whole. For the intellectual historian the most relevant implication is the obvious one, that an understanding of oue of Avicenna's doctrines must always be grounded upon the principal discussion of that teaching (if a full treatment exists) and never upon inferences drawn from a series of passing mentions. (This restriction supplements two others: that one must ignore, for the most part, rhetorical presentations whenever a dialectical or demonstrative one exists, and that one must 'read between the lines' in order to recognize places where esoteric doctrines may be lurking - the latter by no means a particularly difficult feat for a reasonably experienced and unprejudiced student.)

In the case of the empirical acquisition of knowledge, Ibn Sinā in his earlier descriptions has depended upon the latitude of meaning in the terms his and

without intellectual help. (But, Ibn Sinā reminds his readers, what the wahm discerns is one thing, what the intellect grasps is another.) This discrimination is accomplished. Avicenna says, not by sense-perception proper but specifically by estimation. One may infer that the recognition of natural species is in fact an elemental function of 'experience'. 52

Like Aristotle, Ibn Sinā brings his analysis to a balt when he has identified the faculty which acquires abstract and indemonstrable knowledge; any further investigation of the means of knowing belongs elsewhere, that is to say in the study of psychology. In the Posterior Analytics, sensation and its further development ria memory and experience seem to have formed a necessary and sufficient source for all intelligible knowledge; but to Ibn Sinā a sensory foundation is necessary only in certain areas of enquiry (and for some few people not even there), and in no case can it become a sufficient principle for intellection. The incomplete human intellect, in Avicenna's view, always needs external help to possess actual intelligibles. Moreover, the sensory and 'estimative' aids become obstacles to any intellect that has already developed its capacities and come to know its way about in the intelligible world. Things relating to sense are to be discarded as quickly as possible, Ibn Sinā maintains; dependence on corporeal faculties can lead one's soul only to torment in an afterhie where bliss is intellectual.

Tajriba is the final result of sifting and arranging the intentiones, but upon the intentiones the light of the Active Intellect must shine if the mind is to acquire real knowledge. Although still subject to all the detailed qualifications presented before, Avicenna's final doctrine can be summarized quite simply: when something the intellect is supposed to know is displayed before it in suitable 'images', it does know it, in an intelligible way – for that is its peculiar power as an intellect. Of such 'images' the most highly developed and directly stimulating ones are the sorted ma'āni, the ordered intentiones that are held in the retentive faculty and constitute 'experience'. Prepared by 'experience', the soul has become ready for its intellectual faculty to be actualized from without, ready to grasp the intelligibles in actual through conjunction of its individual potential intellect with the eternally actual Active Intellect.

This discussion in Burhan IV: 10 provides the last instalment of Ibu Sina's explanation of 'experience'. Here he correlates the analyses of the earlier chapters with the psychological theories of the Kitāb al-Nafs. The previous treatments are elaborated in such a way as to disclose the parts played in the sensory half of human cognition by two additional 'active' faculties, the combinative imagination (al-mufakkira, the 'cognitative' faculty) and the estimative faculty (wahm), and by the repository for the products of the wahm, the retentive or memorative faculty (al-hāfiza, al-dhākira). Associated with the

Under the influence of Aristotle's exposition in Posterior Analytics II: 19 (esp. 100a3-9), tajriba has become in Burhān IV: 10 not merely the process similar to 'a mixture of sensory induction (istigrá') with intellectual deduction' that was described in III: 5, but also a cognitive state of the soul established by the well-marshalled contents of the retentive faculty. Tajriba has been made the nearest possible Avicennian equivalent of Aristotle's empeiria, which 'develops out of frequently repeated memories of the same thing' (100a4-6) and from which originate the arts and sciences (the latter contention being explained more fully in Metaphysics I: 1, 980b25-981a12).

An analogous change should almost certainly be made retrospectively in the interpretation of Avicenna's notion of istigrá': although sensory in a general way it too must belong primarily to 'estimation'. Indeed in the light of statements elsewhere in the Shifá', especially regarding mathematical examples, this is a safe inference and not simply a conjecture.³²

Through the discussion in Burhān IV: 10 the word 'tajriba' has come to denote the resultant state of the soul as well as the process, or family of processes, from which that state arises. Moreover, tajriba now may be described in another way, as the settled judgements in the retentive faculty that have been obtained through 'estimation', and thus ultimately from a sensory basis

Having presented his alternative to Aristotle's explanation of how universals, especially the primary premisses, are acquired, Ibn Sinā turns for the first time in the chapter to an explicit consideration of Aristotle's text, to the analogy drawn by the 'First Teacher' between the coming-to-a-stand of a universal in the soul and the coming-to-a-stand in their proper battle-formation by troops after a rout / Posterior Analytics II: 19, 100a12-13). Avicenna concedes all that he can, but it is not really very much Knowledge ("ilm) and the intelligible universal form are delineated little by little from sensible singulars, he agrees, and when these have been joined together, the soul acquires upon this basis the universal as such and then discards the sensory antecedents. Although the universa lman is somehow contained in the individual man reported by the senses, the notion 'man' qua sensible is 'diluted', Avicenna says; or, he continues, using a different and favoured metaphor, the sensible 'man' must be 'pared' by the intellect (so as to remove the 'husks' and permit access to the intelligible kernel). Working upward from the sensibles, however, the wahm, both in higher animals and in man, is able to distinguish between individuals of one biological species and those of others

^{32.} See the references given on pp 82-84 in Shlomo Pines. 'Philosophy, Mathematics, and the Concepts of Space in the Middle Agos', The Interaction between Science and Philosophy, Y. Elkana, ed. (Atlantic Highlands, New Jercey, 1974), pp. 75-90. The relationship of 'mathematicale', mathematical reasoning, and the socker in the Shoë's system is more complicated than it appears there, however I hape to publish an article on this topic with full documentation, especially from the Shoë', in the trasouably near future.

demonstrables. 30 (The function of tajriba in tajawuur, it should be noticed, emerges here for the first time).

The analysis is rounded off by Ibn Sina's etatement that the other composite universals, i.e., those that are not first principles, gain assent (taidq) from the intellect either by means of tajriba or by syllogistic demonstration through a middle term. It Tajriba in this case must relate to the extraction as intentiones of that which is essential in the sensorily apprehended conjunctions among things and from which the intelligible relations can be fully abstracted. In looking back it seems that this is the process that was meant in III: 5, and that scammony's purging of yellow bile and the other examples there were instances of this particular utilization of tajriba. It is made where there can be no middle term, yet where the composition of the simple intelligibles does not in itself necessitate assent. Finally, one may infer that the apprehension of middle terms also can involve tajriba in the way just introduced, or that, instead, it can be purely intellectual.

The account in Burhān IV: 10 is a disjointed one, even more dispersed in the original than here. But, especially when supplemented, as indeed it must be, by a reading of the Kitāb al-Nafs (to which the reader is explicitly referred at the end of the chapter), it is a very substantially coherent treatment. Insofar as tajrība is concerned, one has gradually been informed that it assists in tasawwur with respect to intelligibles generally and in tajdiq with regard to primary premisses. Tajrība of this kind is generated from a sorting of the contents of the retentive faculty, so that the products of the wahm become almost abstract. In creating tajdiq about secondary premisses concerning the observable world, tajrība is the most usual means and often it appears a necessary one. Here again it would be pre-eminently the macānī that are involved, although Avicenna leaves this as an inference to be made by the reader. Experience, in short, is the ultimate cognitive product of the sensory level of the soul and is what the human intellect can use heat when sceking the actual intelligibles from the Active Intellect.

^{30.} Burhán, Coiro ed., IV.10, p. 331, 11 16-20. Cf. Post. An. Wills, 10063-9, and also Msia I 1, 980b25-981a12 Although in Ariatotle's secounts, 'memory' is always undine, in the Arabic versions it is sometimes translated by dhike, sometimes by hig. No Arabic MS of Mrta. I (i.e., A). I is known to survive, but the main source for the Arabic text of the Pasterior Analytics, the translation by Abi Bishr Matth the Young, a extant. The Arabic translation of 100a3-9 (ed Badawil, op. cit. in note M mbove, vol. II, pp. 463-464) has both dhike and higs, thanks to the rhetorical style favoured by the Baghdad philosophers; the alternative word, moreover, is given as a variant in each case. Portupa the best reading is indeed that which is most suited to Avicenna's purposes, ris., that in which shife is connected with sensation and higs with 'experience'. The most important phrase is rightly worded in any case (with no variants given in the one - albeit very authoritative. MS used by Badawi). shifted withouthin fill-add high talpida widned ('many rememberings produce (lit., 'are') a single "experience", where 'rememberings' comes from the root [5-f-z.]).

^{31.} Ibid., p. 332, 11, 1-3,

The incomposites are subsequently related to each other with the help of the active imagination (i.e., the cognative faculty). A commentator on the Shifa' would like to add here 'and the help of the wahm'; but this does not appear in the text, and it is conceivable that compound intentiones are to be obtained only by abstraction from sensible forms joined together in the mufakkira, instead of through direct combination in the wahm. Whichever be the case, Ibn Sinā states that composites then appear among the marāni; and when one is produced that the intellect should know without instruction, it does know it, and in a fully abstract and intelligible way. Where necessary, the intellect tries out (Ij-r-b], II) the now intelligible premiss, in order, it seems, to comprehend it completely. So, Ibn Sinā concludes, tajdiq often arises from the senses by way of tajrība. The torm here may only refer to the 'trying out' that has just been mentioned; and it must designate the same kind of 'experience' as that which was discussed in Book III, for at this point Avicenna actually draws the reader's attention to his earlier treatment of tajrība.

Specifically as regards first principles, apprehension (tasaweur) occurs via sensation, cogitation, and estimation, lbn Sina now asserts; through these the incomposites are 'imaged' and then combined so as to be apprehensible qua composed. After being grasped in this way the composites are intelligized in essence, and assent (tasdiq) takes place spontaneously with respect to correctly related intelligibles - provided that the intellect thus prepared by sensible forms and intentions he conjoined to the 'divine emanation', i.e., to the Active Intellect. These 'first principles' or 'first cognitions', as Avicenna calls them here, are what in the Kitāb al-Nafs he terms 'primary intelligibles' and describes as 'the basic premisses to which assent (tasdiq) is given without being obtained ([k-s-b], VIII) [by any process] and without any awareness that assent might be withheld'.*

Ibn Sinž provides further and very enlightening information in this chapter. The retentive faculty, he says, is reinforced by repeated sensory impressions that resemble each other (mahsūsāt mutashābīha mutakarrira) - indirectly reinforced, for first (in a necessary step rather confusingly omitted here) the wahm must act upon the sensible forms. In the next stage, 'experience' (tajriba) is reinforced - nay effected. Ibn Sinž adds, strengthening his assertion - by repeated intentiones that resemble each other (mahfūzāt mutashābīha mutakarrira). The maḥfūzāt are literally the 'contents of the retentive faculty', but these are, of course, the ma'dni or intentiones that have been retained by the soul. And then from 'experience', Avicenna concludes, the intellect snares universals, either incomposite or combined, as objects of apprehension (almutaṣawwara) and composite universals as objects of taṇdiq, if they are in-

²⁸ Ibid., p. 331, 11, 7-10.

^{29.} Kitāb al-Nafs I.S., ed. cit. in rote 8 above, p. 49, the passage is also contained in the Najāi (Arabir text, ed. cit. in auto 10 above, p. 166, in Rahman's Eng tr., cited in the same note, p. 36).

in its restricted technical sense. This meaning is explicitly utilized in IV; 10, where khaydi designates the lower, 'passive' imagination or 'representative faculty', which, as one is told in the Kitāb al-Nafs, serves as the memory for the synthesized sense-reports assembled by the 'common sense' and, when required, 're-presents' these integrated images for use by other faculties. But there is also a higher, 'active', combinative imagination, able to divide, recombine, and manipulate images, and thus 'imagine' in the usual modern sense; Avicenna calls it the 'imaginative faculty', (al-mutakhayyila), or, without ambiguity, the 'cogitative' (mufakkira) faculty. The mufakkira, like the khaydi and, as noted earlier on, the wahm, is fully described only in the Kitāb al-Nafs. Unlike the estimative faculty, however, the combinative imagination is by no means original with Avicenna. Even as early as Aristotle there was a similar distinction which was made, namely that between 'sensory' and 'deliberative' imagination (e.g., in De Anima III: 10-11; cf. also the analysis in De Memoria et Reminiscentia as a whole).

The introduction of 'active imagination' and 'estimation' in Burhon IV: 10 elaborates the analysis of the acquisition of knowledge into a form coherent with the theoretical psychology developed farther on in the Shifa' in the Kitāb al-Nafs. The mufakkira and the wahm, while remaining on the sensory side of the cleft between sensation and intellection, do help to narrow it; sensory and intellective processes never can be continuous with each other in the system constructed by Avicenna, but he is reasonably successful here in his attempt to align them with precision in areas where tajriba has brought them close together.

The fuller descriptions in IV: 10 emphasize a second sort of taidiq, harely noticed previously, where the 'acceptance' follows automatically upon the 'apprehension'. It is this kind of acceptance which Ibn Sīnā assigns to first principles. By these he means the indemonstrable universal statements that serve as axioms for thought in general or for individual sciences. The example which he gives here is the idea that the whole is greater than the part; elsewhere he mentions the rule that quantities equal to the same quantity are equal to each other and the laws of contradiction and of the excluded middle.

A full synopsis seems the only satisfactory way to explain the place alloted to tajriba in the final scheme. From the contents of sense-perception, Ibn Sinisays, two kinds of cognizable entities are obtained: the sensible forms, stored in the passive imagination, and the intentionss (macdni), extracted by the estimative faculty and stored in the retentive faculty. These forms and intentiones are confirmed, or 'reinforced', in modern terms, by further sense-perception and estimation. From them are apprehended incomposite universals (of entities sensible in essence).

premisses by means of experience (tajriba), he adds. But even in these cases, where sensation indeed allows one to reach the universal premisses, the actual cognizing of them is not by sensory means.

The carefully delayed attack against Aristotle's position comes at last in al-Burhān, IV: 10⁸⁵ - predictably, for this chapter occupies the place corresponding to Posterior Analytics II: 19. Avicenna, clearly, must oppose the wholly empirical theory of knowledge which there received Aristotle's most lucid exposition. No mention of this delicate fact falls on the innocent cars of the reader, however; the offending doctrines of the First Teacher are simply not indicated. Instead of such argumentation, Ibn Sīnā at last provides a full if discontinuous summary of his own theory.

The object of the chapter is indeed the same as that of Aristotle's: the identification of the faculty of the human soul whose business it is to know primary premisses without being taught and the discovery of the manner in which this faculty becomes operative. For both men the entity sought is, in fact, the intellect: the nous (as 'intuitive reason') in the case of Aristotle – a faculty immanent and complete in itself, at least in this analysis; and the potential intellect ("aqi bi'l-quavea"), which is actualized by the external Active Intellect, in the case of Avicenna. The most interesting divergence here between their doctrines is that which concerns the relationship of knowledge to experience. Before these accounts can be compared, however, Avicenna's needs to be studied with some care, the more so as it departs very considerably from what might be expected on the basis of Book III.

Ihn Sina now presents an integrated epistemological and psychological description of the acquisition of basic premisses. In the apprehension and acceptance of these first principles, he explains, other faculties assist the intellect, viz., the external and internal senses. Among the latter this time he names the 'estimative' faculty, whose quasi-universal intentions he discusses, the special memory for the intentions, and two carefully distinguished imaginative faculties.

Whenever Avicenna spoke of imagination in Burhān III: 5 he used only the term 'khayāl' and its derivatives and talked in a way appropriate to khayāl

^{25.} Burhan, Cairo ed., pp. 330-333.

Post, An. II.19, 99520-100517. This account is complemented by that in Meta. I:1, 980a27-981a30.

Aristotle's 'empiricism' is, finally, a matter of interpretation, but the opposed view must take account not merely of these two passages, and the two already discussed by Ibn Sinā in Burhān III.5 and III.8, but a great many others, all of which are ignored here. The idea that Aristotle believed latelligibles to be abstracted from sensory 'imagings' by an internal active principle of human intellection, and to be stored, in poissitia, in those images, receives powerful support from such texts as Ds Anima III.3, 432a 7-10, III. 7, 431a 14-20 and b2-19, and III; 8, 432a-14, and Do Mom. et Rem., 1, 449530-450a 14. Ariemna deals with those in connection with other issues, munity in the Kittle it. Nafs, and invariably dismisses any interpretation of Aristotle's spistemology that makes it empirical.

and its greatest importance lies in natural philosophy and in such related arts as medicine. Indeed, Avicenna's examples in this chapter are of physical causation, for instance, that 'the lodestone attracts iron' or that 'scammony purges yellow bile'. 21

Ibn Sinā has gone some way towards saving the letter of Aristotle's dictum that deprevation of sensation produces a deprivation of knowledge. With a few exceptions (which are not mentioned here), people usually need sensory information to permit intellectual apprehension of species of existent things that are sensible in essence. They may need observations of sense to remind them of intelligible premisses not thoroughly acquired previously. Most significantly humans usually require repeated observation of natural things to produce 'empirical' laws, such as 'the lodestone attracts iron'.

The greater part of the necessary technical analysis has just been presented in connection with Avicenou's first discussion of knowledge and experience. His second account of these matters, in Maqdla III, fail 8 of al-Burhan need only be touched upon. Let one point alone be stressed: in this chapter Ibn Sīnā is able to postpone the inevitable confrontation of Aristotle's views only by a deliberate but rather ingenious misinterpretation of what is said in the parallel chapter (I: 31) of the Posterior Analytics. There Aristotle talks of the effects produced by a lack of sensory data (literally, 'a failure of sense-perception', but the context is unusually limpid); Ibn Sīnā chooses to understand this as concerning the effects of an 'incapacity of sense to penetrate', for which there is no textual basis. Greek or Arabic. Avicenna thereby allows himself to cover, rather more quickly, much of the same ground already traversed in chapter 5.

It is the concern of the intellect, he states, to devise from repeated particulars an intelligible abstract universal (kullivy majorrod ma'qūl), an intelligible meaning to which sense has no access. Thus, for example, neither can one sense every eclipse nor can one sense any eclipse universally. Instead, Avicenus tells the reader once again, the intellect obtains the abstract universal by the light from a divine emanation. The intellect often 'anares' universal

²¹ Ibid., p. 224, 1.2 The famous 'empirical method' (regarding the use of compound medicines) in the Sinà's Canon of Medicine (Al-Qanan fi'l-Tibb, is indeed 'empirical' in this sense. The discussion there holds virtually nothing of opintenological anterest, however, and nothing at all for psychological theory. (See Canon II 1.2 and 3. Arabic text, Cairo (Bullaq), A.B. 1204 (1877), Vol. I, pp. 224-231 Again one linds the example of scarmony.)

^{23.} See Burbin, Carro ad., p. 224, f. 11, where Avicenna and his discussion by saying, 'Therefore, everyone deprived of a certain [amount of] sensation is deprived in respect of a certain [amount of] knowledge, even though sensation is not [itself] knowledge'. Cf. note 12, above.

^{23.} Ibid., pp. 249, 1, 11 - 250, 1, 10, esp. p. 250, 11, 1-6.

^{24.} The 'misunderstanding' of Aristotle here is theroughly treated in 'Affit's introduction, ibidpp 39-40. The crucial line comes at Post An. 1-31, 88s 11-12; in Matth's Arabic translation, the phrase is faqdu'l-hers (ed. 'Abdul'l-Rahmān Badawi, in Mantiq Arista, vol. II (Carro, 1949), p. 398).

Although this degree of distortion in the use made of the inherited technical vocabulary by Ibn Sinā is rare, it should be emphasized that the method as such is standard with him, and perhaps not much less so with Aristotle and most ancient and medieval philosophers. The philosophical and scientific usages of a term are analysed, and a meaning is then adopted which in part 'saves' the earlier ones but also reinterprets and refucuses them, so that the significance of the word is shifted and may be greatly distorted. (Perhaps the most amusing example in Ibn Sina is his blithe equation of the Galenists' terms for the higher psychological faculties with his own not dissimilar names, when he knows full well that his psychological schema is radically different from theirs and thoroughly anti-Galemetic. Many medieval and modern physicians and scholars have thus been misled. Similar remarks might possibly be made about his use of the language of the sali's in the Isharat). Potential converts to an unfamiliar intellectual position are to be won over. Avicenna's writings reveal, by the use of a familiar language which contains some suitably reinterpreted terminology.

Only the means designated as 'tojribo', which, however, is the most important and interesting of the ways through which sensation can contribute to tasdig, now remains to be treated in Burhan III: 5.19 In discussions relating to cognition, 'tajriba', like 'empeiria', means 'experiencing', 'gaining or having experience of or . . . acquaintance with or . . practice in with a connotation of 'testing' or 'trying out' in the case of tarriba. Avicenna here describes tarriba simply as having in it 'a mixture of sensory "induction" (istigra' hissi) with intellectual deduction (quyas cagli)', to Aristotle's 'empeiria' seems to have been a hexis, a 'developed state' of the soul, but Avicenna's 'tajribu' looks at this point to be a process; on this, more below. In any event, tarriba is a judging through many particular examples that there exists a constant relationship between two universals such that a certain premiss asserted of them may be given assent. It seems reasonable to infer from Ibn Sina's abbreviated explanation that individual happenings gradually limin a universal, the representation of which is then completed by examining (or 'testing'?) further instances. One is actually told only that after sense-reports of often-repeated happenings of the same specific sort have been received, the intellect judges that the conjunctions involved are essential (dhatt), not coincidental (attifagt), because 'coincidence does not persist'. So the intellect is able to abstract what is in essence from what is by accident after a sufficient amount of 'experience'. In this manner tairiba will generate tasdia, according to the present account, and 'experience' will actually bring to pass ([w-q-'], II) in human minds proper universal cognitions.

'Experience' necessarily is concerned only in things accessible to sense,

^{19.} Ibid., pp. 223, 1, 16-224, 1, 5, 20, Ibid., p. 224, 11, 6-7; cf. p. 223, 1, 16.

it is not linked with tajriba. Indeed the sifting process is not granted a name, nor in this chapter are its products given any special designation.

When he turns to taidiq, Ihn Sinā finds not one but four ways through which sensation can contribute. The first is 'by accident' (bi'l-'arād) where apprehension (tasacceur) of one or more of the simple universals has been achieved with the help of the senses in the manner already explained, and the intelligibles have then been combined directly. Tasdiq is here an immediate result of the 'light' of the Active Intellect; in Avicenna's words, this kind of intellectual assent occurs only 'through conjunction (titigāl) of the [human] intellect with the light (nār) from the Creator emanated upon souls and nature, which is called the Active Intellect ('aql face'āl) and which is the agent that leads the [human] potential intellect out into set'. It must be noted that the 'light' is only ultimately, not immediately, 'from the Creator', and that 'the Creator' designates the One or the Necessary Being of the philosophers, not the creator-God of the Qur'ān and the Bible.

The second way of reaching tasdiq from sensory starting points is the 'particular syllogism' (qiyās jux'i). By this phrase Avicenna means a predicating about some natural species of something already known to be predicable of its proximate genus, through having apprehended by sense individuals which belong to that species (and a fortion to the genus).

In the third place comes 'induction' (istiqua'), a term which usually stood for the Greek word 'epagoge'. Whereas Aristotle meant by epagoge an advancing from all available individual instances to a universal judgement. Ibn Sina perversely chooses to denote by istiqua' a process in which the attention of the intellect is merely drawn to a relationship among universals by one or more perceptible examples of it, whether this be in the first instance or later on as a reminder. The intellect becomes aware of believing the intelligible relationship, but the 'induction' itself does not create that behef. By means of intiqua' sense is only able to occasion the acceptance of premisses, and that almost trivially.¹⁹

For Avicenna, of course, the inductive leap in the usual sense is ontological as well as logical, so a metaphorical understanding of spaging; is the best that can be expected. Even so, his interpretation of istigra' certainly must be called guileful, for it does not preserve the meaning that a reader of works of folsafa is justified in expecting. Its principal ment may be to obviate a later explanation of Aristotle's doctrine (100b3-5 in Posterior Analytics 11: 19) that 'the method even by which sensation implants the universal in us is inductive'.

^{16.} Burhan, Cairo ed., III:5, pp. 222, 1, 17-224, 1, 10

^{17.} Ibid., p. 223, 11. 3-4.

^{18.} Ibid., 11. 11-15, contains the description of istigrd' Perhaps it is meant as a gesture towards Plato's anamnésis - the main account, in the Phaedo, should have been known to Iba Sina.

are either received completely and correctly by the rational faculty, since they are its proper objects, or are not received. When the simple intelligibles have been combined, connected, that is, in such a way as to be expressible in syllogistic premisses, the resulting composites may be either true or false; so beyond simply apprehending their intelligible content the mind must judge whether they are right, must guin conviction about their truth or falsity. The second stage, the accepting of the composite intelligible or premiss. Ibn Sīpā calls tasdig. This word was regularly used by Arab translators to render Aristotle's puties, which was something logically different, being the confidence or conviction associated with the intellectual assent to a premiss. Nonetheless the usage of tasdia employed by Ibn Sina and the distinction between tasawwar and tasdig are standard in Islamic philosophy.15 The ideas of tasawaar and tastia and their relation to simple and composite objects of thought seem to depend ultimately on Aristotle's remarks about the subject, for example in Metaphysics IX: 10 and in De Anima III: 6, although there are perhaps also Stoic influences.

The accounts of the acquisition of knowledge given by Aristotle in Posterior Analytics II: 19 and Metaphysics I: 1 did not make full and consistent use of this analysis. Avicenna, however, is obliged by hindsight to do so. In the Posterior Analytics Aristotle was writing about the starting-points for episteme, so he should have concerned himself with the grasping of first premisses; but his description seems really to apply only to the separate universals contained in those premisses. In particular, emperria emerges as the cognitive condition which results from the sifting and ordering of repeated evidence of the senses and which permits the rise of universal concepts in the soul. But in the discussion in the Metaphysics Aristotle clearly referred to composites and made empeiria the immediate source of the premisses in the arts and sciences.

So Avicenna has a good deal of room in which to manoeuvre, even if he wishes to be purely Peripatetic. His first move in Burhān III: 5, as was noted, is explicitly to restrict the possible range of empirical cognition to objects that are sensible of essence. He then separates his analysis of tasaccour from that of tasdiq, and for the present, limits his discussion of the function of tagriba (i.e., 'empeiria') to the second stage of the acquiring of intelligible premisses, to tasdiq.

The sorting of the sensory contents of the soul in preparation for the tagainwur of incomposite universals remains more or less as it was in Aristotle, but

¹⁵ The standard examination of this topic, no longer completely satisfactory, is Harry Austryn Wolfson, 'The Terms Tagaesser and Tagdig in Arabic Philosophy, and their Greek, Latin, and Helrew Equivalents', The Modern World 33 (1943), pp. 1-15, repr. in Harry Austryn Wolfson, Stadies in the History of Philosophy and Religion, vol. 1, ed. 1. Twersky and G. H. Williams (Cambridge, Mass., 1973), pp. 478-492. (See also Josef Van Eas, Die Erksontinistelere des Adadadd Li (Wiesbaden, 1966), pp. 95-113; passim, and Febru Jadasne, l'Influence du Stoicsme sur la pense musulmone (Berrit, 1968; Recherches... de l'Institut de Lettres Orientales de Reyrouth, sér. 1, t. 41) pp. 106-113, passim.

truly can be said to attain to knowledge. And indeed, despite his lengthy discussion of the help provided by the senses, Ibn Sină does not deviate from this position even here in Burhan III: 5. Were be forced to summarize what he has actually asserted in this discussion he would be unable to save Aristotic's doctrine. He could come no closer than to claim that for people other than prophets and the best philosophers, sensation provides support that is widely necessary as an aid for intellection when they are first acquiring certain branches of learning, and that lack of sensation under those conditions does mean a loss of knowledge.

A résumé of Avicenna's description in this chapter of the psychological processes used in gaining knowledge of the temporal world will facilitate the tracing out of the developments that occur in his next two accounts. That the sensible and intelligible natures in things are distinct is his starting-point here: sense does not encounter the nature of man, for example, qua generalizable (al-insān al-mushtarak fihi). The 'man' apprehended in the human intellect through the essential definition (hadd)¹³ has been abstracted ([j-r-d], II) from all the accompaniments and individualizations of material existents, and qua abstract it is no object of sense. What the external senses do is merely to take up the sensible form and deliver it to the representative faculty (khayāl), i.e., to the sensory memory, where it becomes subject to operations superintended by the individual potential intellect. The intellect causes the images to be compared and, noting what is different, abstracts that which is common; thus it pares away the accidents and obtains the intelligible essence – but not from the images themselves. 14

As Ibn Sinā explains in many places, but not in this passage, the potential intellect after being thus prepared acquires the intelligible from a separate and eternal intellect-in-act, the Active Intellect, indeed, which has already been described. Nor can the human intellect store the universal thus gained; it is able only to increase the degree and range of its receptivity and remember where to 'look' for intelligibles previously possessed.

Up to this point Avicenna has been dealing with the apprehension (taxonteur) of incomposite universals, which the mind either grasps or does not, which, in other words, are not true or false in themselves but in every case

^{13.} Tepicower of the incomposite intelligibles is primarily by way of the hadd, see Shifd': Höhryd. V: 5, 7, and 8, pussim, and cf. III 8 (The best text of Avicenna's Metaphysics is in the Shifd'. Care ed. Al-Hährydi, vol. I ed. by G.C. Answer and Sa'id Za'id, vol. II ed. by Muhammad Yhauf Müsl. Sulsymän Dunya, and Sa'id Za'id (Caro. 1960).) The hadd in this are narrowest technical sense, is the abstract, intelligible nature (hagia) of an infina species, which is also present in each individual of the given species and comes to it from the Active Intellect as datar formarum (cf. Hährydi IX-5, passim, The hadd when expressed as the formulable essence of a species becomes its essential defination, still called the 'hadd' (now strictly = Gk. horos ar horismos). This idea of the rôles of the hadd is a comparatively obvious extension of Aristotchan teaching; cf., especially, Meta, VII: 4, 10300 2-17.

^{14.} Burbán, Cairo ed., 111:5, pp. 220, 1, 8-222, 1, 16.

er used in imagination, are derived from sensations. Ibn Sina tells his readers. and with such images the human intellective faculty can act in such a way as to acquire incomposite universals. These it can then join together into definitions, premisses, and syllograms. Sensation in this way is a principle for the apprehension (tagawaur) of intelligible universals, but only by accident (bi'lfarad), not in essence (bi'l-dhit). In the sciences concerned with things that have corporeal existence, and are thereby sensible of essence, that same division of function between sensory and intellective processes is to be found also in the acquiring of primary premisses, i.e., those from which demonstration has its start; sensation plays a part in the recognizing of first premisecs (provided they relate to things sensible) as well as in apprehending the universal terms they contain and the subsequent middle terms that are needed to construct the demonstrations. In other words, the products of sense-perception are a source for the objects of nous, in the narrower Aristotelian sense of 'direct intellectual grasping', whether they be incomposite or composite. Sensory processes may also be employed, it turns out, in testing derivative premisses, empirically.

But sensation will ultimately be allowed only as a basis, and often a dispensable one, for acquiring the genuine universals. Even in this early chapter one discovers that things which in their existence are sufficiently unconnected with matter as to be intelligible in essence cannot be apprehended from any sort of sensory foundation. Some few persons, moreover, have strong enough intellectual faculties, Avicenna maintains, that they can attract all or most intelligibles without recourse to information from the senses; other persons less gifted but still intellectually able can develop their intellects to a level where reference to sense-data and imaginings becomes unnecessary. These doctrines, which are not developed in the Burhan, appear in the Kitab al-Nais and elsewhere: furthermore, it is safe to infer from discussions in the Kitāb al-Nafs and the Ilahiyyat that all persons can obtain at least a few of the universals that relate to the natural world without any recourse to the senses or to imagination. 140 Since, finally, it is only the intellect, when complemented from without, that can grasp the pure universals, only the intellect

remark by Aristotle about a loss of rensation, Post. An. 7: 18, 8la 38-40, as repeated by Avicanna at p. 220, 11 5-7, in the present chapter (and cf. p. 224, 1. 11).

See also "Affit"s description of the correspondences between Avicanna's and Aristotle's texts, pp.

³⁶⁻³⁷ in his very useful introduction to this work.

⁽At De Anima 111: 3, 432s 7-10, and De Mom et Rem. 1, 439h 31 segg., Aristotle makes a related chaim, that if one paremyos nothing though the senses, one is incapable of learning anything).

¹²s That in principle every corpored aid to human intellectual cognition is dispensable is something Avicentia seems sever to assert outright, it is necessary to study all the possibilities one by one to extract this generalisation, which remains provisional, even though any exceptions will have to have a carrow range. See, int. al., in the Shifa", al-Hāhiyyai III. B and IX 7 and Kirāb al-Nafs V 3 (with sare) and V 5 and 6, no well as some relevant passages in all Risata al-Nafshuyya; Note especially Kitāb al-Nafs V 6, pp. 248-250, ed. cit. in note 8 above, English translation in Rahman, tr., op. cit. in note 10 above, pp. \$3-37 (= pp. 166-168 of the Arabic text of the Nagit, ed. cit. in the same note).

cognizable objects that are more abstract and less immattered, quasi-universals hke the lower kind of things that are now called 'intuitions'. These products of the wahm, which Ibn Sina designates ma'ani, are perhaps best referred to by the Scholastic term 'intentiones'. A stock example is the intuition of 'enmity' that a sheep forms about wolves; although post-sensational, it is not completely abstract, not 'intelligible'. " For a person, intentiones are the final and most abstract result of his apprehension of the sensory world. They provide the nearest Avicennian equivalent to what Aristotle called 'empeiric' when he spoke of 'experience' arising from repeated memories of the same thing (cf. Metaphysics I: 1, 980b 25-981a12, and Posterior Analytics II:19, 100a3-9). These intentiones can show a person's intellect where to 'look' in the intelligible world for the true universals - the concepts and ideas contained in the indemonstrable first premisses and subsequent middle terms which build up the demonstrative sciences. But knowledge as such arises solely through intellection: through grasping the intelligibles, which emanate into human minds only from the separate Active Intellect, in which also they are stored. In this way Ibn Sina has found a rôle for the senses and for experience in reaching knowledge, but knowledge itself has been kept absolutely intellectual and incorporeal, essentially independent of sensation and everything bodily.

The main account of this borderland between psychological theory and epistemology comes, as one would expect, in that book in the logical jumla of the Shifa' which corresponds to Aristotle's Posterior Analytics, vis., the [Kitāb al-] Burhān. As might also be anticipated, the treatment is not straightforward. One must look at three fairly widely separated chapters, III: 5, III: 8, and 1½: 10, and cope with a lack of candour concerning Aristotle's views that ranges from mild deviousness to intentional and unblushing misrepresentation. One is taught a great deal, however, about how Ibn Sinā expounds and develops his ideas – a sobering and cautionary experience for anyone tempted to use the obiter dicta of Avicenna as a basis for construing his doctrines.

In his first discussion, the one in [Kitâb] al-Burhân III: 5, Avicenna constructs an interpretation of the subject-matter of Pasterior Analytics I:18 and tries to show that loss of sensation results in loss of knowledge, as Aristotle there has clearly stated. It images in the soul, including those stored in memory

^{11.} The main treatment of the wahm is located in the Kitáb al-Nafs of the Shifa', Bk. IV, chs. 1 and 3 fed cit. in note 8 shove, pp. 163-169 and 182-194); other discussions are to be found in 1.5. Ht. 8, and the last part of V 6 (csp. pp. 45-46, 153-154, and 244-246). The connection with tagribals mentioned in IV: 3, pp. 182-185.

The Najót again presents a rudimentary but halpful summary of the doctrines. See Rahman, tr., op. cst in note 10 above, pp. 30-31 in ch. 3 and pp. 39-40 in ch. 7 (but ignore the commentary, which here no longer stands up well)

^{12.} Shifa', Caira ed. 4l-Mantiq, 5: al-Burhān, ent. ed. and introd. by Abu'l-'Al&' Affii (Cairo, 1956) (hereafter, 'Burhān, Cairo ed'), Magdia III, fail 5, pp. 220-227. Only pp. 220-224, l. 11 are relevant here. Aristotle is not mentioned by name, the Sind merely writes 'q.la...', 'it has been said...'. The

eternal world that is grasped by the intellect. (In this, of course, Ihn Sīnā follows an ancient Greek intellectual tradition that goes back at least to Parmenides). These realms never overlap, and they meet only in the human species, in each individual soul. There, the lower world rises as far as sepseperceptions (mahsūsat) and 'estimative' intentiones (see below), and the intelligible world reaches down to the potential intellect, which it renders actual. Sensibles (mohsūsāt) — sensory information of any kind — do not contain, and sensation cannot grasp, any true universals (kulliyyāt). Consequently, Ibn Sīnā may not allow any genuinely empirical theory of the acquisition of knowledge: in the end, authentic knowledge ('ilm) can be attained by a human being only through his externally actualized intellect ('aql).10

Induction (istigrā': translates Greek epagoge), in particular, is strictly if disingenuously proscribed as a generative source of knowledge. But when it comes to smpeiria (rendered in the Arabic texts as tajrība), Avicenna equivocates, for he is anxious to save Aristotle's all-too-unambiguous presentations of the empirical basis of knowledge in Metaphysics I: 1 and, especially, in Posterior inalytics II: 19. Experience, Ibn Sīnā decides, can lead to knowledge; and, tortured also by Aristotle's plain speaking in Posterior Analytics 1: 18, he even grants that sensation may be regarded as a principle of knowledge but, the reader can infer, not as a strictly essential (dhātī) principle nor by any means as a sufficient one.

The connection between tajriba and 'ilm is eventually explained in terms of two faculties that seem to be among Ibn Sīnā's own contributions to the analysis of the soul, the 'estimative' faculty (wahm, quivea wahmiyya) and the 'storehouse' or special memory associated with it, which is called the retentive, or memorative, faculty (hāfiţa; dhākira). From the sensible images contained in the soul, whether they are simply remembered or have been separated and recombined in imagination, the estimative faculty forms

10. Besides the main reference given on p 52, above, see also the preliminaries contained in Kudb al-Nofs, Bk. I, ch. 1 (last third); IV: 2 (passin), V: 1 (second balf), and V: 2 (passin) (ed. ch. in note 6 above, pp. 12-16, 163-169; 204-209, and 209-221). Short discussions pertinent to the question of tagribs and "ilm, both subordinate to the main accounts in the [Kudb] al-Burhān (for which are below), appear in Bk. II, ch. 2, of the Kudb al-Nafs and in V. 3 (ed. cu., pp. 60-61 and 221-222).

An incomplete presentation of the psychological theory of the acquisition of knowledge is to be found in the Najds, see F. Rahman, tr., Aucenna's Psychology. An English Translation of Kudh al-Najds'. (London, 1952), this 5, 7, and 11, pp. 33-35, 40, and 55 (corresponding to pp. 165-166, 170-171, and 182 of the second edition (Cairo, 1936) of the Arabia text), for sajriba, see esp. p. 55.

Chapter 16 of this part of the Najdi (Rahman, tr., pp. 68-69, Arabic text, ed. ci., pp. 192-198) is also relevant, although unlike the other chapters mentioned it has not actually been excerpted from the Shifd'. The full doctrine is simplified here by omitting the rôle of 'estimation'; compare the remarks below on the Sind's sigular procedure in the [Kudh] al-Burhān.

Persons unfamiliar with the area of thought to which Ibn Sina's psychology belongs may be defined by the rather advanced introduction to be had in Herbert A. Davidson's 'Alfarabi and Avicenua on the Active Intellect', Visior 3(1972), 109-178. In the present instance, Avicenna's elaboration of the Aristotelian view has required two entities from without, instead of only one, to complete each human soul. Aristotle's ambiguities were more economically resolved by Alexander of Aphrodisias and by Themistius, and will be so done again by Averrors. But these departures from Aristotle permit Ibu Sinā to save his non-Peripatetic conceptions of immortality and of intellection. It is not too strong to say that his own pecuhar idea of personal salvation determines the nature of his solution to the problem of abstract (i.e., intellectual) thought and, derivatively, to the ensouling of the embryo.

The main difficulty that Avicenna has to face is accounting for the individnation of an intellect; nor does be ever satisfactorily explain it. His approach to the question depends upon the materially individuated potential intellect, which is not problematical in this respect. He attaches the potential intellect to, or identifies it with, a person's rational soul, which he has made the 'intellect' that enters the embryo 'from without', But the continuing individuality of the potential intellect when conjoined to the Active Intellect is left mexplained. Our individual, an intellect must be attached to a body and therefore be mortal; qua actual and eternal it should not be individual. (Whether certain aspects of the rational soul as presented by Ibn Sina justify recent talk of an 'ego'-concept, or something similar, in his psychology, and whether, if so, that would help solve the problem of andividual intellects is a question that I shall take up briefly at the end of the paper.) Ibn Sīnā's aim, in any event. is to justify a scheme whereby the individual potential intellect perfects itself by continually rising to the grade of 'acquired intellect' and receiving actual intelligibles from the separate Active Intellect, so that it can function continnously and in actu after the body has died. The Active Intellect, moreover, with its cternal, actually intelligible contents, remains in Avidenna's program safely outside the corruptible human realm.

But however pleasant this knitting together of psychological, embryological, and soteriological doctrines may be, it is only byplay to the main philosophical drams that derives from Ibn Sīnā's conception of immortality. The centre of the action lies in his metaphysics: in epistemology first and then, without resolution, in ontology.

By way of preface to the second, epistemological example of the influence of Ibn Sinā's psychological theories, it is necessary to emphasize the radical distinction in Avicennian metaphysics between the corporeal and corruptible world that is apprehended by the senses and the higher, immaterial, and

^{9.} Of course the synthesis is not pleasing insofar as it multiplies entities. All too often Avicents systematizes by merely adding theories together, however well he failshes the joins his thought never becomes a perfectly unitary structure, for he attempts to incorporate too much.

Even so, as will become evident, a great deal of his concidentory discourse is samed at disarming criticism of what is actually rigorous and proper system-building on his part.

In Avicenna's Hayawan it is the rational soul that corresponds to Aristotle's intellect 'from without', and this is the human intellectual faculty as such, the undeveloped capacity for receiving intelligibles. For Aristotle, however, one may reasonably conclude that the intellect 'from without' was of the self-sufficient kind which seems to have been implied by his description in Posterior Analytics II: 19 of how universals are acquired, and which therefore must include both the passive and active intellectual faculties that have so tantalized the interpreters of De Anima III. 5. But howsoever one chooses to resolve the ambiguities of Aristotle, there are none left here in the Shifa'. The intellect 'from without' of the De Generatione Animalium has become the rational soul, which is an intellect in potentia (bill-autona) (and which originates from the Active Intellect, in this entity's rôle as dator formarum; cf. al-Shifa', al-Ildhiyyat IX: 5). On the other hand, the active human intellect. in accordance with an exceptical tradition descending from Alexander of Aphrodisias (fl. early 3rd cent. A.D.), has been made external and is, indeed, one aspect of the Active Intellect. The human intellect-in-act, however, is now interpreted as the individual's 'acquired intellect', produced through the 'illumination' of his passive intellectual faculty by the true Active Intellect; it has thus become the more effect of another action 'from without', a collection of intelligibles lent from above. In whatever way Aristotle is to be understood, it is quite certain that he wished to have only one entity from without involved in the human soul, but Avicenna, with Muslim largesse, has given us two.

There is no excuse for considering this a mistake on the part of Ibn Sipa. He is not explicating the texts of Aristotle, but is expounding a consistent philosophy of his own within the general confines of Islamic Peripateticism. That one may speak of a correspondence between chapters of the Shifa' and chapters of Aristotle's works only reflects the fact that the Shifa' is an encyclopaedic work covering the whole of Greek philosophy (in the first, second, and fourth jumlat) and the mathematical sciences (in the third jumla), whose basic order of exposition in logic, natural philosophy, and (to some extent) metaphysics follows the standard Arabic arrangement of the Aristotelian corpus. (Material equivalent to certain other works, such as Porphyry's Essagoge, is added in: and in the Metaphysics (al-Hähryvät) are included various further topics, owed mainly to al-Farabi, that are ethical, political, or religious in nature and replace the 'theoretical' content of the standard texts in ethics and politics (of which Aristotle's Nicomachean Ethics and Plato's Republic are the most important). It may be assumed that the Shifa' is intended to be read by serious students in place of the books by the Greek authors). Consequently, the Shifa' often takes over the structure of Aristotle's writings, sometimes down even to the sequence of thought within judividual paragraphs. But its views are as independent of Aristotle's teachings as Ibn Sina feels to be desirable. The next example will make this assertion more obvious still.

First, however, the biological matters. What specific changes does Avicenns's theory of immortality generate in Peripatetic teachings about the ensoulment of the human embryo? The problem is set by Anstotle's notorious discussion in De Generations Animalium II: 3, where he speaks of the intellect (nous) 'from without' (thursthen). Ibn Sinā's treatment comes in the Shifā', al-Ifayauān XVI: 1; his account at the start follows Aristotle, but it ends with a notable addition.

The vegetative level of the soul, which oversees the development and growth of the embryo, is received with the semen of the father, Ibu Sint asserts; and in the semen there is also something which is 'prepared to receive the connection ("alaga; with the soul", vis., the (vital) heat, which is not fiery like elemental fire but is analogous, rather, to the heat which emanates (vafidu) from the heavenly bodies and is ultimately related to their substance (saidhar). So far, reasonably orthodox Aristotelianism. Also, Avicenna savs. when the heart and the brain bave come to exist in the embryo, the sensitive (hissivva) soul emanates (tofidu) from the vegetative, and the rational (nutgiven) soul becomes attached to it (to the vegetative organism, apparently, at the same time as the sensitive soul is produced). Still Aristotelian, although everything has been consolidated in such a way as to permit the highly tendentious constructions which now follow. The rational soul, Avicenna continues, is different from the other two levels and has nothing do to with matter as a substrate, but the soul (qua rational) is not yet effective (camila), being like that of the drunk or the epileptic. It is completed ([k-m-1], X) only by something external, when, in the person's childhood, that entity first assists the intellect ('agl) (i.e., enables it actually to think).

The last statement may be made more explicit by reference to the Shifa', Kitāb al-Nafs, especially V: 5 and 6. The rational soul which enters the embryo has but the bare potentiality for intellection, the grade of intellect that Iba Sinā calls 'material' (hayālani). This potentiality becomes actualized, becomes truly an intellect, by receiving intelligibles as such from the separate and eternally actual Active Intellect ('aqi fa'c'di), the lowest of the celestial intellects. The grade of its potentiality increases by degrees, but the rational soul attains the intellect in actu (bi'l-fi'l) only when it is 'borrowing', or 'has acquired', actual intelligibles from the Active Intellect. It then possesses a true intellect, called the 'acquired' (mustafād), which is correctly the second entity referred to above, the intellect which 'completes' or 'perfects' the rational soul.'

^{5.} Iba Sina, Al-Shifd', ed.-in-chief Ibrahim Madkur (Cairo, 1952-), hereafter referred to a 'Shifd', Cairo et . Al-Jubi 1993: 8 of Hayanda [more properly, 'Fi Jubi': al-Hayanda], ed. 'Abdullah Balim Muntage, Sa'id Li'id, and 'Abdullah lema'il (Cairo, 1970), Maqdid 16, fail 1.

^{6.} Ibid., p. 403, 11, 1-3 and 8-11.

^{7.} Ibid., 11. 3-8.

9. These chapters contain the main exposition of Ibn Sink's theory of the acquisition of knowledge through the intellect and its subsidiary faculties, see F. Rahman, ed., Avicanna's 'Da Anima' [Al-Shifa': Kindi al-Neri] (London, 1959), pp. 234-259.

le'), and, in some areas, from writings in the Galenic tradition. Specifically, Ihn Sina's psychology in both approach and content was principally Aristotelian. There had been incorporated within it, however, certain insights that belonged ultimately to Plotiman philosophy; and there had also been accomplished the more difficult and less precedented task of transplanting into it certain 'religious' conceptions, Muslim in Avicenna's own eyes but scarcely so in most others.

Ibn Sina's idiosyncratic notion of individual immortality required an elaborate and painstaking integration into his philosophy, into psychological theory first and then into related areas throughout the system. Biology, epistemology, ontology, ethics, and political science, each and all needed to be modified. The idea itself which Ibn Sina had formed of personal salvation was simply that an individual's intellect could be developed during the person's lifetime to the point that it would survive the death of his body and become a part, still self-identical, of a celestial intellect.4 Thus a human being of sound mind would have as his chief task in life the full actualization of his mental capacities, so that deprivation of his senses, his imagination, and his estimative faculty would leave him still able to think. An intellect fully developed in this way would not perish with the body, and the person's resurrection (macad) into paradise would amount to entering a self-conscious but bodyless state of eternal intellection-in-act. One would have reached the intelligible world contained in the lowest of the celestial intellects. This explanation was Avicenna's own, although it had something of the spirit of Plotinus and of al-Fărābi. It was thoroughly non-Aristotelian, and thus proved to be anothema not only to ordinary Muslims but also to pure Peripatetics such as Ibn Rushd.

The requirements of this sort of immortality greatly influenced Ibn Sina's theories. The two doctrines examined in the remainder of this paper both show its effect. In the first, a fairly straightforward modification was made to Aristotelian embryology. In the second instance, a radically anti-Aristotelian epistemological doctrine was adopted; neo-Platonic in appearance but unlikely so in inspiration, it lay at the heart of Ibn Sina's psychology and metaphysics. Both tenets were at root. I believe, philosophical responses to the Muslim precept of personal salvation; and they both had a place in the 'dialogue' between the falsisifa and the other groups of Muslim intellectuals. Indeed in the latter case, where Avicenna effectively denied the necessity and, rigorously speaking, even the possibility, of acquiring knowledge from experience, the doctrine should be considered one of the most important contentions in that debate as regards the consequences for philosophy and the other Greek sciences.

^{4.} This non-Qur'anic view is only adumbrated in the Shifa' (Kudh al-Nafe V· 5 and Hidhyydt 1X: 7 and X· 1), the complete, 'esotoric' teachings are presented in Al-Rirdia al-1dhawiyya fil-Ma'dd (ed. with Halian tr., introd. and notes by Francesca Lucchetta, as Epistola sulla vita futura, vol. I (Padua: Antenore, 1969)).

thought during that period. Let me note in this connection, without undue emphasis, that the title of the Kitāb al-Shifa' is to be translated as 'The Book of the Healing [of the Soul]' and the name of the compendium of that work, the Kitāb al-Najat, as 'The Book of the Salvation [of the Soul]'!

The first of the two particular problems that I have chosen to investigate illustrates the integration of a religiously motivated psychological doctrine into a different area of philosophy, in this case embryology, in order to render it more acceptably Islamic. The second and more important example, the question of the empirical basis of knowledge, is intended to exhibit the significance of psychological theory for the career of Islamic science in all four of the ways that I have just described – explicitly as regards the general question of knowledge, and implicitly, but I trust plainly, with respect to the other three. The second example, moreover, should isolate the part which was played by Avicenna's own psychological thought; and it should make clear a major way in which Ibn Sina's theories in psychology, acting through his philosophy as a whole, led towards a transformation of the Islamic philosophical tradition while coordinating it more closely with its Muslim surroundings.

Both problems will illuminate the relationship of Ibn Sinā to his Greek authorities, and the second will have a certain bearing on the vexed question of his 'mysticism'. The latter case, finally, will expose a serious but often unrecognized hazard that one frequently encounters when trying to determine Ibn Sinā's true position on some issue – a difficulty arising from his method of presentation, even in his most straightforward discussions. Incomplete, especially adumbrative, exposition rather than tentative or shifting views will turn out to be his vice.

The examinations below of the zoological and the epistemological topics will both follow the Shifā'. It is this work, indeed, which nearly always contains Avicenna's basic account of his doctrines, even though in certain cases the explanation there is disingenuous or incomplete, and a franker or more developed treatment must be sought elsewhere. In the present instances, certainly, the Shifā' appears to need no important corrections.

The two Avicsnman doctrines which are about to be considered were both consequences of the same basic Muslim belief, the idea of individual immortality and salvation. This tenet, stripped by Ibn Siuā of any notion of bodily resurrection (at least in his franker, or more esoteric, writings), was a cornerstone of his psychological and metaphysical thought. The framework of theory into which it had had to be placed, i.e., Aviceona's philosophical system as a whole, belonged in its methods and concepts to Greek philosophy in its Islamic guise, especially in the form it had taken at the hands of al-Fārābī (ca. 870-950). The teachings derived chiefly from Aristotle and occasionally from the Greek commentators, but they were also tinted – or tarred – with ideas from certain neo-Platonic works (including the pseudonymous 'Theology of Aristot-

themselves in a dialogue principally about philosophy and Our'anic religion. both among themselves and against the other interpreters of Islam. What I said earlier of the discussion in general is especially applicable here, namely, that a cluster of psychological issues assumed exceptional importance. The older questions of the definition of a believer, the nature of God's attributes, the createdness of the Our'un (largely replaced as a problem for the faldsifa by the createdness of the world), and freedom of the will had all been given stereotyped sets of answers by the teuth century. But other issues arose and demanded resolution; the nature of the soul; the distinctive characteristics of revelation. maniration, dreaming, prayer, and titual worship; the identifying criteria of true Prophethood (and thus of the basis for the Law - a vital matter for Islam); the personal immortality of individual souls, the manner of their salvation. and the nature of their bliss; the resurrection of the body, which was a prominent Muslim belief, but one that remained inexplicable within the limits of falsafa; the means whereby God can know particulars (and thus reward and punish individual believers properly, carrying out the 'Promise' and the 'Threat' of the Our'an); and the right mode and criteria of human knowledge. With the one significant exception of the eternity of the world, the major doctrinal problems that were set for the students of the ancient sciences by their Muslim environment required solution within one or another area of psychological theory. For Ibn Sina even political science reduced to an exercise in faculty psychology: the 'virtuous city' (i.e., the best political community) was conceived as a society ruled through a Law that had been revealed by a true prophet, and the true prophet he identified as a man whose soul had a special faculty, so extra, higher degree of intellect called the 'prophetic' or 'holy' intellect. and who, through the overflow from this powerful intellect into his imaginative faculty, could put into images that were suitable for the common people all the essential conceptions of the Law and the religion.

The history of philosophy and science in Islam, then, was very greatly affected by the development of psychological theory in several ways: through the transformation in the nature of philosophy, through the changing ideas of the purposes of an intellectual life, through the framing of doctrines concerning the origin of knowledge, and most basically through the handling of contentious issues in the philosophers' general debate against other intellectual groups. Psychological questions were crucially involved in the processes that shaped classical Islamic culture, and theorization about the soul and its functioning thus shared indirectly but decisively in fixing the destiny of Islamic science.

I hope I have sketched enough background to make my initial assertions more plausible and persuasive. What I can do now is only to paint in a very small bit of the foreground. I shall discuss certain aspects of Ibn Sina's psychology in order to show the pervasive influence it had in his philosophy and to reveal at the same time the importance of psychological issues in Islamic

emphasis in philosophy away from comulative investigation of the human and natural world towards metaphysical illumination (a change where the centrality of psychological questions has already been asserted) was in the end a metamorphosis wherehy speculative philosophy effectively distanced itself from the several scientific disciplines and left them more susceptible to theoretical stagnation and to futile elaboration of a positivistic sort.

Secondly, the philosophers convinced themselves that the highest philosophic and human good and the greatest happeness (sacida) was conjunction (ittifal) with a higher intellect. By so doing they very largely reduced moral philosophy to theoretical psychology, to discussion of this psychological state of quasi-union and the means of achieving it. Such a goal for the philosophical life would have appeared to most non-philosophers to be just a poor substitute for ittihād, the uniting with God depicted by the sūfi's, and this view most have had a considerable effect in channelling the interest of educated Muslim youths away from philosophy itself and all that much farther away from the scientific disciplines.

In the third place, classical Islam was characterized by the extraordinary prominence granted by the entire society to the question of knowledge ("ilm) of the kind of knowledge that a Muslim ought to accept as right and of the basis for certainty in that knowledge. But asking what knowledge is, in effect implied asking how knowledge is to be obtained; and that meant understanding the operations of the soul, Greek philosophy and science, suitably modified, formed one way of knowledge that was open to the Muslim believer. Apologists of the Greek sciences (al-culum al-ana'ıl) were forced by the internal constraints of philosophical theorizing and the external demands of legitimization in Muslim society, to explain the special nature of their sort of knowledge and the basis of its claims to truth. The burden of these explanations fell upon psychological theory. But the account that was produced, ris, human participation in a higher intellectual world, left philosophy without a 'religious' justification as convincing as that of the Qur'anically based disciplines or juff mysticism and without any good 'secular' substitute, such as, for example, a rigorous Aristotelian empiricism nught have supplied.

Finally and most generally, psychology influenced the development of Islamic science by its assumption of the leading rôle when in the tenth century the students of falsafa and the other Greek disciplines attempted to come to terms with their Islamic environment. This they did by entering into the general debate which I mentioned, where each of the several opposed groups of Muslim intellectuals represented a different attitude to the religion and a different approach to knowledge. The adherents of the Greek sciences engaged

³ See Franz Rosenthal, Knowledge Triumphons the Concept of Knowledge in Medieval Islam (Leiden: Brill, 1970); especially pp. 1-5 where something of Rosenthal's analytical framework is disclosed.

Nasir al-Din al-Tüsi (1201-1274) was able to effect through his exegesis of Ibn Sinā in the Sharh al-Ishārāt and elsewhere. The philosophical cursus, which in the ninth and tenth centuries comprised logic and mathematics, natural philosophy and the mathematicized natural sciences, metaphysics, and ethics and politics, retained with Avicenna something of the original Aristotelian regard for research and the cumulative development of knowledge. Afterwards, however, it became a mere propaedeutic, albeit an essential one, for a directly illuminative, and supposedly more valuable, kind of knowledge, eventually interpreted in the later Iranian school as mystical gnosis. Although I cannot discover a real mysticism present in Ibn Sinā's works, and certainly not in the frequently cited chapter on 'The Stages of Those Who [Seek to] Know' (Maqamāt al-ʿĀrifīn) in the Kitāb al-Ishārāt (ed. cit., pp. 198-207), nevertheless illuminationist features were decidedly prominent, and the ground for the fully mystical development was thoroughly prepared by Avicenna's philosophy.

The driving force behind this transformation of falsafa derived, I am convinced, from the philosophical investigation of the soul, or rather from the implications that psychological doctrines yielded in nearly all areas of philosophical enquiry. The same ultimately psychological issues were also present to the mutakalliman (the so-called 'rational theologians' of Islam) and the intellectually inclined among the suffi's - and indeed to all educated Muslims of those centuries. In the development of classical Islamic thought the primary task was the broadening and theoretical deepening of the Our anically based religious culture. So it is not surprising that there was a scarcely interrupted general debate among opposed groupings of Muslim intellectuals fundamentalist jurists, rationalist theologians, philosophers, suff's, and lama-'ilis, among others which had a great directive influence on the culture, and which very often addressed itself to matters in psychology. The question of the soul and the problems of right knowledge and right belief that were inseparably joined to it became and remained a fundamental concern, perhaps the most basic one of all, to Islamic thinkers. Psychological issues formed a vortex that eventually drew every theoretical system into its whorls, and usually threw it out again a shivered wreck. To understand the cultural history of medieval Islam it is essential to study the theories of the soul.

In a single paper one cannot document nor even illustrate all features of the description that has just been offered. But it seems appropriate to provide some indication of how psychological theories in the Islamic world had such importance specifically for the history of science. In brief, I find that there were four ways, all of them indirect. (Of course there was a direct way, too, for psychology after all had long been a part of 'science'!) First, the shift of

^{2.} These remarks were originally made in answer to a question asked from the floor by Prof. A.I. Sabra. They are incorporated here in their natural place in the text.

A Decisive Example of the Influence of Psychological Doctrines in Islamic Science and Culture:

Some Relationships between Ibn Sīnā's Psychology, Other Branches of His Thought, and Islamic Teachings

ROBERT E. HALL*

PSYCHOLOGICAL THEORY was a central concern of the medieval Islamic world, and Ihn Sinā¹ was a key figure in the history of Islamic thought. Appropriately enough then, psychology was a main focus of Ihn Sinā's own work, and his theories were of great importance in the history of psychology. Indeed, during the Middle Ages in Islam or in the West and, I am tempted to add, in the Renaissance, Ihn Sinā was rivalled as a psychological theorist only by Ihn Rushd (Averroes; A.D. 1126-1198). But if I am right in my thinking, Ihn Sina's psychology had a further significance in Islamic intellectual history; for much of Ihn Sinā's thinking revolved around the analysis of psychological issues; the philosophical system that he created signalled a turning-point in the history of philosophy and science and theoretical enquiry as a whole—even religious enquiry—in the Islamic world. So a correct grasp of Ibn Sinā's psychological doctrines is prerequisite, I believe, to any full analysis of Islamic intellectual history and, a fortiori, to a proper understanding of the course of Islamic science.

Ibn Sīnā's Shifā' was the longest systematic exposition of falsafa (by which I mean simply Islamic philosophy in the Grack tradition) to have been produced in the classical period. Yet in the Shifā' and in Avicenna's other philosophical works was contained potentially (and even actually, in the view of certain present-day scholars) a radical transformation of the Islamic philosophical tradition: witness the abuse that Ibn Rushd heaped upon Ibn Sīnā for abandoning pure Peripateticism and the strikingly mystical philosophy which

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^{1.} Ihn Sina (A.D. 980-1037) is the great physician and philosopher known in the West as Aviceons.

gold which is the goal of human life and which allows man to play the role for which he is destined, to act as the bridge between heaven and earth, as the eye through which God views His creation, as the channel through which the grace of heaven penetrates the earth and fecundates it. Through this inner alchemy, to which all other aspects of alchemy are subservient, man comes to see nature not as the chaos of coagulated matter but as the theophany which reveals the paradise which is here and now and which man must rediscover through the attainment of the gold which resides at the heart of all beings and which remains to be extracted by means which tradition offers to those who are willing to surrender themselves to it. Although Rāzī sowed the seeds of what was to become known later as the science of chemistry, Islam continued to harbor that spiritual alchemy which refuses to see nature as deprived of life, which aims at transmuting the inner being of man and attempts to bring about, through his transmutation, the spiritual revival of nature

Applied to nature, to'wil means penetrating the phenomena of nature to discover the noumena which they well. It means a transformation of fact into symbol and a vision of nature, not as that which wells the spiritual world, but sa that which reveals it.

Alchemy is precisely such a science, one based on the appearances of nature, particularly the mineral kingdom, not as facts in themselves but as symbols of higher levels of existence. It is not accidental that Jābir was both a Sufi and also a Shifite and that in fact the Jābirian corpus later became closely associated with Ismāfīliam which added certain treatises to the original body of Jābir's works.

Jähr, while also interested in natural occurrences, never divorced the facts of the natural world from their symbolic and spiritual content. His famous Balance (mizān) was not an attempt to quantify the study of nature in the modern sense but "to measure the tendency of the World Soul". His preoccupation with numerical and alphabetical symbolism, with the study of natural phenomena as determinations of the World Soul, with specifically alchemical symbols, all indicated that Jähir was applying the process of ta'wil to nature in order to understand its inner meaning.

Rāzī, by rejecting prophecy and the process of ta'wil which depends upon it, also rejected the application of this method to the study of nature. In so doing, he transformed the alchemy of Jābir into chemistry. That is not to say that he stopped using alchemical terminology or ideas, but in his perspective, there was no longer any Balance to measure the tendency of the World Soul, nor any symbols to serve as a bridge between the phenomenal and noumenal worlds. The facts of nature were studied as before, but as facts, not symbols. Alchemy was studied, not as real alchemy, but as an embryonic chemistry. The religious and philosophical attitude of Rāzī was therefore directly connected to his scientific views and was responsible for this transformation. In fact, his case marks one of the clearest examples of how philosophical and religious questions have played a role in many significant developments of science and in the history of science in general, displaying the intimate relation between man's view toward the sciences of nature and his vision of Reality as such.

Islamic civilization however rejected the philosophical views of Razi and his like and romained faithful to its own ethos and the burden which the hands of Providence had placed upon it, namely to bear the Divine Message of the Qur'an for mankind to the end of the world. This truth has allowed Islam to preserve to this day, despite all the viciositudes of time, the knowledge and practice of an inner alchemy which makes possible the cultivation of

Răzi and his rejection of the alchemical view, see Corbin (with the collaboration of S. H. Naar and O. Yahya), Histoire de la philosophic islamique (Paris, 1963) pp. 194-201. On the alchemy of Jābir see Carbin, "Le 'Livre do Glorieux' de Jābir ibn Ḥayyān (alchime et archétypes)", Eranos-Jahrbach (Zurieli, 1950).

Throughout these works, there is a description and classification of immeral substances, chemical processes, apparatuses, and so forth, so that these works could be easily translated into modern chemical languages. There is no interest in the symbolic aspect of alchemy, in the discussion of metals and their transformations as symbols of the transformation of the soul. The correspondence between the natural and spiritual worlds which underlies the whole worldview of alchemy! has disappeared, and we are left with a science dealing with natural substances considered only in their external reality, albeit the language of alchemy and some of its ideas are still preserved.

The reason for Rāzi's departure from the alchemical view must be sought in the peculiar philosophical position which he held. As we know from many later sources including Birūni, who was scientifically sympathetic with him. Rāzi wrote several works against prophetic religion and even denied prophecy as such. He thus rejected a central theme of Islamic philosophy which in fact is "prophetic philosophy". Moreover, Rāzi was particularly opposed to Ismā-'ilism and carried out a series of highly philosophical debates with one of the leading figures of Ismā-'ilism, Abū Ḥātim Rāzi. When the religious and philosophical attitudes implied by Rāzi's position are analyzed, it becomes clear why he transformed Jabirian alchemy into chemistry.

According to Islamic esotericism in general and Shi'sim – of which Ismā'ilism is a branch – in particular, the sciences of nature are related to the science
of revelation. Revelation possesses an exoteric (zāhir) and an esoteric (bāṭin)
aspect and the process of spiritual realization implies beginning from the
exoteric and reaching ultimately the esoteric. This process is called ta'nil or
hermeneutic interpretation, which is applied by the Shi'sh, and also in Sufisin,
to the Holy Quran, in order to discover its inner meaning. Only prophecy and
revelation can enable man to make this journey from the exterior to the interior, to perform this ta'inil which also means a personal transformation from
the exterior man to the inner one.14

world view, there was no completely secularized domain of nature to which a totally "non-symbolic" science could apply. Therefore, although much chemistry was contained in the medieval alchemical tradition, especially in the case of Rāsī, it was never totally divorced from alchemy.

The Strr al-earde was translated and thoroughly studied by J. Ruska, Al-Ram's Buch Cohermets der Cohermanisse (Berlin, 1937).

15. Concerning this correspondence see T. Burckhardt, op.cst.

16. One of Razi's famous works on this subject is the Refutation of Prophecy, (al-Radd 'ala't-nubuwwah) See Birthel. Epitre de Berunt contenant le repetture des ouvrages de Muhammad b. Zakariya al-Razi, trans. et ed. P. Krans. (Paris. 1936).

17 See P. Kraus, "Razinus", Orientalia, 4 (1935), 300-334; 5 (1936), 35-56, 358-370. The complete debate between the two Râsi's, which centers mostly around the question of prophecy, rais throughout the many chapters of A'lâm al-nubuceauh (Peaks of Prophecy), ed. by S. al-Sawy and Ch. Azvanz, (Tehran, 1977) Later Isma'ill authors such as Hamid al-Dia Kirmani in his al-laged al-dhakabiyyah and Nāsiri Khusspay in his Jāms' al-lakastayn were to continue this debate.

18. This theme has been thoroughly studied in the many writings of H. Corbin. As far as it concerns

And in fact, there is both similarity and difference when their alchemical and chemical ideas are compared.

Jabir believed that the elixir contained animal and plant substances as well as minerals, while Rāzī limited it to minerals and only casually mentioned animal and plant substances. Rāzī divided metals into seven species including khārṣini just like Jābir in his Kitāb al-khamsin. However, contrary to Jābir, Rāzī showed no interest in the numerical symbolism connected with this division. Jābir sought to discover the ultimate causes of things, while Rāzī, following the views of the Peripatetics among the physicians, denies openly that such a possibility exists. Rāzī in his al-Madkhal and al-Asrār did not follow the Jābirian view that minerals are composed of sulphur and mercury but believed that they are constituted of body (jasad), spirit (rūh) and soul (nafs). However, the Jābirian belief that there are five principles—the first substance, matter, form, time and space—certainly bears close resemblance to the famous five eternal principles of Rāzī. 10

Rāzī also closely followed the terminology of Jābirian alchemy. He adopted not only technical names from Jābir but also titles of books. A large number of Rāzī's writings in this field bear the same titles as those of Jābir, while some are simply modifications of names of works belonging to the Jābirian corpus. This is particularly significant in the case of such an independent philosopher as Rāzī. Even in the classification of simples ('aqāqīr), which is among the most important scientific achievements of Rāzī in the field of chemistry, he followed the example of Jābir's al-L'stuqus al-uss al-awwal.

One may then ask why Razi's works have been called the first books of chemistry in the history of science. We have several extant alchemical works of Rāzi, such as al-Madkhal al-ta-limi which served as a basis for the section on alchemy of Mafātih al-culām, and most important of all, the Sirr alasrār, well-known to the Western world as Liber Secretorum Bubacaris.

- 7 Kraus, op. cit., p. 3.
- 8. Krans, op. cit., p. 95, clies from Rasi's Kitch ol-khawdss to this effect.
- 9. Stapleton, op. cit., pp. 320 ff
- 10. Kraus, up. cit., p. 137 Regarding the five eternal principles of Rāzī and bis general philosophical views, see R Walson, Greek into Arabic, pp. 15-17.
- 11. Stupleton, op. ett., op. 336-337, where he cites infecen works of Razī which have either identical or modified titles of works of Jabir and seem to deal with the same subject
 - 12. Stapleton, op. cit., p. 329
- 13. The text of this work has been translated with commentary by Stapleton in the shove-mentioned articles.
- 14. This work, whose title may have also been Kutö al-sir as cited by Ibn al-Nadim, is the most hand work of Råsi on chemistry, one in which the transformation of alchemy into chemistry may be clearly discerned. It was well-known during the later centuries in the Islamic world not only in its original Arabic version, but also in a Persian reconsion, and it was also influential in the West. But everywhere it was considered an alchemical work rather than a chemical one because, in the medieval

terials wed to the crafts and guilds.² Yet, it was also in Islam that the first seeds of a science of chemistry were sown, although the symbolic view of nature predominated and never allowed a secularized view of material substances to become dominant, for it is not possible to have a chemistry until the living body of nature has become converted into a cadaver and until nature has become deprived, for him who has lost the symbolist spirit, of the sacred presence which nevertheless continues to glow within all things.

The appearance of chemistry is related to the birth of a school of philosophy at the margin of Islamic intellectual life, and is bound to a change in intellectual perspective which corresponds directly to the profound difference between the world views of alchemy and chemistry. Moreover, the creation of this peripheral philosophical school and the birth of chemistry belong to the early period of Islamic history and concern two of the most famous figures of Islamic science, namely, Jābir ibn Hayyān, the Latin Geber (d. 3rd/9th century), and Muhammad ibn Zakariyyā' Rāzī, the Latin Rhazes (d. 4th/10th century).

No two figures are better known in the annals of Islamic alchemy than these two men of many-sided genius. Both men were calchrated masters of alchemy. Both are believed to have belonged to the same school by later generations of alchemists in the Islamic and Western world. Yet a study made of the writings of both men clearly reveals that although Rāzī employed the languages of Jābirian alchemy, he was in reality dealing not with alchemy but with chemistry. One night even say that Rāzī transformed alchemy into chemistry, even though alchemy endured long after him and chemistry continued to be cultivated in the Islamic world within the bosom of alchemy. Thus the chemistry of Rāzī was by no means independent of alchemy, and in fact the two never parted ways completely in Islamic civilization as was to happen in the West after Robert Boyle.

Before discussing the philosophical and religious divergences between Jābir and Rāzī which led also to the separation of chemistry from alchemy, it is worthwhile to note the similarities and differences in the alchemical views of the two authors. Or rather, a comparison must be made between the Jābirian corpus, of which certainly much was written by Jābir himself and some of the treatises added later by Ismā^cīlī authors, and the writings of Rāzī. Scholars studying these writings differ as to how closely Rāzī followed Jābirian alchemy^e

^{3.} See H. Corbin, En Islam transien, vol. 1V, (Paris, 1978), pp. 205 ff.

Ruthat al-linkim considers Wast to be a through of the school of Jabir, while in almost all Latin
alchemical texts the names of both men appear as unquestionable masters of alchemy.

See G. Heym, "Al-Rant and alchemy", Ambix, 1 (1938), 184-19.; and J. R. Partington, "The Chemistry of Rant", Ambix, 1 (1938), 192-196.

^{6.} For example, P. Kraus in his Jöbir ibn Hayyan, vol. II, pp. 3 ff., does not believe that there is any direct and close relation between them, while N. F. Stapleton in "Chemistry in "Iraq and Persia in the Tenth Contrary A.D.", written with R. F. Azo and M. Hidayat Huwan. Memoirus of the Asiatic Society of Bongal, 1927, pp. 317-415, considers Ran, as a direct disciple of Jahir

Islamic Alchemy and the Birth of Chemistry

SEYYED HOSSEIN NASR*

A LCHEMY is at once a science of the cosmos, or cosmology, a sacred science of the soul, or psychology, a science of materials and a complement to certain branches of traditional medicine. It is not a proto-chemistry although it deals with physical materials from a particular point of view; nor is it the origin of the modern scientific method-although alchemy has been concerned in the profoundest sense with experiment and experience, that inner experiment which alone leads to certitude and of which all external experience is but a pale shadow.1 The traditional alchemist serves as the window through which the light of the spiritual world shines upon the natural domain and the revivifying air or more precisely ether of the empyrean penetrates the arteries of nature. His aim is not to work with sheer material substances from a nurely physical point of view, this being the work of charcoal burners. Rather, he aims to transform nature in order to return nature to that primordial perfection. that paradisal beatitude which nature is in reality, although this face of nature remains veiled and hidden from the view of modern man. Through the transmutation, based upon a sacred science of things, of the soul of the beholder to pure gold, alchemy permits the solar element or the supernal Apollo to shine upon the world of the gross elements and their compounds.

These general remarks on alchemy pertain as much to Islamic alchemy as to the Alexandrian or Lutin schools, for all schools of traditional alchemy share ultimately the same world view and even the same symbolic language; although each of course possesses certain distinct characteristics, Islamic schemy inherited at once Alexandrian and Chinese alchemy and created that immense synthesis. The translation of some of their fruits into Latin in the form of such texts as the Turba Philosophorum and Picatrix² brought Latin alchemy into being

Islamic alchemy has managed to preserve over the centuries and even to our own day an integral spiritual alchemy wed to Sussm and other esoteric schools, such as that of the Shaykhis in Persia, and a symbolic science of ma-

[&]quot;The Iraneau Academy of Philosophy, 6 Nexami Street, Avenue Français, P. O. Box 14, 1699, Tehran, Iran.

¹ On the alchemical trudition and its spiritual significance see T. Burckhardt, Alchemy, Science of the Cosmas, Science of the Soul, trans. W. Studdert (Baltimore, 1971), and E. Zolla, Le meravigle della natura - Introduzione all'alchimia (Milan, 1975).

On Islamic alchemy see S. H. Neer, Islamic Science - An Illustrated Study (London, 1975), pp. 193 ff., and S. H. Neer, Science and Civilization in Islam (New York, 1970), pp. 242 ff.

ment to a Jewish prayer book published in Venice in 1520 we learn that R. Abraham ben Yom Tov Yerushalmi used the tables of Ulugh Beg. It is otherwise known that this R. Abraham was in Istanbul in 1510.²³

10. As a result of a comprehensive search of manuscript collections for Hebrew astronomical tables, some of the fruits of which have been presented here, it now appears that Levi ben Gerson (southern France, d. 1344) was the only Hebrew author to construct tables based on original models, rather than modifying or copying existing tables.24 Moreover, his tables are embedded in a text that describes his models and their derivation from specified observations. In most other cases we find an introduction preceding the tables in which only the procedures for using them are indicated-this holds true for a large number of Islamic tables as well as those in Hebrew. Levi was certainly indebted to his Muslim predecessors, particularly al-Battani whom he often cites as his source for tables representing Ptolemy's models. Levi also mentions al-Bitruij but rejects his models categorically, preferring to take those of Ptolemy as his point of departure. In a general sense Levi's entire research program was an outgrowth of the Arabic scientific tradition, for his goal was to construct a system that was philosophically sound and mathematically rigorous. This view was expressed by a number of his predecessors including Ihn al-Haytham (Egypt, eleventh century), Ibn Bājja (Spain, twelfth century), Averroes (Spain, twelfth century), and al-Bitrūjī. Carrying through with these ideas. Levi not only originated new planetary models, but proceeded to construct new tables, based on his models. Although Levi's astronomical treatise was translated into Latin, the extant manuscripts of that version contain few of the tables that belong to it.

Conclusion: We can see that the process of transmission is complex and that it is not always the result of a specific plan. Some translators, such as Moshe Ibn Tibbon, had clear goals to bring a certain literature to the attention of a recognizable group. 25 but in most cases we have too little information to make an informed judgment of the translator's motivation. What seems to emerge is a sense that in the late middle ages astronomy took on the character of an international enterprise despite the language barriers that separated its practitioners.

^{33.} B R. Guldstein, The Astronomical Tables of Levi ben Gerson (Hamden, Ct., 1974), pp. 75-76.

^{34.} On Lovi, see Goldstein (op.c.i., n. 33). In addition to the Hebrett mannicripts listed their (pp. 74 ft.), I have found a Gentra fragment of Levi's Astronomy, chapters 97 and 98 (corresponding to Paria Hb. 724, fol. 177a, 24 to 178a, 14 and sociuding the marginal note on 178a) in Jewish Theological Seminary of America, Ms. ENA 2905, fol. 1.

^{35.} On Mosha Ibn Tihbon, see D. Romano, "La transmission des sciences arabes par les juife en Languedoc", in Juife et judaisme de Languedoc, eds. M.-H. Vicaire and B. Blumankranz (Toulouse, 1977), pp. 363-386. For biographical enformation on a fourteenth century translator, see L. V. Berman, "Samuel Ben Judah of Marseilles", in Jewish Medieval and Romansance Studies, ed. A. Altmann (Cambridge, Mass., 1967), pp. 389-320.

al-Shaur or his models, they do yield information on other important aspects of late Islamic astronomy, and one may yet find references to Ibn al-Shairand the Maragha School in Hebrew.* The main center for Islamic astronomy in the lifteenth century was the observatory in Samarquad in Central Asia established by the Mongol ruler Ulugh Beg, himself a noted astronomer.14 The scientific legacy of Samargand reached Istanbul, where the study of astronomy flourished in the sixteenth century, and there is now some evidence that this tradition also reached Italy. A Hebrew manuscript (Paris 1091) uniquely preserves an anonymous undated Hebrew translation, without the introduction. of Ulugh Beg's tables originally composed ca. 1440, and indeed the observatory at Samargand is specifically mentioned in it (folio 70a); "Table for half-daylight for the latitude of Samargand at the place of the observatory" (ha-rasad). Although the planetary tables are taken from Ulugh Beg's work, the star catalogue in this manuscript is not the famous list that became known to western scholars in the seventeenth century.19 but an older list presumably from a Hebrew source because its epoch is given in the text as "the beginning of the sixth millenium", i.e. 5000 A.M. (anno munde), which corresponds to 1240 A.D. Both Arabic and Hebrew names are displayed for each of the 50 stars together with their longitudes, latitudes, and magnitudes (folios 73a-74a). In an unpublished description of this manuscript on deposit at the Bibliothèque Nationale in Paris, M. Georges Vaida dates this copy by means of paleographic evidence to about 1500 A.D. Based on the watermark which is a simple anchor I am confident that the paper was produced in Venice between 1477 and 1508.14 The pages are arranged in quires of 12 folios numbered in the upper loft corner, e.g. on folio 13a we find 2:1 (in Hebrew alphabetic numerals) meaning quire 2, folio 1, on 14a we find just the numeral 2, and so on to 18a where we find the numeral 6: then on folio 25a we find 3:1. The keeper of Hebrew manuscripts at the Bibliothèque Nationale informed me that this arrangement is typical for Italian manuscripts of this period." Italy, of course, was an important scientific center at the time and it is possible that knowledge of eastern Islamic astronomy was brought to the attention of Christian scholars by Jews. Ulugh Beg is mentioned in a few Hebrew texts deriving from Istanbul and I think it most likely that this translation was made there in the latter half of the fifteenth century. Steinschneider noted that Elia Bashyası (d. Israubul 1490) mentioned Ulugh Beg's tables in a work published in Istanbul in 1530/1,12 and in a supple-

^{28.} See Kennedy (op.cit., n. 2), pp. 166 f. A. Sayili, The Observatory in Islam (Anhara, 1960), pp. 259-305

²⁹ See E. B. Knobel, I high Beg's Latelogue of Stars (Washington, 1917), superally p. 9.

³⁰ Cf \ Moslim. Anchor Watermarks (Amsterdam, 1973), especially plote 19, no. 228, Agother text to Lound with these tables to form Pars Mt. Hb. 1091, and its paper has a completely different watermark

Cf. M. Best Arie, Hebrew Codicology (Paris, 1976), p. 48.
 Steinschneider /ap.cu., n. 1), p. 196.

^{*} Vote added in proof to July 1979 I discovered a copy of Ibn al-Shāṭir's aij al-jadīd in Hehrev characters JTSA Mix 2580 (cf. Ms. Oxford, Bodleian Arabic Arch. 5eld A 30). A note on the fiscal in the vame hand as the rest of the manuscript gives the solar, lunar, and planetary radices for 1260 AB (1844 AD) for Aleppo, and on internal evidence it seems to be a numeteenth century copy: in the mean motion tables rutters are listed for 750, 980, 1050, 1280, 1280, 1290 AB (c. g. fal. 16b). Thus certainly suggests that the copyist (or his mentor) lived in the thirteenth century of the Hijra, the the ameteenth century of the Christian era. It is surprising to find such a late copy of this text is Hebrew characters.

geographical coordinates are given as 72°E, 38°N. 42 Shelomo ben Elivahu had the nickname "golden sceptre" (sharpit ha-zahar), an allusion to Esther 4:11. and Steinschneider conjectured that there was an intention to find a biblical parallel to the Greek name Chrysococces; 10 this seems to be confirmed by the character of the text. In the introduction to the Hebrew version (Paris, Ms. Hb. 1042) we learn that the tables are arranged for the city Tivini (read: Tabriz) whose longitude is 72° rather than for Saloniki whose longitude is given as 493°. The mean motions are displayed for Persian years and months with radix 720 Yazderird, i.e. 1350 A.D. The tables for the planetary equations are all derived from the Almagest, but in a form introduced by Islamic astronomers that Kennedy has called "displaced (Ar. nud"i) equation tables".24 As in Ptolemy five functions are tabulated for each planet, but here some are displaced vertically to eliminate pegative entries, some horizontally, and some both vertically and horizontally such that the resultant equations are in agreement with Ptolemy's values. For example, Jupiter's first correction (fol. 64b) which is due to the argument of longitude (or centrum) is tabulated at degree intervals where the entry for 00 is 4:270, the maximum entry 11:150 corresponds to arguments 246° to 252°, and the minimum entry 0:45° corresponds to argumenta 70° to 78°. These values derive from the Almagest XI, 11, columns 3 and 4 with horizontal shift of 180 and a vertical shift of 60; e.g. Ptolemy's value for an argument of 18° is -1;33° and 6° - 1;33° = 4;27°, the entry for argument O in our table. Jupiter's second correction (fol. 65a) which is due to the corrected anomaly is given at degree intervals where the entry for 0° is 12°, and the maximum entry 23:30 corresponds to arguments 990 to 1030. All the entries are exactly 12° greater than the corresponding values in the Almagest XI,11, column 6. Kennedys showed that these displacements must satisfy an algebraig relationship; the sum of the vertical displacements equals the horizontal displacement, in this case 60 + 120 = 180. This technique was already in use in the ninth century by the Muslim astronomer Habash al-Hāsib and continued with many variants throughout the middle ages.28

9. There has been considerable interest in the possibility that eastern Islamic scientific material reached Europe at the time of Copernicus because his models resemble quite closely those of Ibn al-Shātir (Syria, fourteenth century).²⁷ Although the Hebrew texts I have studied do not allude to Ibn

^{22.} Pingree (op.cit., n. 21) pp. 145-144.

^{28.} Steinschneider (op.eit., n. 1), p. 179.

^{24.} E. S. Kennedy, "The Astronomical Tables of Ibn al-A'lam", Journal for the History of Arabic Science 1 (1977), 14.

^{25.} Kennedy (op.cit., p. 24), p. 15.

²⁶ Kennedy (ap.cu., n. 24), pp 16 f; H. Sakan and E. S. Kennedy, "Solar and Luner Tables in Early Islamic Astronomy", Journal of the American Oriental Society 87 (1968), 492-497.

²⁷ Cf. Imad Ghanem and E. S. Kennedy (eds.), The Life and Work of Ibn al-Shifter (Aleppo, 1976).

pended his own tables to this text, but they are unrelated to the Alfonsine Tables. The Hebrew translation of the Alfonsine Tables was not made until 1460 when Moslie ben Abraham de Nîmes translated them from Latin in Avignon together with the Latin introduction of John of Saxony (early fourteenth century), and so the Hebrew version is of no help in recovering the early history of the text." There is another text in Hebrew, called the Paris Tables, based on the Alfonsine Tables and computed with radix 1368.17 We read in this treatise that it was translated by Solomon ben Davin de Rodez in southern France (a punil of Immanuel Bonfils of Tarascon), although no Latin title or author is cited. These tables are very extensive and make use of double arguments for finding the planetary longitudes and latitudes.10 Some Latin texts are related to it: the carliest set of tables of this character are those of John of Lignières who worked in Paris about 1320. Although the principles underlying the computations are the same, all the entries differ because of a difference in convention. The entries in the planetary tables in this Hebrew text are, however, identical with those in an Oxford text by Batecombe (?) with radix 1348.19 No copy of this Oxford text has been found in France, and no Latin version with radix 1368 and arranged for Paris, Lyons, and Ayignon (as in the Hebrew version) is known.10

8. There were also translations of scientific works from the eastern Islamic world into Hebrew. Shelomo ben Eliyahu of Saloniki (fl. 1374-86) translated a text, called *The Persian Tables*, from Greek into Hebrew where the ultimate sources are the Sanjari Zij of al-Khāzini (ca. 1120) and the "Alā"i Zij of al-Fahhād (ca. 1150).²¹ The author of the Greek text, George Chrysococces, is not identified by Shelomo ben Eliyahu. In a passage written shortly after 1347, George Chrysococces tells us that he studied Persian astronomy with a Greek priest in Trebizond from whom he learned that a Greek scholar, Chioniades, had traveled to Persia to study astronomy and had brought back a number of texts which he then translated into Greek. Chrysococces wrote a commentary on these Persian tables of Chioniades which were constructed for Tabriz whose

^{16.} On Moshe ben Abraham de Nimea, see Steinschneider cap.cat., u. 1), pp. 196 f.

¹⁷ I have consulted two copies of the Paris Tables, Manich, Hb. 343, fols. 104-157, and Oxford, Bodicion, Ms. Reggio 14, fols. 57-103. There is a Hebrew commentary on these tables by Moshe Faristel Botarel (southern France, on. 1465), of Oxford, Bodician, Ms. Hb. 2022.

¹⁸ Cf. M. J. Tichenor, "Late Medieval Two-argument Tables for Planetary Longitudes", Journal of Neur Eastern Studies 26 (1967), 126-128.

¹⁹ North (op.cs. n. 15), pp. 279 and 299 (n. 40). I have consulted two copies of the Latin venion of these tables. Oxford, Bodiesan, Ms. Rawlinson D.1227, fols. 64r-87r; and Bodiesan, Ms. Laud Miss. 594, fols. 51r-81v.

^{20.} Private communications from J. North, University of Groningen, and E. Poulle, Ecole Nationals des Chartes, Paris.

^{21.} On Shelono han Eliyahu, see Steinschneider (ap.cit., p. 1), pp. 178 ff. For the Greek version of the Persian Tables, see D. Piagree, "Gregory Chianuades and Palacologan Astronomy", Dumbares Oaks Papers 18 (1964), 135-160.

method of Maestro Campano for the meridian of Rome and Novara" (cf. TCD 491; Tabula equationis lune). At the end of the Hebrew manuscript (folio 129b) one finds a page in Latin script but probably in Spanish; there is no heading and the few words are all technical terms: Abril, Mayo, dias. altitud, etc. It contains a somewhat confused version of a table of noon solar altitudes deriving from an Arabic of Hebrew original; in each entry the minutes precede the degrees indicating a thoughtless transcription from a script written from right to left. This table obviously was not taken from Campanus, and its source is unknown to me.

TABLE I

Paris Hb. 1102, 31a-32a
Mars [in Latin, Hebrew, and Arabic]
Table for the mean motion of Mars in
collected Christian years for the
meridian of Novara in Italy

Radix 2° 17;46,15,0,0,0,0° 28 1° 7;6,34,49,5,29,27°

56 11° 26:26.54.38.10.58.54°

TCD, 63r Tabula medii motus martis in annis domini iesu christi

> 2° 17;46,15° 1° 7; 6,35° 11° 26:26,55°

ad meridiem nonarie.

1512 1 12;4,5,10,56,30,18

1" 12:4.5"

7. The Alfonsine Tables were probably the most widely used tables in late medieval and renaissance Europe. The original form, based on Islamic models, was written in Spanish in the thirteenth century, but they were better known in the Latin version that appeared in the early fourteenth century. Indeed the Spanish form does not seem to have survived. A Hebrew text by Isaac Israeli (ca. 1310), Yesod Olam, provides us with some background information: Isaac ben Sid, a Jewish astronomer who worked for King Alfonso of Castile, observed a solar celipse in Toledo on 5 August 1263 to be about 7 digits in magnitude and he noted that the times of the eclipse phases were all a quarter-hour prior to the times predicted by the tables available to him (the Toledan Tables?). He also observed three lunar eclipses at the request of King Alfonso: 24 December 1265, 19 June 1266, and 13 December 1266. The discrepancies between observation and calculation were undoubtedly presented as part of the justification for constructing a new set of tables. Issae Israeli ap-

^{13.} J. North, "The Alfonsiae Tables in England", in Prismute Fesischrift für Willy Hartner, eds. Y. Maeyama and W. G. Saltzer (Wiesbaden, 1977), p. 271.

^{14.} Isaac Izmeli, Liber Yesod Olam, eds. B. Goldberg and L. Rosenkrana (Berlin, part 1, 1848, part 2, 1846), part 2, 465-47a.

^{15.} Isaac Intach (op.ca., n. 14), part 2, 11b.

to al-Battani in later Hebrew texts seem to derive from Bar Hiyya's adaptation rather than from a direct translation of the text. These tables were very popular in Hebrew, and they played much the same role as did the Toledan Tables for the Latin world-bringing technical astronomy to a new scientific community. It is puzzling that manuscripts of Bar Hiyya's Tables also contain tables ascribed to Abraham Ibn Ezra who lived somewhat later in the twelfth century. For example, one finds two tables of solar declination: one based on Ptolemy's value for the obliquity, 23,51,20°, ascribed to Abraham Bar Hiyya; and one based on the improved value, 23;33,8°, ascribed to Abraham Ibn Ezra. There are also many explanatory notes of a relatively trivial character written in the margins that are ascribed to Ibn Ezra as well. I have not found a separate set of tables in Hebrew composed by Ibn Ezra, though there are indications that they once existed."

5. Al-Battāni's tables were also the basis for the popular tables, called *The Six Wings*, by Immanuel Bonfils of Tarascon (southern France, fourteenth century) who mentions his debt to his Muslim predecessor in the introduction.¹⁰ These tables for computing conjunctions, oppositions, and solar and lunar eclipses use the Hebrew calendar with its nineteen-year cycle. Curiously, they were translated into both Latin and Byzantine Greek.¹⁴ In this instance computations based on Ptolemy's models went from Greek into Arabic into Hebrew and then back into Greek.

6. Another set of tables related to those of al-Battani can now be identified. A unique copy in Paris (Bibliothèque Nationale, Ms. Hb. 1102) contains an Arabic text in Hebrew characters that derives from the Latin text of Campanis of Novara (Italy) composed in the thirteenth century. This version in Hebrew script is anonymous and undated but seems to be from the fourteenth century. Its most important difference from the Latin version, at least the copy consulted by G. J. Toomer (Ms. TCD: Trinity College Dublin, D. 4.30), is that here the mean motions are expressed to six sexagesimal places whereas in the Latin they are only given to seconds (see Table I). Campanus is mentioned in the Hebrew text (folio 93a): "Table for the equation of the moon according to the

⁹ Cf. J. M. Millás Vallicross (op.cu., n.8), p. 189 f.; and viem, El libro de los fundamentes de los Toblas entronomicas de R. Abraham Ibn Esra (Madrid-Barcelona, 1947), pp. 59 ff.

^{10.} The Riebrew text was published (Zhitomir, 1872), and a large number of manuscripts survive. Among the copies consulted in the course of this study is a fragment from the Cairo Ganiza. Strashours Ms. 4845, fold. 20-22 (on fol. 22n the heading is faint but legible, "wang two").

^{11.} On the Greek version of Bonfils' tables, see P C Solon, "The Six Wings of Immanust Bonfils and Michael Chrysofiokkes", Centaurus 15 (1970), 1-20. The only copy of the Latin translates is Florence, Billioteca Nazionale, Ms. J IV 20 (the tables are on fols, 160r-182r). Despite the extalogue, Ms. Manich rod. Join, 15954 is a Hobrew copy of these tables in which the headings were translated into Latin.

^{12.} I wish to thank G. J. Toomer, Brown University, for providing me with a detailed comparison of Ms. TCD with my notes on Paris Hh. 1102. This Latin manuscript is noted in F. S. Benjamin, Jr. and G. J. Toomer, Campanus of Novero and Medison! Planetory Theory (Madison, 1971), pp. 15-16.

star catalogue, and in most cases few of the figures were drawn. A partial exception is Paris Hb. 1019 (Anatob's version) which has the chord table in Book I but otherwise, although lines are drawn for tables, no entries appear.* One wonders how working astronomers were able to make sense of the translation.

- 2. Southern France was the major center for translations from Arabic into Hebrew in the thirteenth and fourteenth centuries, and most of the texts that were in common use in Spain became available in Hebrew at that time. For example. Moshe Ben Tibbou, mentioned above, translated al-Buruit's On the Principles of Astronomy, written to Spain about 1200 A. D. A Latin version by Michael Scot is also extant but it is much freer than the Hebrew. Al-Bitroji attempted to harmonize Aristotelian cosmology with Ptolemaic astronomy by placing the geometric models for planetary motion on the surface of spheres rather than in the plane of the coliptic. A number of later astronomers (some writing in Latin and others in Hebrew) found a variety of shortcomings in this synthesis and it was ultimately rejected. Several other scholars attempted to construct spherical models: for example, Joseph Ibn Nahmias (Spain, fourteenth century). His treatise was composed in Arabic (the unique surviving copy, in Hebrew characters, is Ms. V: Vatican Hb. 392), and translated into Hebrew anonymously (Ms. B. Oxford, Bodleian, Canon Misc. 334). His system was intended to be an improvement on that of al-Birroji, whom he cites (Ms. B 126v, 9, Ms. V 52b, 12), but the text awaits detailed analysis
- 3. Another author whose work survives in Hebrew and Arabic versions is Joseph Ibn al-Wakkär (Spain, fourteenth century). He composed a set of astronomical tables for Toledo in Arabic and translated the introduction into Hebrew himself. In the unique surviving copy (Munich, Ms. Hb. 230) the Arabic text is in Hebrew characters and the Hebrew translation follows the Arabic. In the introduction Ibn al-Wakkär mentions the tables of Ibn al-Kammād which do not survive in the original Arabic, but only in a Latin version. Ibn al-Wakkār's zīj is not mentioned in Kennedy's Survey of Islamic Astronomical Tables (1956).
- 4. The earliest set of astronomical tables in Hebrew are those of Abraham Bar Hiyya composed in Spain in the twelfth century." His introduction is largely based on the introduction to al-Battāni's zij (Syria, ninth century), and the tables agree very closely with those of al-Battāni as well. Indeed, the references

⁵ On folios 209b, 227b, etc., of Paris Hb. 1019 we find notes by Abraham ben Yom Tov Yernshalmi who fived in Istanbill in the sixteenth century (see paragraph 9, below).

^{6.} See B. R. Goldstein, 41-Bitraff on the Principles of Astronomy, 2 vols (New Haven, 1971).

J. M. Millás Vallicrosa, Las Traducciones orientales en los manuscritos de la Biblioteca Catedral de Toledo (Madrid, 1942), pp. 231 ff.

The introduction together with an excerpt from the tables was published by J. M. Millás VallicroLibro del calculo de los movimientos de los astros de R. Abruham Bar Hiyya Hu-Burgelom (Barcelona, 1959).

new light on many aspects of Atabic science, and this will be illustrated here by concentrating on a few texts that I have studied in the past few years, several of which have been identified for the first time.

1. The translations from Arabic include works originally written in Greek such as Euclid's Elements and Ptolemy's Almagest. There are even two conies of the Arabic Almagest in Hebrew characters out of some ten extant comes: a complete copy with all the tables in a beautiful manuscript in Paris (Bibliothèque Nationale, Ms. Hb. 1100), and an incomplete copy in Cambridge (University Library, Ms. Mm 6.27 (8)), Another manuscript (Vatican Hb. 392, folios 1-49) has been described as a copy of the Arabic Almogest in Hebrew characters, but in fact it is only a summary of it. The headings suggest that it is Ptolemy's work, for example we find "Book Four of the Almagest" (folio 5h), but later we find the heading "Book 7 and 6" (folio 28b), i.e. the entire discussion of the star catalogue is combined Steinschneiders had queried whether this might be a copy of Tusi's thirteenth century recension of the Almagest, but a comparison with British Museum Ms. Ar. Reg. 16 A VIII excludes that possibility, and the author of this text remains unidentified. There were two translations of the Almagest into Hebrew, one by Jacob Anatoli in Italy and the other by Moshe Ben Tibbon in southern France, both of whom lived in the thirteenth century. I have looked at quite a few copies of these translations and have been surprised to find that almost none of them has tables or the

including a few tables, by Yosef ben Yefet Halevi (fourteenth century) with a Hebrew translation, (2) a version of the air of al-Fárisi (Yomen, thirteenth century) with tables, and (3) the Tashil al-Majusi by Thabit Ibn Quira On the sil of al-Farisi, see E. S. Kennedy, 4 Survey of Islamic 4stronomical Tables. in Transactions of the American Philosophical Society, NS 46 (1956), p. 132. Acabic manuscripts of this wij are found in Cambridge (University Library, Ms. Cg 3.27) and Istanbul of M. Krause, "Stambulet Handschriften islamischer Mathematiker", in Quellen und Studien zur Geschichte der Mathematik, Astronomie, and Physik, Abt. B, Vol. 3 (1930), p. 491. Two additional Arabic copies in Hebrew thatacters are preserved. Berlin, Ms. Hb. 682 Qu (ef. M. Steinschneider, "Schriften der Araber in behitischen Handschriften", Zruschrift der deutschen morgenländischen Gesellschaft 47 (1893),355), and Jewish Theological Seminary of America, Ms. 11h Micr. 2650 (the text is incomplete and only one table appears). F. Klein-Frunke has given a brief description of a fragmontary Yemenite copy in Hebrew characters of al-Biruni's Elements of the Art of Astrology , Kiryut Sofee 47 (1972), 720, in Hebrew). Combridge University Library Ms. Add. 1191 contains two texts in Arabic written in Hebrew characters in a Yememite band. The first text is another copy of al-Kharaqi's. Kudh al-iobjira. (folios l-18b): both the beginning and the end of this treatuse are musting to this copy (cf. (h) shove). The second text to Jahir the Affah's Islah al-Majisti (folios 19a-131a), and its colophon (f. 131a) gives the date of the copy as 1665 Seleucid Lea (1354 A. D.), the beginning of this treatise is massing here. Another Arabic copy of this treatise in Habrew characters is found in British Library Ms. hab. Or. 10,725 folios

^{3.} P. Kunttasch lists uine copies of the Arabic Almagest in Der Almagest: Die Synsaxis Mathematica des Claudius Ptelemaus in arabisch-latanischer Überlagferung (Wiesbaden, 1974), pp. 34-46. The Cambridge manuscript, which is not mentioned there, follows the Jahjaq-Thälut version for the most part, but the Hajjaj version for Book VII 2-4 (cf. Kunitssch, pp. 131 ff.). The star catalogus is missing side most of the tables come at the end, following Book XIII.

^{4.} M. Steinschneider (ep. cft., n. 2), p. 359.

The Survival of Arabic Astronomy in Hebrew

BERNARD R. GOLDSTEIN*

Introduction: Hebrew manuscripts are an important source for Arabic science, often containing texts that otherwise do not survive. Three types of texts can be distinguished: Arabic written in Hebrew characters, translations into Hebrew, and original Hebrew treatises based on Arabic models. In the areas where Arabic became predominant most Jews adopted it as their vernacular as well as their literary language. But beginning in the twelfth century, particularly in Spain, they began to use Hebrew for scientific and philosophical purposes. By the end of the middle ages we find such Hebrew texts being written in Spain, southern France, Sicily, Greece, and Turkey. Moreover, we find Arabic texts in Hebrew characters from these places as well as from Egypt, Syria, and Yemen. The study of this vast array of documents sheds

* The University of Pittaburgh (JS-2604 CL, Pittaburgh, PA 15260, U S. A.) and The Invitute for Advanced Study, Princeton.

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- 1 The best bibliographic study is still M Steinschneider's Mathematik bei den Juden published in a series of articles between 1893 and 1901 and reprinted in a single volume (Hildesheim, 1964). See also E. Renan, "Les écrivains juife français du XIV° siècle", in Histoire Littéraire de la France, Vol. 31, 1893.
- 2. (a) For Egypt we have a number of documents from the Carro Geniza. Ser, for example, B. R. Goldston and D. Pingree, "Horoscopes from the Carro Geniza", Journal of Near Eastern Studies 36 (1977), 113-144.
- (h) For Syria I have found only one astronomical text in Hebrew characters and it is from Aloppo, dated 1822 (Jewish Theological Seminary of Amarica (JTS 4), Ma. Ho. Micr. 2621, folios 1-23). The title is given in the colophou as Kitth al-tabjira. In fact, the text is Kitth al-tabjira ft "ilm al-hay" a hy sl-Kharaqi (d. 1138, 39 in Merv) as I determined by comparing the manuscript in JTSA with a manuscript in the British Library (BL). The beginning of JTSA Ms. Hb. Micr. 2621, fol. la, corresponds to BL Ms. Add. 23394, fol. 99b:3 (Part 2, chapter 1, in the middle); the end of the JTSA ms. (fol. 33a) terresponds to the end of the BL ms. (fol. 110s: end of Part 2, chapter 14). The colophou of the JTSA ms indicates that this copy was executed by David ben Joshua Mainann, Nagid of the Egyptin Jewish community and a descendant of Mainmonides, who left Egypti for Syria in the 1370s and is otherwise known to have been in Aloppo in 1375 and 1379 (Encyclopedia Judaca (1971), vol. 5, p. 1351). For a description of the Arabic text see E. Wiedemann, Aufsatse zur arabischen Wissenschaftugeschichie, vol. 2, pp. 634 ff. (Hildesheim, 1970), On al-Kharaqi, see also Encyclopedia of Islam, 2nd ed., vol. 4, p. 1059.

(c) For Yemen, see Y. Ratzaby, "The Literature of the Yemenite Jews," Knyat Sefer 28 (1952), 599-400 [in Hebrew]. Of special interest is British Museum Ms. Or. 4104, a Yemenite manuscript in Hebrew characters, which contains (1) an Arabic treatise on the motions of the run and the moon.

the theorem of Ptolemy concerning a cyclic quadrilateral. He also used an expression for the area of an oblique triangle inscribed in a certain manner in a right triangle (cf. [7]). Abū al-Wafā' exhibits no knowledge of al-Shannī's work, although we have seen in the introduction that it is just possible that the former was required to use a method different from one already known.

Thus we have exhibited four algorisms for the area of a triangle, and five distinct proofs Of course, by using algebraic techniques, it is not difficult to transform any one of the expressions into any other. But it must be remembered that similarities made obvious by algebraic symbols may not be apparent when the investigator is constrained to write out his rules in ordinary prose. This was the case with our ancient and medieval forebears.

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Combining (29) and (30),

$$\overline{AB^4} \cdot \overline{GB^3} = (\frac{\overline{AB} + \overline{BG^4} - \overline{AG^2}}{2})^4 = 2 \text{ area } \triangle ABG,$$

which is equivalent to (27a), hence (27).

The treatise closes with a curious passage (82v 36-38) in which the author remarks apologetically that areas should not be multiplied together, but that he has done so for the sake of simplication. His qualms are a vestigial remnant of the ancient geometrical algebra in which terms of the first degree represented line segments, quadratic terms areas, and cubic terms volumes. In his rules indeed many quartic elements appear.

The Background of the Problem

The earliest of the rules for calculating the area of a triangle in terms of its sides is the elegant

(31)
$$\sqrt{s(s-a)(s-b)(s-c)}.$$

where s is the semiperimeter. Although it is known as "Heron's Formula", its discovery is by Bīrūnī (in [1], transl., p. 39) attributed to Archimedes (c. 250 B.C.). However, Heron's "Metrica" (written c. 75 A.D.) contains a proof which employs the properties of the incircle, similar triangles, inscribed angles, and the properties of proportions ([4], vol. 2, pp. 34-35).

The same book proves a different rule, namely

$$\frac{c}{2} \sqrt{a^{1} - \left(\frac{c^{3} + a^{2} - b^{2}}{2c}\right)^{1}}.$$

This expression differs only slightly from Abū al-Wafā's third rule, (27) and Heron's proof is also strikingly similar, employing the same proposition from Euclid as does Abū al-Wafā'. Nevertheless, the latter does not mention Heron or anyone else in this connection.

Two proofs of formula (31) have been noted in the Arabic literature anterior to Abū al-Wafā'. The earlier (c. 875) is by the Banū Mūsā, and exhibits only trivial divergences from that of the Heronic Metrica ({2}, pp. 279-289).

The second is by a certain geometer named Abi 'Abdallah Muhammad b. Ahmad al-Shanni (c. 950). He uses the excircle, similar triangles, and a property of a broken line inscribed in a circle ([1], pp. 39-40). It is considerably more involved than Heron's proof.

In a different source the same al-Shanuï states and proves expression (1), Abū al-Wafā's first rule. The two proofs differ widely, for al-Shanuï applies

Two More Rules

After completing the proof, the text states that it is possible to calculate the area of a triangle by operations performed upon its sides as such. Expressed in modern symbols, the rule is

(26)
$$\frac{1}{4} \sqrt{((c+b)^3 - a^2)((c-b)^2 - a^2)}.$$
 (82v: 21-25)

No proof is given; perhaps it was felt that (1s) and (26) are sufficiently similar that proof of one suffices for the other.

The author goes on to say that there is yet another rule for the area of a triangle in which no altitude is employed; it is

(27)
$$\frac{1}{2}\sqrt{c^2a^3-\left(\frac{e^4+a^2-b^2}{2}\right)^4}$$
 (82v:26-28)

For this a proof is given. Before presenting it we restate the expression above in terms of the capital letters on the figure. The text has a separate figure but the previous one will serve.

To prove

(27a)
$$\frac{1}{2} \sqrt{\overline{A}\overline{B}^{1} \cdot \overline{G}\overline{B}^{2}} - (\overline{A}\overline{B}^{2} + \overline{G}\overline{B}^{2} - \overline{A}\overline{G}^{2})^{2} \quad \text{area } \triangle ABG$$

Proof:

$$\overline{AB}^{2} + \overline{BG}^{2} = A\overline{G}^{2} + 2 \cdot GB \cdot BD. \tag{82v:29}$$

This is Proposition 13 in Book 2 of Euclid's Elements ([5], vol. 1, p. 406).

Hence

(30)

(28)
$$BG \cdot BD = \frac{AB^{1}}{2} + \frac{BG^{2}}{2} - \frac{AG^{2}}{2}.$$
 (82v: 31)

Square both sides of (28) and subtract each side of the result from $\overline{AB}^a \cdot \overline{GB}^b$ to obtain

(29)
$$A\overline{B}^1 \cdot G\overline{B}^2 - \overline{B}\overline{G}^2 \cdot B\overline{D}^4 = A\overline{B}^3 \cdot \overline{G}\overline{B}^2 - \left(\overline{A}\overline{B}^2 + \overline{B}\overline{G}^2 - \overline{A}\overline{G}^2\right)^{1}$$
.

The left hand side of (29) is

$$(AB^{3} - \overline{BD}^{3}) \overline{BG}^{3} = \overline{AD}^{3} \cdot \overline{BG}^{3}$$

 $= (A\overline{D} \cdot \overline{BG})^{3}$ (82v:35)
 $= (2 \text{ area } \Delta ABG)^{3}$.

by application of the Pythagorean theorem to $\triangle ADB$, and the fact that AB is an altitude of $\triangle ABG$.

proportional, and the angle they enclose is common, the triangles are similar),

So angle BKY is a right angle (for triangle ZBT, similar to it, is inscribed in a semicircle).

Also
$$TZ/K[Y] = TB/BK$$

(The text has KB. The segments are corresponding sides of similar triangles. Squaring both sides),

$$TZ^2/YK^0 = TB^4/BK^0. \tag{82r:34}$$

Further.

(21)
$$(\overline{T}\overline{Z}^{2} - \overline{K}\overline{Y}^{2}) / \overline{T}\overline{Z}^{2} - (\overline{T}\overline{B}^{2} - \overline{K}\overline{B}^{2}) / \overline{T}\overline{B}^{2}$$
(since if $x/y = u/v$, then $(x-y)/x = (u-v)/u$,

But

(8)
$$TZ^1 - KY^2 = AD^2$$
. (82r:35, 82v:1)

(This is the second lemma).

Moreover,

(22)
$$\overline{TB}^{3} - \overline{BK}^{2} = \overline{B} L^{2}. \qquad (82v:1)$$

(The text has NL. To verify this, apply the Pythagorean theorem to triangle EBL to obtain $\overline{EB}^3 \to \overline{EL}^2 = BL^2$, and to this apply (2), (3), and (5).

So (applying (8), (22), and (2) to (21)

$$\bar{A}D^{3}/\bar{T}Z^{3} = \bar{R}L^{3}/\bar{R}\bar{E}^{3}. \tag{82v:2}$$

And (since AD is the altitude to side a and BE = a/2)

(23)
$$AD^{2} \cdot B\overline{E}^{1} = \text{area } ABG^{3} = \overline{T}Z^{2} \cdot \overline{B}\overline{L}^{2}.$$

Now

$$\overline{TZ}^{4} = \overline{R}\overline{Z}^{2} - \overline{R}\overline{E}^{4}. \qquad (82v:3)$$

(This follows by combining with (2) the Pythagorean expression

$$\overline{TZ}^1 = BZ^4 - \overline{B}\overline{T}^4$$
.)

Also

$$(25) \qquad \qquad \overline{B}L^{1} = \overline{B}E^{2} - \overline{A}Z^{1},$$

(which is obtained by combining with (3) the Pythagorean expression $\overline{BL}^3 = \overline{BE}^3 - \overline{EL}^3$).

(Substitution of (24) and (25) in (23) gives

(1a)
$$\operatorname{area} ABG^{2} = (BZ^{2} - \overline{BE}^{2}) (B\overline{E}^{2} - A\overline{Z}^{2}) \cdot O.E.D.$$
 (82v: 4)

Now

$$D\bar{E}^{i} - \bar{A}\bar{Z}^{i} = \bar{K}\bar{Y}^{i}.$$

(To demonstrate this, use (4) and (5) to write $DE^2 - \overline{AZ^2} = B\overline{Y}^2 - B\overline{K}^2 \approx YK^2$, the last by applying the Pythagorean theorem to triangle YKB. It is proved to be a right triangle at 82r:33 without invoking the second lemma, so the demonstration is not circular).

Also

(18)
$$B\overline{Z}^{1} - [\overline{B}\overline{E}^{2} = \overline{T}\overline{Z}^{1}]. \tag{82v:21}$$

(Here use (2) to put

$$BZ^4 - \overline{B}\overline{E}^4 = \overline{B}\overline{Z}^4 - \overline{B}\overline{T}^4 = \overline{T}\overline{Z}^4$$

the last by applying the Pythagorean theorem to triangle ZTB).

Finally, application of (17) and (18) to (16) yields

(8)
$$[\overline{TZ}^{1} -]\overline{K[Y]}^{3} = A\overline{D}^{1}.$$
 (82v:21)

(The text has KG. A copyist apparently left out the few words so indicated from line 21, but the intent of the author is clear).

Q.E.D.

The Main Demonstration

$$\overline{BZ}^{a} - \overline{BE}^{a} = \overline{TZ}^{a} \qquad (82x:30)$$

(By the Pythagorean theorem, $\overline{BZ}^i - \overline{TB}^i = \overline{TZ}^i$, and invocation of (5) yields (19),)

$$BE^{a} - \overline{AZ^{a}} = \overline{BL^{a}}. \tag{82r:31}$$

This follows from the Pythagorean expression $\overline{BE}^2 = \overline{EL}^1 = \overline{BL}^1$ and use of (3).)

The first lemma says

(6)
$$HB/BG = DE/AZ. (82x:31)$$

Hence

$$ZB/BE = DE/A[Z]. \tag{827:32}$$

(The text has AB. The expression follows from the fact that HB=2ZB and BC=2BE). And (by use of (2), (4), and (5))

(20)
$$ZB/BT = YB/BK$$
, (82x:32)

Hence

$$YK \mid \mid TZ$$
 (82r:33)

(since by (20) two pairs of corresponding sides of triangles ZBT and YBK are

The Second Lemma

To prove:

$$TZ^4 - \overline{Y}K^4 = A\overline{D}^4 \qquad (82v:15)$$

Proof:

(9)
$$BZ^{\mu} + ZA^{\mu} = 2(BZ\cdot ZA) + AB^{\mu}$$
 (82v:15)

(This is immediate upon equaring the identity BZ - ZA = AB).

(10)
$$2(B(Z_1 AZ) = BH AZ = BGDE.$$
 (82v:16)

(The text has BE. The first equality is a consequence of the fact that BZ = BH/2. The second equality is equivalent to Lemma 1).

$$AB^* = BD^* + DA^*$$

(by application of the Pythagorean theorem to the right triangle ABD).

(12)
$$BZ^{4} + Z\bar{A}^{4} = 2(BE \cdot ED) + B\bar{D}^{4} + \bar{D}A^{4}$$
 (82v:17)

(In the MS the first three terms are repeated. To obtain (12), note that by (10)

$$2(BZ\cdot AZ) + BG\cdot DE - \alpha \cdot ED = 2BE\cdot ED$$
,

and apply it and (11) to (5).)

But

$$2(BE \cdot ED) = 2(B[D] \cdot ED) + 2\overline{D}\overline{E}^2 \qquad (82v : 18)$$

(The text has BE. Multiply both sides of the identity BE = BD + DE by 2 ED to obtain (13).)

Also

(14)
$$B\overline{E}^4 - B\overline{D}^2 + \overline{D}E^2 + 2(BD \cdot DE)$$
 (82v:19)

(This may be obtained by squaring both sides of the identity above, BE = BD + DE).

So

(15)
$$\overline{BZ}^{1} + \overline{ZA}^{1} = \overline{AD}^{1} + \overline{BE}^{1} + ED^{1}$$

(obtainable by taking (12) and eleminating from it $2(BE \cdot ED)$ by the use of (13). There results $B\overline{Z}^3 + \overline{Z}A^4 = 2(BD \cdot ED) + 2\overline{D}E^0 + \overline{B}D^2 + \overline{D}A^3$. From the right hand side of this expression, pick the elements of the right hand side of (14), and substitute for them $\overline{B}E^3$, the left hand side of (14). There results (15).)

0r

(16)
$$B\bar{Z}^2 - \bar{B}\bar{E}^3 = A\bar{D}^3 + \bar{D}\bar{E}^3 - A\bar{Z}^2$$
 (82v:20)

to the relation between sides b and c. We have taken b > c, implying that both sides of expression (7) below are negative, a concept foreign to medieval mathematics. However, (7) is slightly musleading, for the Arabic word fadl does not translate precisely as "difference", but rather as "the excess (of one quantity over another)". The proof is valid under all circumstances.

Construction

For the proof the text prescribes (82r:28) the dropping of altitude AD to a, and the drawing of semicircles BTZ and BLE with bounding diameters BZ and BE respectively.

Next the laying out of four line segments is called for (82::29), all chords or portions of chords in the semicircles just drawn. They are:

$$(2) BT = BE$$

$$(3) EL = AZ$$

$$(4) BY = DE$$

(5)
$$[B]K = AZ \quad \text{(The text has } YK).$$

The First Lemma

To prove:

(6)
$$HB / BG = DE / AZ,$$
 (82v: 9)

Proof:

(7)
$$\overline{B}\overline{A}^2 - \overline{A}\overline{G}^1 = B\overline{D}^0 - \overline{D}\overline{G}^2, \qquad (82v:10)$$

since, (by the Pythagorean theorem)

$$B\overline{A}^{2} - \overline{B}\overline{D}^{2} = A\overline{D}^{2} = A\overline{G}^{1} - \overline{C}\overline{D}^{2}$$

(The above expression is evidently intended, but the passage is garbled and not easily restorable).

The right hand side of (7) is

$$\overline{BD}^2 - \overline{DG}^2 = (B[D] + [D]G) (B[D] - [D]G)$$

$$= BG \cdot 2DE,$$

(The text has at 82v:12 (BE + EG) (BE - EG), which is absurd).

The left hand side of (7) is

$$\overline{B}\hat{A}^{1} - \overline{A}[G]^{1} = (BA + A[G]) (BA - A[G])$$

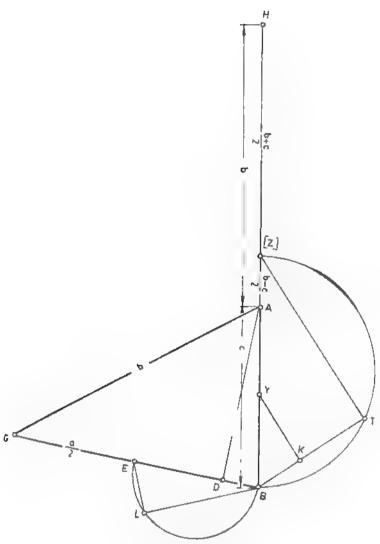
$$= (c+b)(c+b) = HB \cdot 2AZ.$$
(82v:13)

Hence

$$BG \cdot 2DE = 2AZ \cdot HB$$

whence

(6)
$$HB/BG = DE/AZ, \qquad (82v; 14)$$



Restored version of the text figure.

missing, and that the original version was a challenge to produce a proof different from one already current. Be that as it may, the verbal rule which follows is clear. Expressed in modern symbols it is

(1)
$$\sqrt{\left\{ \left(\begin{array}{c} c+b \\ 2 \end{array} \right)^3 - \left(\begin{array}{c} a \\ 2 \end{array} \right)^3 \left\{ \left\{ \left(\begin{array}{c} a \\ 2 \end{array} \right)^2 - \left(\begin{array}{c} c-b \\ 2 \end{array} \right)^3 \right\}} \quad , \quad (82r:21)$$

where a, b, and c are the lengths of the sides of an arbitrary triangle. Passages in the text will be identified, as is the expression above, by a pair of numbers separated by a colon, the first giving the number and side of the folio, the second the line.

For the demonstration which follows, a figure is utilized, transcribed on page 23 below. The Arabic letters of the MS have been replaced on our figure

by Latra characters according to the system given in [6].

To prove (1) Abū al-Wafā' makes additions to the figure and then, with the aid of two lemmas, goes through a long series of deductions which eventually yield what is desired. The next three sections below duplicate his argument, except that we have compressed his verbal statements into symbolic expressions, and whereas he leaves the proofs of the lemmas until after the main theorem has been disposed of, we prove the lemmas first.

The text has two more rules giving the area of a triangle in terms of its sides, there being a proof for the second rule of the two. This material also is

paraphrased by us below.

But, of course, the problem of determining the area of a triangle in terms of its sides is far older than Abû al-Wafâ'. It apparently reaches back to Archimedes, and between his time and the tenth century several rules and variant proofs were worked out. The concluding sections of our paper list these rules in approximate chronological order and discuss the relations between them.

Enunciation of the Theorem

In the triangle ABG, (82r:25, see our version of the figure) extend AB to H, making AH = AG = b. Bisect BH at Z and BG at E. It is to be proved that

(1a)
$$(\widetilde{B}\widetilde{Z}^1 - B\widetilde{E}^0) (\overline{B}E^0 - \overline{A}Z^1) = \overline{\operatorname{area}} A B\widetilde{G}^2 .$$
 (82r:27)

Since from the figure BZ = (c+b)/2, and

$$AZ = BZ - AB = \{(b+c)/2\} - c = (b-c)/2$$

expressions (1) and (1a) are equivalent.

In the text figure, which has apparently suffered at the hands of successive copyists and is grossly inaccurate, AB has not been extended, so no B appears. Where Z should be, a second D has been written (the cognate Arabic letters xa' and $d\delta l$ resemble each other). There is no indication in the text as

الله العواد ع الأرواع من بدفير دما الله أن منه الإمار ع المنظ عود عم أ المشيعة ع الآراي المنها م ذَانِ أَنْ يُطِّرُ فِعَدَتُهُ مَا فَيَ مِنْ عُ أَنْ السَّرَابُ * وَالْمُؤَامِّرُ ۗ أَذَى اللَّهُ عَلَم اللَّهُ صديدة جيدالة والم وورون من والمحلوم الدوسة على العادية علاوية عرامواره مزحة عن حالة تصرب العاش بسار ع وعدد المامع و كا عاد والساعدولللات الما وسيومه و شهد ال ALL THE PARTY OF T ومريوا المدوروا شعزو وعدائه مع مواساتي والمح الما المع المراب المراه والاثالة على وموالاً على المستان من المستان في المستان ا المستان ويستريب من سر هند من آواد وسائه والأوقاء المرابع المرا ن وريام دان المناح الله المعالم الله الله المناح أراح المناح المن و المناول و المناز المن وراري مروب المساورة من منظومهم والما تدويل من ومن عروب من المنظم . في أو مرسد دوة س مر على الشراس مر عاضاً مدة عاد المعداد العداد عيدا مرية الناج ل والمع المال توالود على وطورة المدين المورز والمدرج والمراكم المراكم المراكم والمراكم والمراكم المراكم المرا رياعور المنظال علاظ بداء دهون دارا ويدارما بالمعاص علادري ورا مسطان معالمة علمية وهو بواد ١٠٠ عند إلى أسراط رو من منا الموص الميدوالمدسط مربع الصلح المائية في عشاره براما طراط طريعا تعلى وديرية عاميه ومساوم الترج بد معلوب ومشهاد فيسر بالمعيد وساوفا بطوا والزارج فأصان فيوسترجماء عشاف وفليتكي رجية التالم المسابعة في الراء والماعة موعدة طور والشفط عير و داري ٥٠ وبالمارون التعطيا الأجابلا سلعس مراق في علوس لا برب ويوس مراعي والمعقعة وسله وينشياه ما عدل مر وروس والله من الما من الرحاط الدر واحدال الدراء لهديع المتاجه بزهر بالدالطون ، اجعا أسلت الحواجمة الدفلان مر في المتوسياول مرع الدوسوسية وتعارى وار توسلوس في سورة على الرائع ورية مي دارد الدا مشعه دان رب و ١٠٠ دا جال ال مؤماسع ال و وعراه واح أن سفاولز في الدائن حفوالده من المناج الأسد المرج عُ وَمِن الرَّامِلَةُ وَمَ عَلَى مِنْ عِلَمُ عَالَمَ عِلَّا وَمَ عِلْمَ عَلَى اللَّهِ مِنْ اللَّهِ اللَّ ولصروب كاويخ والمدناه والمراز القطعاص مزحرات المترم خرما وليد من مرتب ملا وخرها 35 اللافيمشا واللاطون مرامز عدا ومرج د ومرج الدوم ي عومز ع معت الماء طاور احد احد وطان وعد للستامة ودقاعه مادودان سيعي في وهيهما مر ومراسونع ن الرسال المرح ميه وصي افاهو عاملي الساوالوال مسعداد يكاح مان استطرع لاعب ان بصوب مصفياء على الماط من الله الداراليورة والما والما المتواج المائية المائرية الالتقار عد المد 1 10 2 to 1 - A 1,100 / - 40

من المعدد هداني معطد عدلي معطد حرق وروهاي و الطوير من و رواد المستخلف الما المستخلف المواد المدار المدارة الم

وطهد العالمة المراجعة المراجع

1,

من الماطاعي التدع الرحم اليم الطريق الراود على مجاليريا في المراف العديم المراف المرف المراف المراف

Abu al-Wafa' and the Heron Theorems

E. S. KENNEDY* AND MUSTAFA MAWALDI*

Introduction

MANUSCRIPT 4871 of the Zāhiriya Library in Damascus contains a number of Arabic translations of philosophical tracts from late antiquity. Several of these have been published. What is less well known is that the same manuscript includes many scientific works, in great part unique, and of ponsiderable historical interest.

This paper discusses the contents of one of them, a short treatise which covers most of a single folio only, 82, reproduced in facsimile here on pages 20 and 21 by kind permission of the librarian of the Zāhiriya.

Two individuals are mentioned at the beginning of the treatise, both being known to historians of the exact sciences. The first, the presumed author of the writing, is the famous Abū al-Wafā' al-Būzjānī (940-998), a mathematician and astronomer of Khurasanian origin who lived and worked in Baghdad ([3], vol. 1, pp. 39-43. Here and in the sequel, references enclosed in square brackets are to the numbered bibliography at the end of the paper. However, any square brackets which appear in algebraic expressions denote restorations of errors or omissions in the Arabic text of the MS).

The second is one Abū 'Alī al-Ḥasan b. Ḥārith al-Ḥubūbī, here called a canon lawyer (faqih), in other contexts given the title of judge ([11], p. 197; [10], p. 336). He was evidently a contemporary of Abū al-Wafā', as our text bears witness. Beyond this, Abū Naṣr Mansūr b. 'Irāq (m [9], p. 424) mentions a letter sent by Abū al-Wafā' to al-Ḥubūbī concerning some developments in spherical trigonometry. Al-Bīrūnī in his treatise on chords ([1], transl., p. 17), gives two proofs by al-Ḥubūbī of a certain theorem. Al-Kāshī ([8], p. 229) attributes to him a method of solving problems in the algebra of inheritances. Al-Kāshī calls him al-Khwārizmī, thus implying that he or his antecedents stemmed from the region south of the Aral Sea.

The Zāhiriya MS states that al-Ḥubūbī requested from Abū al-Wafā' a proof of the rule for calculating the area of a triangle without having recourse to an altitude. Here the text seems to be corrupt. It is possible that a clause is

[&]quot;The American Research Center in Egypt, 2 Maydan Quer al-Dubara, Cairo, Egypt, and the Institute for the History of Arabic Science, Aleppo University, Aleppo, Syris. That part of the study factied out at the ARCE was supported mainly by the Smithsonian Institution. The authors also acknowledge with gratitude assistance given them by Professors Adel Anbouba and M.-Th. Debarnot, who rescued them from an egregious blunder in restoring the text figure.

فقد تبيّن ما قلنا انه منى تحركت نقطة a بمحموع الحركتين المذكورتين حصل لها حركة مستوية بالنسبة الى نقطة د ومساوية في السرعة لحركة دائرة لـنم .

قاذا فرض البصر على نقطة ق من خط طج وفرض بعده من ط مساويا ١٩ لبعد نقطة ط من نقطة د فإن ً هذه الانعاد متى كانت مقاديرها على وفق الاقدار التي وضعها

[345]

بطلميوس لمعدي مركزي الحامل والمعدل من نقطة ق اعلى مركز العالم في واحد من الكواكب كان ما يظهر من هذه الحركات موافقا لما يظهر له بالارصاد . ولتكن هذه الكرة مغرقة في تبخى كرة محديها سطحان متوازيان مركزهما نقطة ك ، قتماس ١٧ سطحيها المتواربين بحيث يماس سطح المدير سطحيها الظاهر والباطن . وتسمى هذه الكرة الفلك الحامل .

فادا تحركت هذه الكرة دورة تامة رسم مركز المدير داثرة مركزها نقطة ك وهي الدائرة الوسطى المذكورة.

و ادا تحرك المدير على مركز ب رسم تدوير الكوكب اعني نقطة ه الدائرة الصعيرة التي في داخل كرة المدير اعنى دائرة اس» المذكورة .

فاذا تحرك الحامل تحركت نقطة ل محيط دائرة لدام الثالثه التي مركزها نقطة لئ حركة مستوية فأنها تدير ١٨ دلورانها كرة المدير . فيدور الدوران كوة المدير مركز التلوير على دائرة اس الصغيرة على مركزها اعي نقطة ل حركة مستوية ايضا ومساوية في السرعة لحركة نقطة ل .

قاذا انتقلت نقطة ل على دائرة لـنم الى ن ثم الى م في النصف الايسر من دائرة لـنام التقلت نقطة ع ثم الى نقطة ح . التقلت نقطة ع ثم الى نقطة ح . واذا تصورت هذا الامر على ما شرحاه فإنَّ مركز المدير ومركز التدوير على اي وضع فرضاه . ووصئنا خطوط كفات ، درع ص ، نعت الى محيط التدوير .

فاقول إن ْ خطَّي لئـ فن ، درع ص متوازيان .

درهانه ان قوس لـ من دائرة لـ نم تكون في جميع اوصاع نقطة لـ اعي ن من دائرة لهنم شبيهة بقوس فع من الدائرة الصغيرة . فزاويتا ملكن ، فنع متساويتان . فخطا كن دع متوازيان . فزاوية ادع مثل راوية لـ لكن ، فحركة بقطة ه اعني ع على مركز د شبيهة بحركة نقطة لـ اعنى ن على مركز كـ في اي وضع وزمان فرص .

لكن حركة نقطة ن على مركز لئا حركة مستوبة فحركة نقطة ع على مركز د عني مركز معدل السير حركة مستوية . وهذه الحركة التي حصلت لنقطة ع على مركز -حركة مركبة من حركتي نقطتي له اعني نء المستويتين .

۱۷ -- پاس ،

۱۸ - يدير ،

جورج صليبا 16

مركزها اقرب من النقطة التي عليها النصر من أجل أنَّ مركز التدوير يكون على هذه الدائرة في بعديه المختلفين اعني اعظم ابعاده من البصر واقربها منه .

وكوئها قريبا من محيطها في باقي ذروته حداً فللنك ظنَّ نظلميوس أنَّ مركز التدوير لازماً لمحيطها والله يرسمها بمحر كته .

١٤ لنضرب لذلك مثالاً ليطهر ظهورا بينا. فليكن دائرتان متساويتان في بسيط واحد متفاطعتان. الاولى منهما وهي يجعلها بطلميوس دائرة معدل المسير عليها ابجمر كزها؟ نقطة د. والثانية منهما وهي التي يجعلها الهلك الحامل لمركز التدوير دائرة هزح ومركزها نقطة ط. وليتقاطعا على نقطتي وي. ونصل خط دط المار بالمركزين وننفله في الجهتين الى عميلها. وليقطع دائرة ابجعلى نقطتي اجودائرة هزح على دح. ونقسم خط دط بنصفين على نقطة ك ونجعلها مركزاً وندير عبيها دائرة وببعد دا اعني نصف قطر لدائرة الاولى على نقطة له ونجعلها مركزاً وندير عبيها دائرة وببعد دا اعني نصف قطر لدائرة الاولى على نقطة له.

فنجعل نقطة ل مركز أ و بدير ببعد ال دائرة صغيرة عليها اس.. . قتماس ١٤ دائرة اسج م داخل على نقطة ا وتماس دائرة هزح من خارج على نقطة a . ولتكن١٩

[# 109]

نقطة من في النصف الايمن من الدائرة الصغيرة.

فمن البيتن أنَّ تصف قطر هذه الدائرة اعني مل يكون مساويا لحط دك اعني تصف الحط الذي بين مركزي دائرتي ابج ، هزح الاولتين

فاذا توهمنا أنَّ دائري ابج ، هزح الاولتين ثابنتين وان الكرة المحيطة بتدوير الكوكب يماس١٦ سطحها سطح التدوير يكون مركزها نقطة ل وتسمى هذه الكرة الفلك المدير للتدوير .

١٢ — النص ، من هـ وصاعداً ، هو عيته النص الذي ورد في نهاية الادراك لقطب الدين الشيرازي مع انبيرات طفيفة إلى تجرهمها .

١٢ - مگروي ١٤ - ليناس ،

٥١ - وليكن بيلي هذه الكلمة شكل مخدل (به مثل هذه الدوائر غير انه مرمور اليه على هامش الصفحة بدله إرة
 التالية بـ " هذا الشكل عطأ " , بدلك اعدنا رسمه حسب متضيات النص النظر (شكل با دار مق بهذا المقال .

75 – آباس ،

وتقطع هذه الدائرة كل واحدة" من الدائرتين الأولئين على نقطتين غير نقطتي تقاطع الدائرتين الاولتين .

فاذا جعدنا موضع قطع هذه الدائرة لاحد قسمي الحط الذي فيما بين الدائرتين مركزاً وادرنا عليه دائرة صغيرة تماس الدائرتين الاولتين ، فإن قطر هذه الدائرة يكون مساويا لبعد ما بين مركزي الدائرتين الاولتين .

فمثى تحرله مركز هذه الدائرة الصغيرة عبى محيط الدائرة الثائلة وهي الوسطى من الدوائر الثنئة المتساوية الى ان يصير وضعها على هذا الحفظ من الجهة الاخرى مقاطراً لهذا الوضع فإن الدائرة الصغيرة تصير ايضاً مماسة للدائرتين اللتين كانت مماسة لهما في الوضع الاول من داخل ومن خارج وبالعكس في الاخرى . داخل ومن خارج وبالعكس في الاخوى .

واذا توهم مركز فلك تدوير الكوكب محمولاً على محيط هذه الدائرة الصغيرة وفرضت متحركة على مركزها الله يقدلك مركزها البيها ، واما في القوس السفلى بالعكس وفرضت الحركتان المتساويتين الوفرضت الله الدائرتان المالولتان المائية بالعكس وفرضت الحركتان متساويتين الوفرضت الدائرتان المالولتان المائية بالعكس وفرضت الحط المار المراكز وبعده من مركز الحدى الدائرتين الاولتين الاولين مثل بعد ما بين مركز بهما . فاذا توهم مركز تدوير الكوكب على القطة التي تحارج الحيى التي مركزه القطة التي تحركتها القطة التي توضع عليها ثم تحركت الدائرة الصغيرة فحركت بحركتها القطة المماسة اعني مركز التدوير الى خلاف الجهة التي يتحرك مركزها اليها ، ويتحرك مركزها المماسة اعني مركز التدوير الى خلاف الجهة التي يتحرك مركزها اليها ، ويتحرك مركزها المماسة اعنى المائرة الحامل له . حصل لمركز التدوير بتحركها اعنى بانتقال

[109]

جملة الدائرة الصعيرة وبحركتها ايضا على مركز نفسها حركة مركبة من هاتين الحركتين يظنّ آنها بسيطة مستوية عند مركز الدائرة التي هي اكثر خروجاً عن موضع البصر وهي المسمّاة بمعدل المسير .

واما مركز التدوير اعنى نقطة المماسة المذكورة فقد يخال انه محمول على الدائرة الي

يه سايراسيد.

١٠ – الحركتين متماريتين

١٤ – الدائرتين الاراتين .

جورج صليها 14

لهنقم على خط اب خطي ۲ اج ، ب.د ويحيطان معه بالزاويتين الموصوفتين المتساويتين. ويوصل خط جد .

فاقول إنَّ جد مواز لحط اب . برهانه أنَّا نخرح خط اب على استقامة الى نقطة ه فإن كانت زاوية دبء الحارَّجة مساوية لزاوية جاب الداخلة على ما في الصورتين الاولتين ممن البيّن أنَّ خطّي اج ، بد المتساويين يكونان متوازيين . مخطا اب ، حد كدلك

واما إن كانت

[401]

الراويتان المتساويتان هما الداخلتين اللتين في جهة واحدة اعني زاوية جاب مساوية لراوية دباكما في الصورتين الناقبتين فنخرج من نقطة د خطأً موازياً لخط اج وليلقى خط اب على نقطة ني .

فمن اجل ان اج مواز ِ لدَّز تكون زاوية جاب مثل زاوية دره . فندلك تكون **دَرْب** مثل زاوية دبر . فخط دَرْ مُساو لحط دب اعلي اج ومواز ٍ له. فخط اب ، جد متوازيان . وذلك ما اردنا بيانه .



ومن ذلك ايضا أن كل دائرتين متساويتين يتقاطعان في نسيط مستو يوصل بين مركزيهما بحط مستقيم وينفذ في الجهتين الى محيطها ثم نعلم على نقطة عنى منتصف الحط الذي بدين مركزيهما وتجعل هذه النقطة مركزاً ويدار عليه دائرة يكون نصف قطرها مساويا لنصف قطر احدى^ الدائرتين الاولتين ، فان محيط هذه الدائرة يقطع كل واحدة من القطعتين اللتين تقعان من الحط المستقيم المار بالمراكز فيما بين محيطي الدائرتين بنقطتين نصفين .

۷ حد شطا

[.] A - lak .

وليس نتحقيق دلك طريق سوى الامتحان بالرصد في الوقت بعد الوقت . ولهذا يجب .ن تختار من الارصاد ما يقرب مناً زمانه لكيلا يكون القــــدر الدي يفوتها مضاعفاً مرات كثيرة .

ولما لم يكن لاهل زمانها وملوك عصرنا ومن له البسيطة ٢ رغبة في هذا العلم وقصر بنا تحن ضعف الحال و حمله العبال وقلة المساعد فلذلك لم نتكلم فيها من غير امتحان كما يفعل مصمور الزيجات بان يزيدوا او ينقصوا من عند انفسهم بلا دليل ولا حجة سوى جهلهم بالطريق التي استخرجت بها هده الامور . واتما حسر بهم على ذلك كولهم يرون الحسلات الواقع في كتب اهل هذه الصناعة فاختار كن واحد منهم اوساطاً من نفسه فوضعها .

فىڈلك صارت زيحاتهم على ما يرى من التناقض . ونعود الى كلامنا في افلاك الكواك نقول :

إن السبب الذي من اجنه صار مركز التدوير يرى انه محمول على فلك خارج المركز ويرى مسيره المستوي عند مركز فلك آخر غير الذي هو محمول عليه ان نقمة مركز التدوير التي يظن بطلميوس أبا بسيطة ليست كذلك . وانما هي حركة مركبة من حركتين بسيطتين مستويتين على مركز ين غير المركزين الموصوفين اعتي مركز الحامل ومركز معدّل المسير اللذين ذكرهما .

لكن فلك التدوير اذا تحرك بالحركتين اللتين سنوصحهما فانه سيحصل من تركيبهما حركة مستوية تحال انها نسيطة عند مركز معدّل المسير . ونقدم للملك تدكرة ً نافعة فنقول :

إِنَّ كُلُ خَطَّ مُسْتَقَيِّمُ نَقِيمُ عَلَيْهِ خَطِينٌ مُسْتَقِيمِينَ مُتَسَاوِيينٌ فَي جَهِةً وَاحَدَّةً فيصيران زاويتين من الزاويا التي تحدث مع الحط اما الداخلة مع الحارجة وأما الداخلتان اللتان في جهة واحدة متساويتين؟ ثم يوصل بين طرفيهما? بخط مستقيم فانه يكون موازيا المخط الدي قاما علمه .

۱ -- صححت على القابش

٧ - اليسلة في المخطوط .

۲ – مستقود

^{. 135 - 4}

ہ ۔ خطان مستقیمان متسویان

۴ ب عبارة مكررة

f.160r

by Ptolemy for the distances between the deferent center and the equant from point Q, i.e. the center of the universe, for any planet, then what appears of these motions will be in agreement with what appeared to him (i.e. Ptolemy) by observation.

Appendix

[۱۵۷ ظ] الما الهيئة الصحيحة التي يتهيأ بها اصابة ما يحرج بالارصاد ويشاهد بالعيان ويجري على الاصول الموضوعة من غير مخالفة لشيء منها فنحن مشتوها بابسط ما نقدر عليه . ونبير وضع الأكر التي تكون عنها الحركة السيطة المتصلة على أن حركائها مستوية عنها مراكزها ، والحركة المستوية هي التي يقطع المتحرك بها في الازمان المتساوية زوايا متساويسة عند مركز المحرك له ، والمختلفة هي التي ليست كذلك .

رينبغي ان تعلم أنّ إصابة مثل هذا الامر الجليل على الوجه الصواب في اعلى مراتـــب القوى الفكرية البشرية وهو تمام بالحقيقة للجزء المظري من التعافيم .

والذي ينبعي أن يسلمه الناحث في هذا العلم هي الارصاد القديمة التي يظن بها الصحصة مثل أرصاد ابرخس ويظلميوس أذ كان تمن يوثق بعلمهما وعملهما . فلنسلم ما أورداه من هذه الارصاد وهي التي عديها كان يعمل هو أيضاً وعليها عمل حسابه الذي أخرجه بطريق [١٥٨ و] الخطوط والاوساط وهي المنتزعة من أزمان الادوار .

فاما الزمان الدوريّ ومقدار مسير كل كوكب في يوم يوم بالوسط والحاصة فسيان تحقيقه موقوف على الامتحاد فلا يصار اليه نعيره . واصابته بغاية التدقيق يعسر بل لا يمسكن ان يدرك على الاستقصاء بحيث لا يفوت فيها ولا القدر اليسير . ومنى فات فيها مقدار مساوان قليّ قانه اذا مرّ عبيه زمان طويل طهر طهوواً بيسًا ويزداد كلما طالت عليه المدة . then its center will be point L and the sphere will be called the director (almudir) sphere of the epicycle.

Let this sphere be sunk into the thickness of (another) sphere whose curved parallel surfaces are around center K, so that it is tangent to its parallel surfaces in such a way that the surface of the director is tangent to its outer and inner surfaces. That sphere is called the carrier sphere (i.e. deferent).

When this aphere makes a full revolution the center of the director will then describe a circle whose center is point K, and that is the (above-)mentioned middle circle.

And as the director moves around center L, the epicycle of the planet, i.e. point E, will describe the small circle which is inside the sphere of the director, i.e. the (above-)mentioned circle ASE.

Now if the deferent moves uniformly, point L will move along the circumference of the third (circle) LNM whose center is point K. It will then move through its motion the sphere of the director. With the motion of the director sphere the center of the epicycle will also uniformly move along the small circle ASE and around its center, i.e. point L, at the same speed as point L.

So if point L moves along the circle LNM to point N and (then to) M on the left-hand side of circle LNM, then point E will move on circle ASE on the right-hand side to point O, then to point H.

Now if you imagine the situation as we described it, let the center of the director and the epicycle be at any assumed position. Then we join lines KFN, DZOC, and NOR to the circumference of the epicycle.

Then I say that the two lines KFN (and) DZOC are parallel.

Its proof is that arc LN of circle LNM in all positions of point L, i.e. N of circle LNM, is similar to arc FO of the small circle. Then the two angles EKN and FNO are equal. And lines KN and DO are parallel. Then ADO = angle LKN. And the motion of point E, i.e. O, around center D is similar to the motion of point L, i.e. N, around center K at any assumed time and place.

But the motion of point N around center K is uniform, hence the motion of point O around center D, i.e. the center of the equant, is uniform. This resulting motion of point O around center D is composed of the two uniform motions of points L and E, i.e. N and O.

That demonstrates what we said, that if point E moves with the sum of the two motions mentioned (above), it will have a uniform motion with respect to point D and equal in speed to the motion of circle LNM.

If the eye is assumed to be at point Q of line TG, and its distance from T were to be equal to the distance of point T from point D, then these distances, when their values are of the same quantities assumed (over a millenium before)

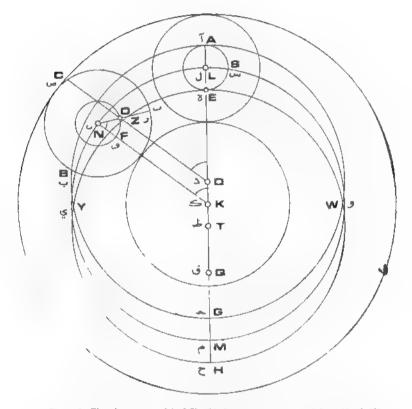


Figure 2. The planetery model of Shaykh Imam as reconstructed from Marsh 621.

by as much as the distance between the two centers, and if the center of the epicycle of the planet were imagined to be at the point where the small circle is externally tangent to the one of the two original circles whose center is closer to it, then if the small circle moves and with it the point of tangency, i.e. the center of the epicycle, in the direction opposite to that of the motion of the center. And if the center moves with the motion of its deferent, then the center of the epicycle moves with its motion, i.e. with the motion

f. 159r

of the small circle and its own motion on itself, in a motion composed of these two motions in such a way that it is thought to be simple and uniform at the center of the circle that is more eccentric from the eye, which is called the equant.

As for the center of the epicycle, i.e. the point of tangency mentioned above, it looks as though it were carried along the circle whose center is closer to the point of sight, on account of the fact that the center of the epicycle will be on this circle at its two distances, i.e. its farthest distance from the eye and its closest distance to it. And since it is very close to its circumference at the remaining portions of its distances (dhurvon), that has led Ptolemy to believe that the center of the epicycle is coincident with its circumference, and it describes it with its motion (Fig. 2).

Let us give an example to illustrate (that) very clearly. Let there be two equal circles intersecting in the same plane. The first of them, which is called the equant by Ptolemy, has points ABG on it and its center is point D. The second, which he calls the sphere carrying the center of the epicycle (i.e. deferent), is circle EZH with center T. Let the two (circles) intersect at points W and Y. We join the line DT that passes through the centers and produce it to the circumference on either side. Let it intersect circle ABG at the points E (and) H. We then bisect line DT at point K and with it as a center we draw a circle with a distance DA, i.e. the radius of the first circle, and (mark) in it points L, N, (and) M. It will bisect each of the two lines AE and GH at points L and M.

With point L as a center and with distance AL we draw circle ASE. It will be tangent to circle ABG internally at point A and tangent to circle EZH externally at point E. Let

f. 159v

point S be on the right-hand side of the small circle.

It is obvious then that the radius of this circle, i.e. EL, is equal to line DK, i.e. half the line connecting the centers of the first two circles ABG and EZH.

If we then assume that the first two circles ABC and EZH are fixed, and that the sphere surrounding the epicycle of the planet is tangent to the epicycle,

But if

158v

the two equal angles were the interior ones that are on the same side, i.e. angle GAB = DBA as in the remaining two cases, then we produce from D a line parallel to AG and let it meet line AB at point Z.

Since AG is parallel to DZ then angle GAB = DZE. Therefore DZB = DBZ and line DZ = DB, i.e. AG and is parallel to it.

Then the two lines AB and GD are parallel, and that is what we wanted to show.



In the same way, if two equal circles intersect on a plane surface and their centers are joined with a straight line that is produced in both directions to their circumference, and if we mark the midpoint of the line joining their centers and make it a center of a circle whose radius is equal to the radius of either of the two circles, then the circumference of this circle cuts the two segments of the straight line that is between the two circumferences of the two circles at their midpoints.

This circle intersects each of the two circles at two points other than the points of their original intersection.

If we make the point at which this circle cuts the two segments that are between the two circumferences a center and with it draw a small circle tangent to the two original circles, then the diameter of this circle is equal to the distance between the centers of the two original circles.

When the center of the small circle moves along the circumference of the third circle, which is the middle one of the three circles, until it reaches the diametrically opposite position on this line, then the small circle will also be tangent to the two circles to which it was tangent in the previous position, internally and externally, so that it will be externally tangent to the one to which it was internally so, and conversely with the other circle.

If one were to imagine the center of the epicycle of a planet to be carried on the circumference of this small circle, and (the circle) itself were assumed to be moving around its center in the direction of the zodiacal aigus on the upper arc, i.e. the direction of the movement of the center, and in the reverse on the lower arc, and if the two motions were equal and the two original circles assumed to be fixed, and the eye (basar) were assumed to be on the line that passes through the centers and distant from the center of one of the two circles

hān) and is not obtainable otherwise. Its accurate determination is very difficult and rather cannot be achieved with high refinement (istiqṣā") in a way that no slight inaccuracy is incorporated into it. And when any amount (of error) is incorporated into it, even if it be small, it will become quite apparent after the passage of time and will increase as the time increases.

The verification of that can only be achieved through testing by observations time after time. For that reason we must select the observations that are close to us in time so that the amount that we miss (i.e. the error) does not get multiplied several times.

And since our contemporaries and the kings of our times and those who have the authority have no bent toward this science, and we ourselves are lacking on account of our weakness and the expenses of our dependents and the lack of a helper, we did not say anything about it (i.e. observation) without testing as would the authors of sijes do when they add and subtract on their own without any evidence nor do they have any proof except their ignorance of the method by which these things are derived. They are (encouraged?) to do so by what they see of the variations in the books of the people of this science and hence each of them selects mean motions for himself and sets them down.

For that reason the contradictions in these zijes are obvious. But let us return now to our discussion of the planets and say:

The center of the epicycle appears to be carried by an eccentric sphere, and its motion appears to be uniform with respect to the center of a sphere other than the one by which it is carried on account of the motion of the epicycle center which Ptolemy thinks is simple, but it is not so. (On the contrary) it is composed of two equal and uniform motions around two centers other than the ones described above, i.e. the centers of the carrier (deferent) and of the equant that he had mentioned.

But when the center of the epicycle moves with the two motions that we will describe the resulting uniform and composite motion will look as if it is simple with respect to the center of the equant.

Let us then introduce that with a useful reminder (tadhkira) by saying: Every straight line upon which we erect two equal straight lines on the same side so that they make two equal angles with the (first) line, be they alternate or interior, if their edges are connected, the resulting line will be parallel to the line upon which they were erected.

Erect on line AB the two lines AG and BD so that they surround with it the two equal angles described (above). Let line GD be connected.

Then I say: Line GD is parallel to line AB. Its proof is to produce AB to E. Then if the exterior angle DBE is equal to the interior angle GAB as in the first two cases, it is obvious that the two equal lines AG and BD are parallel.

"Some of the esteemed modern workers in this science (sinā a) say in this place: If something is to be taken as a reference point for any motion, it must be stationary with respect to the moving thing so that motion will be due only to the moving body as it draws away from it or comes close to it."

This same statement is made by Shaykh Imam in Marsh 621 in the relevant discussion of the moving center of the lunar deferent and which he uses as his own axiom to begin his new model. Furthermore, Quth al-Din, as usual, taken issue with this statement, hence proving that the author of Marsh 621 is a different person. In addition, this demonstrates that the work of Shaykh Imam was available to the Maragha scholars and was actually incorporated into their works.

In what follows we give a translation of the text appended to this paper, from Marsh 621. fol. 157v-160r, attempting to be as literal as possible, only inserting a few explanatory words in brackets here and there to facilitate comprehension on the part of the reader.

Translation

f. 157v

As for the correct astronomy which agrees with what is obtained by observation and is apparent to the eye and (also) agrees with the accepted principles without any variation, we will explain it in the simplest way we can. We will also show the position of the spheres, which produce the continuous simple motion that is uniform with respect to their centers. The uniform motion is the one through which the moving (body) describes equal angles at the center of its mover in equal times. The non-uniform one is the one that is not so.

You must know that achieving such a momentous result in a correct fashion is of the highest human intellectual degrees and it is actual perfection of the theoretical part of the mathematical (sciences).

The researcher ought to accept in this science the ancient observations that he thinks are true, such as those of Hipparchus and Ptolemy, for they were trustworthy in knowledge and in practice. Let us accept what they have recorded by way of observations through which he (i.e. Ptolemy) himself used to work and upon which he based his computations, that he derived through

£. 158r

geometry (khutūt), and mean motions that are taken from periods of revolution. As for the period of revolution and the daily motion of the planet in mean longitude (wasat) and in anomaly, its verification depends upon testing (imperiods).

S. We transcribe here the text from Marsh 621, fol. 124v:1-3, to facilitate the computison.

ا إن الشيء الذي بفرض علامة لمبدأ حركه منه, لله يحب انه يكون ساكناً بالنسبة الى المنحرك بسكون الشيء الذي بفرض علامة المناطقة ا

this paper. We summarize here the tentative results reached so far and reported in the article mentioned above.

The author of Marsh 621, at this stage, can be called al-Shaykh al-Imam as the scribe refers to him on fol. 126r. He must have lived between 1138 A.D. and 1272 A.D.

Shaykh Imam did not participate in the activities of the Maragha observatory, for he says that he has no access to new observations. Hence he was probably writing before 1259. This author suspects that Shaykh Imam was not Mu'ayyad al-Din al-'Urdi, a likely candidate.*

Shaykh Imam was not known to Ihn al-Shatir except through the works

of Outh al-Din al-Shirazi.

And finally, it is highly probable that the "Tusi couple" grew out of Imam's

model as a logical consequence.

Due to the historical significance of this source, this author has undertaken a full transcription of it, but will give here only the relevant section on the planetary model with an English translation for the benefit of the reader who is not familiar with Arabic.

Quib al-Din and Shaykh Imám

The first reading of Marsh 621 revealed the identity of Shīrāzi's planetary model and that of Shaykh Imām. A first working hypothesis, however, was to assume that Marsh 621 was some earlier work of Shīrāzī reproduced in the Nihāyat al-'idrāk of Quth al-Dīn in a different format. That hypothesis ran into immediate problems, for the author of Marsh 621 is referred to as deceased by 1272 A.D., as was already noticed by Goldstein and Swerdiow, whereas Quth al-Dīn was still writing in 1281 A.D. and lived till 1311 A.D.

The task remained, however, to prove beyond doubt that the phrase quddosa 'Allahu rāḥahu (May God bless his soul) is to be taken literally, and hence to establish Shaykh Imām as different from and earlier than Qutb al-Din.

Hence it was necessary to examine the work of Qutb al-Din with this question in mind. The present writer did so, braving Qutb al-Din's "exasperating traits" of prolixity and repetition, coming upon the following passage of the Nihāyat al-'idrāk:

^{3.} These results were first reported on December 12, 1978, to a commentary read at the Boston Collequium for the Philosophy of Science. The full text of the commentary will be published in the proceedings of the Colleguium.

^{4.} Op. cit., p. 146.

Note added in proof: In an article appearing in Isis the present author has now established that al-Shaykh al-Imām was indeed al Drdî (d. 1256) and that the text preserved in Marsh 621 was written before the building of the Maragha observatory in 1259.

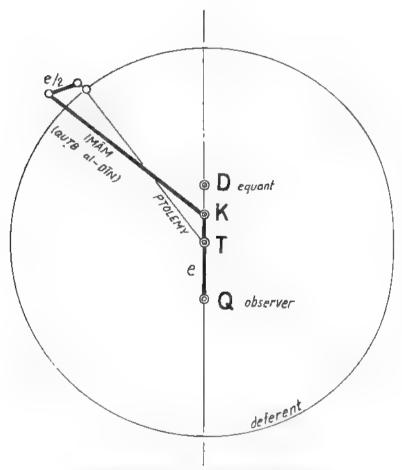


Figure 1. Sketch (not to scale) illustrating the two models,

The Original Source of Qutb al-Din al-Shirazi's Planetary Model

GRORGE SALIBA*

Introduction

A STUDY' published some twelve years ago reviewed the information then available concerning late medieval planetary theory. In this article, more space was devoted to the work of Qutb al-Din al-Shīrāzī (fl. 1280 A.D.) than to any other individual. The model he uses for all the planets except Mercury differs from those of his contemporaries, Naşīr al-Din al-Ṭūsī and Ibn al-Shāṭir. It was then remarked that perhaps the unique feature of Qutb al-Dīn's arrangement had not been invented by him, but had been inherited from a predecessor.

This paper introduces a text,² anterior to that of Quib al-Din, in which the distinctive device is fully described and motivated. As such, it constitutes the earliest successful effort thus far discovered to eliminate a supposed fault in the Ptolemaic system. It was a belief widely held in antiquity that the motion of any celestial body must be circular and uniform, or a combination of uniform circular motions. Ptolemy's equant device (see Fig. 1 below), although imposed by the facts of observation, violated this principle. The mechanism here explained conforms fully to the requirement of uniform circularity, retains the effect of the equant and yields predictions differing only slightly from those obtainable with the Ptolemaic model.

In a separate article, the involved problem of authorship and priority as well as the relationships among the members of the "Maragha School" has been treated in some detail, and further research is still going on to unravel the intricate relationships and historical questions involved. Nevertheless, there seems to be no way in which future research can change the thesis of

^{*}Department of Near Eastern Languages and Literature, Faculty of Arts and Sciences, N. Y. U., Washington Square, New York City 10803.

^{1.} E. S. Kenpedy, "Late Medieval Planetary Theory", Isis, 57 (1966), 365-378.

^{2.} Bernard R. Goldstein and Noel Swerdlow, "Planetary Distances and Sizes in an Anonymous Arabic Treative Preserved in Bodleian Me. March 621", Contaurus, 15 (1970), 135-176. The author windes to thank Prof. N. Swerdlow of the University of Chicago for hydraging this Ms to bis attention. The author is also indebted to the courtesy of Prof. B. Goldstein of the University of Pittsburgh for Mawing him to investigate this manuscript.

ARABIC SECTION

Article

ADEL ANBOUBA: A Treatise of Abū Jatfar al-Khāzin on Rational Right
Triangles

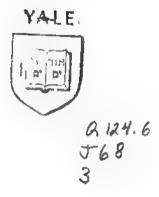
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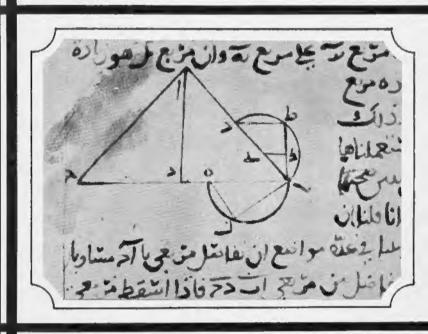
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